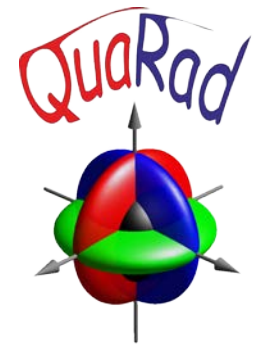




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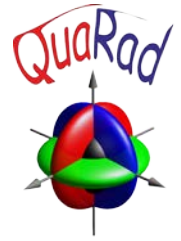
# Photon triplet generation in photonic crystal fibres

Andrea Cavanna, C. Okoth, M. Frosz, G. Leuchs,  
M.V. Chekhova, N. Y. Joly, and Philip St.J. Russell

MPL Erlangen, Germany



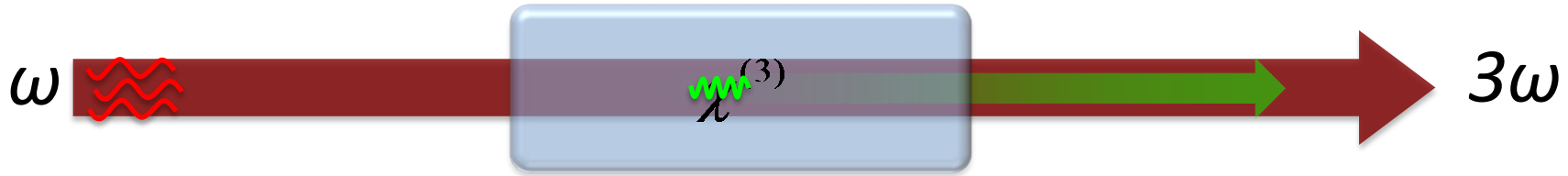
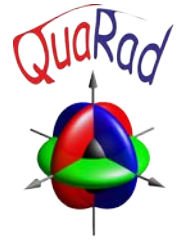
# Outline



- Photon triplet generation
- Introduction
- Tapered fibre
  - Motivation
- Hybrid solid core fibre
  - Wigner function
  - Structure
- Hollow core fibre
  - Characteristics
  - Structure
- Summary – Conclusions
  - Third-harmonic generation
  - Photon triplet phase matching
  - Third-harmonic generation
  - Photon triplet phase matching



# Introduction



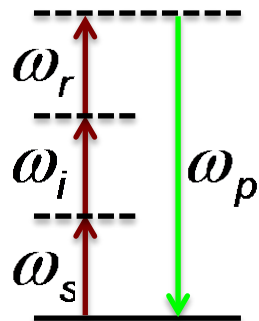
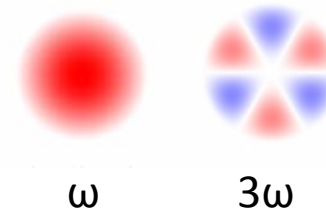
Third harmonic generation:

$$P_{3\omega} \propto \gamma^2 L^2 P_{\omega}^3 \text{sinc}^2(\Delta k L / 2)$$

$$\gamma \propto \chi^{(3)} J_3$$

Overlap integral:

$$J_3 = \iint_{A_{NL}} (F_{\omega}^* \cdot F_{3\omega})(F_{\omega}^* \cdot F_{\omega}^*) dS$$



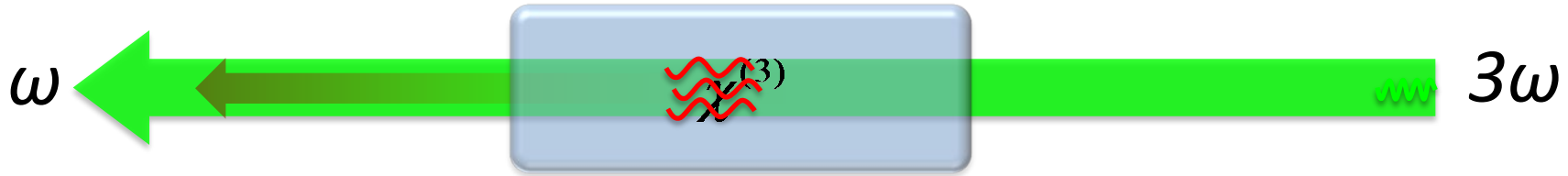
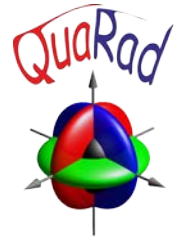
Energy and momentum conservation:

$$\Delta k = k_p - k_s - k_i - k_r = 0$$

$$\omega_p = \omega_s + \omega_i + \omega_r$$



# Introduction



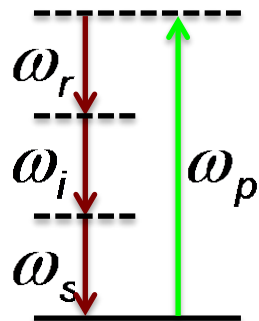
Third harmonic generation:

$$P_{3\omega} \propto \gamma^2 L^2 P_{\omega}^3 \text{sinc}^2(\Delta k L / 2)$$

$$\gamma \propto \chi^{(3)} J_3$$

Triplet generation:

$$P_{\omega} \propto \gamma^2 L^2 P_{3\omega} \text{sinc}^2(\Delta k L / 2)$$



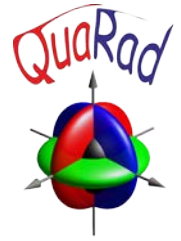
Energy and momentum conservation:

$$\Delta k = k_p - k_s - k_i - k_r = 0$$

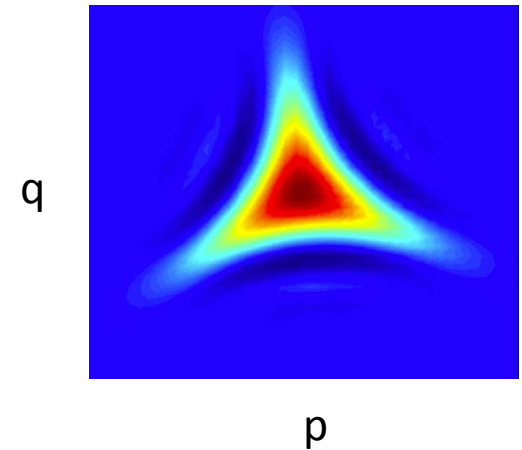
$$\omega_p = \omega_s + \omega_i + \omega_r$$



# Motivation

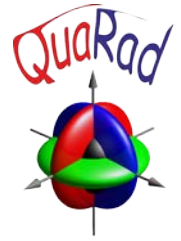


- Novel effect
- Non-Gaussian squeezed state
- Wigner function negativity
- Quantum information
  - Heralded two photon source
  - Three-party quantum secure direct communication





# Wigner function



Two photon state:

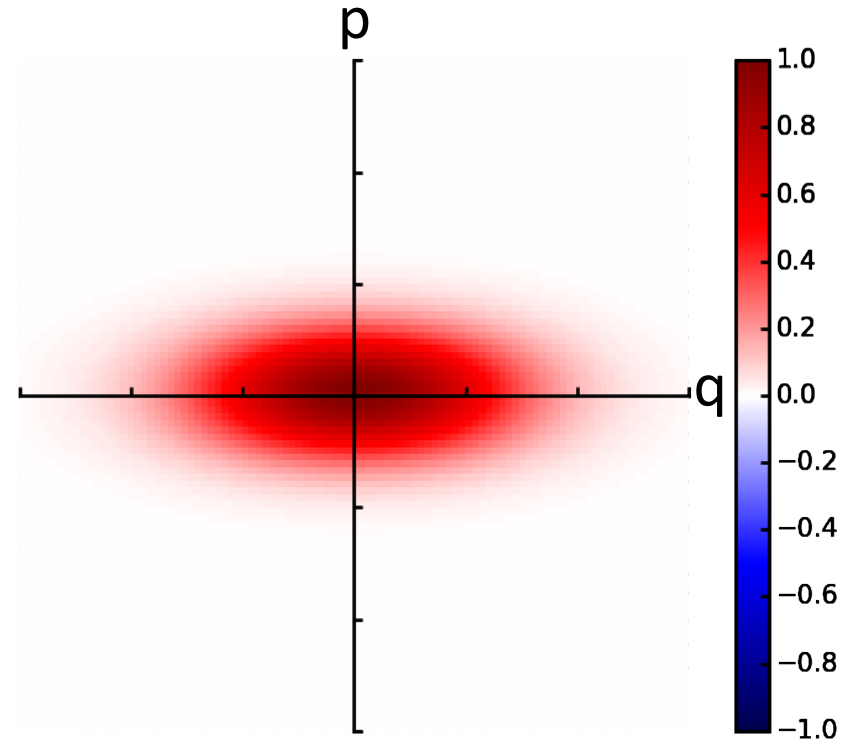
$$|\psi\rangle = c_0 |0,0\rangle + c_1 |1,1\rangle + \dots$$

Equations of motion:

$$\frac{dq}{dt} = 2\Gamma q$$

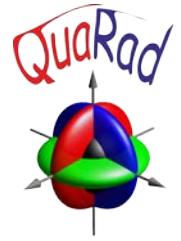
$$\frac{dp}{dt} = -2\Gamma p$$

$\Gamma$ : parametric gain





# Wigner function



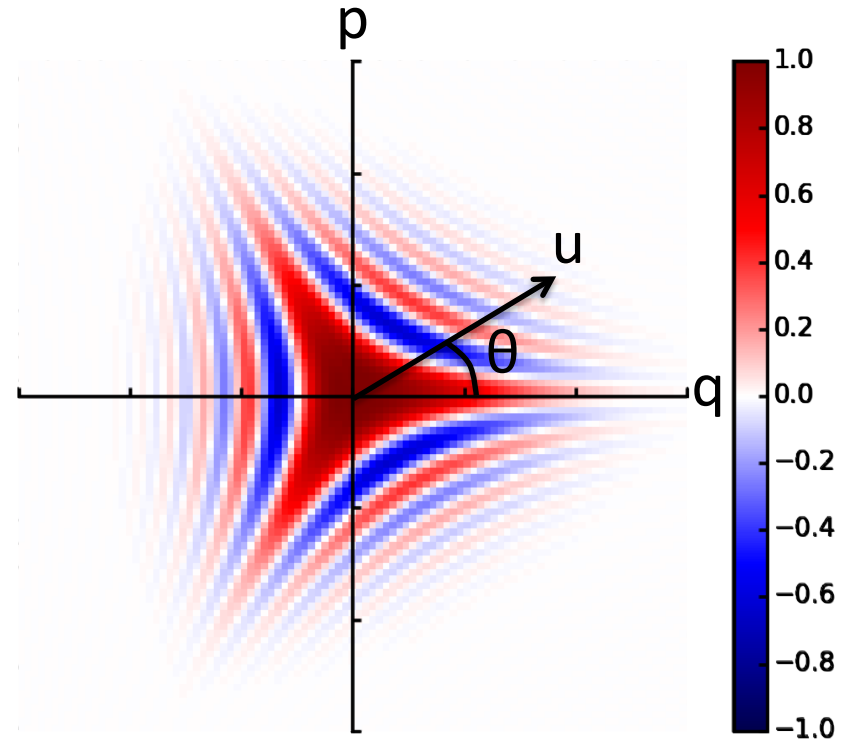
Three photon state:

$$|\psi\rangle = c_0 |0,0,0\rangle + c_1 |1,1,1\rangle + \dots$$

Equations of motion:

$$\frac{du}{d\tau} = 3u^2 \cos(3\theta)$$

$$\frac{d\theta}{d\tau} = -3u \sin(3\theta)$$

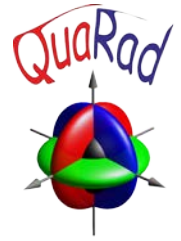








# Challenges

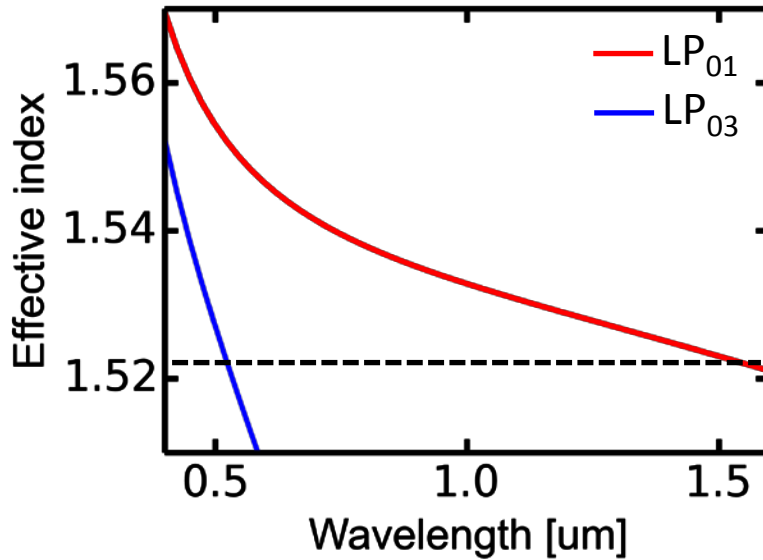
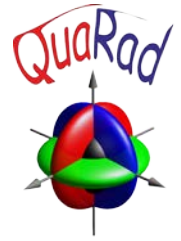


$$P_{\omega} \propto (\chi^{(3)} J_3)^2 L^2 P_{3\omega} \text{sinc}^2(\Delta k L / 2)$$

- $\chi^{(3)}$  : high values of nonlinearity also correspond to high absorption and luminescence
- $J_3$  : can be strongly reduced in case of inter-modal phase-matching



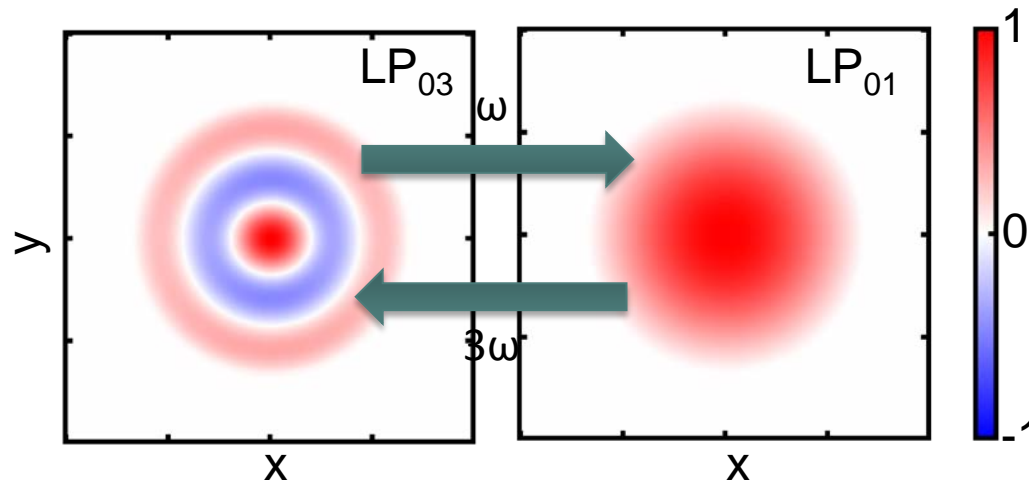
# Inter-modal phase-matching



$$\Delta k = 0$$

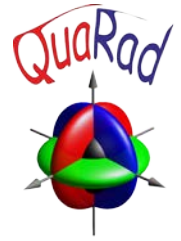
$$k = n_{\text{eff}} \frac{\omega}{c}$$

$$n_{\text{eff}}(\omega) = n_{\text{eff}}(3\omega)$$





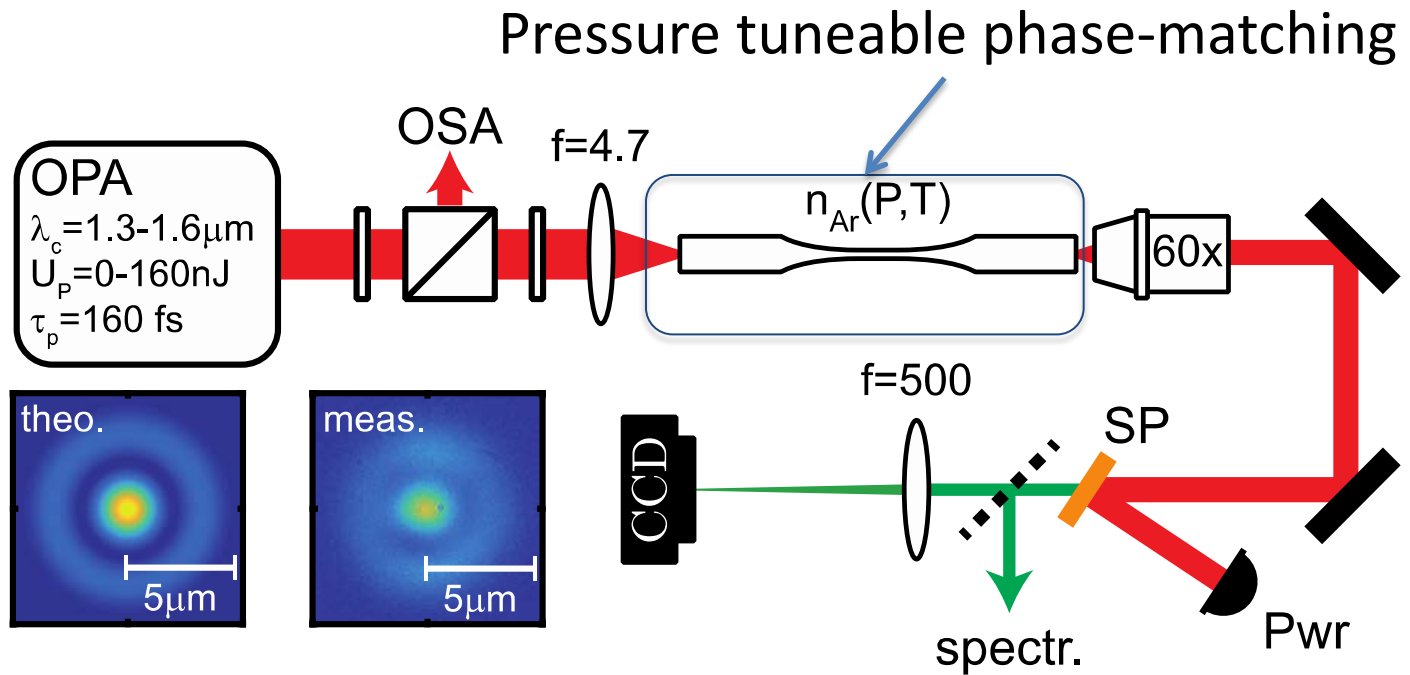
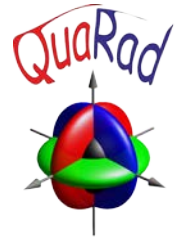
# Fibre types



- Tapered fibre → High overlap integral and ‘tuneable’ phase-matching.
- Hybrid fibre → High overlap integral between Gaussian-like modes.
- Hollow core fibre → Tuneable phase-matching and high damage threshold.

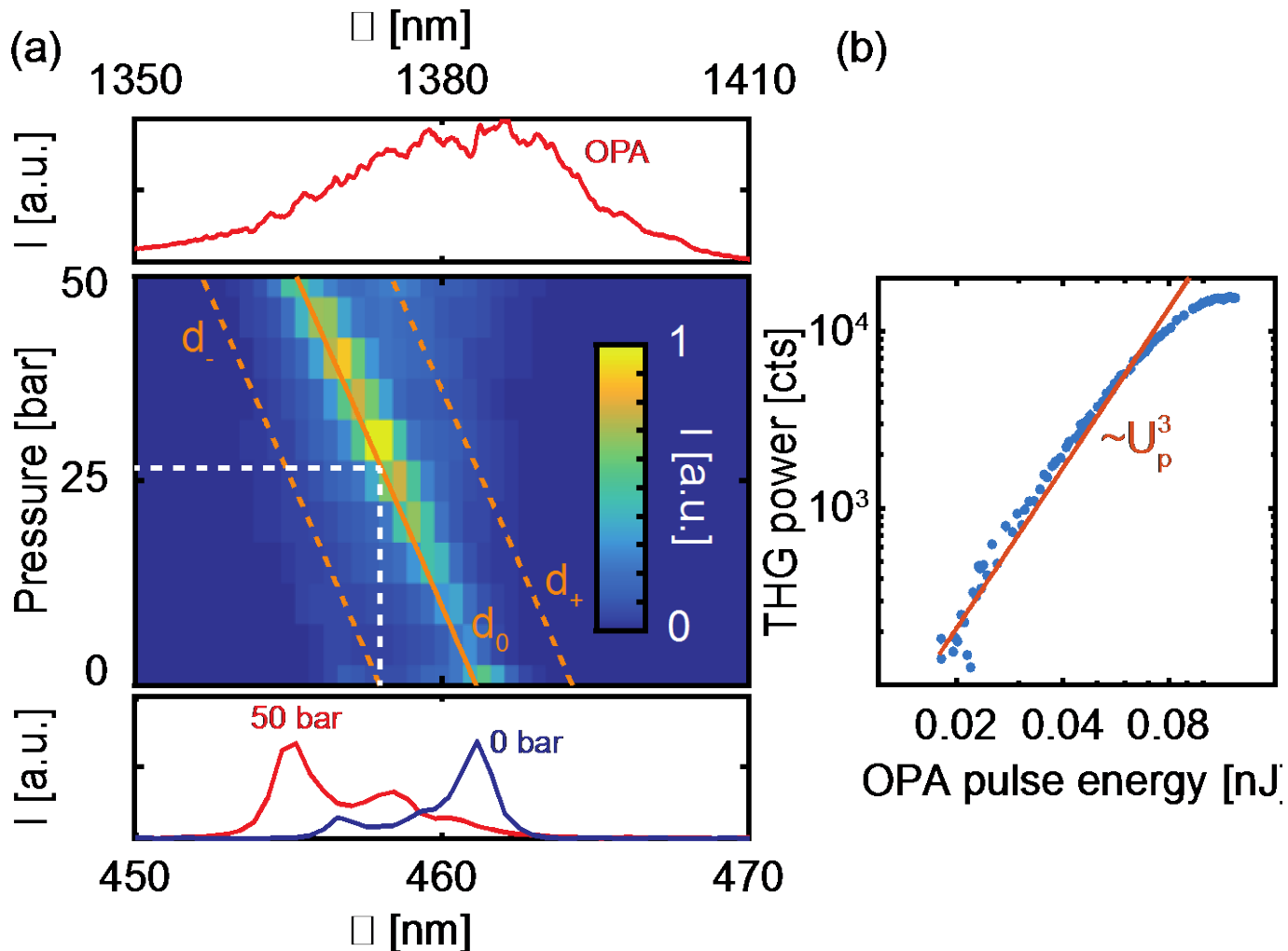
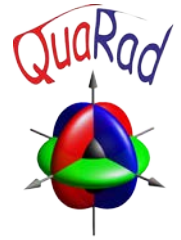


# Tapered fibre



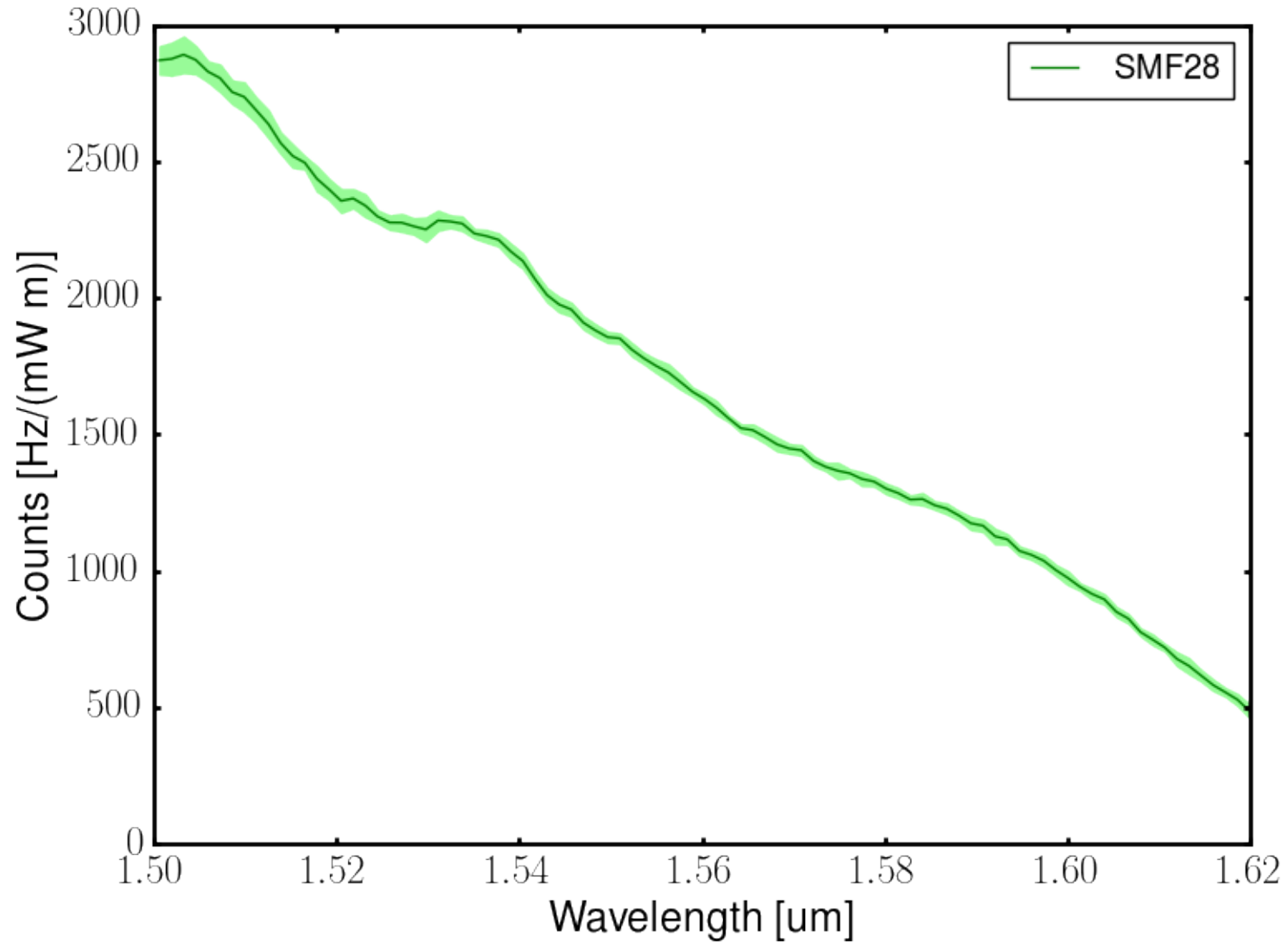
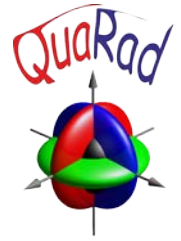


# Tapered fibre



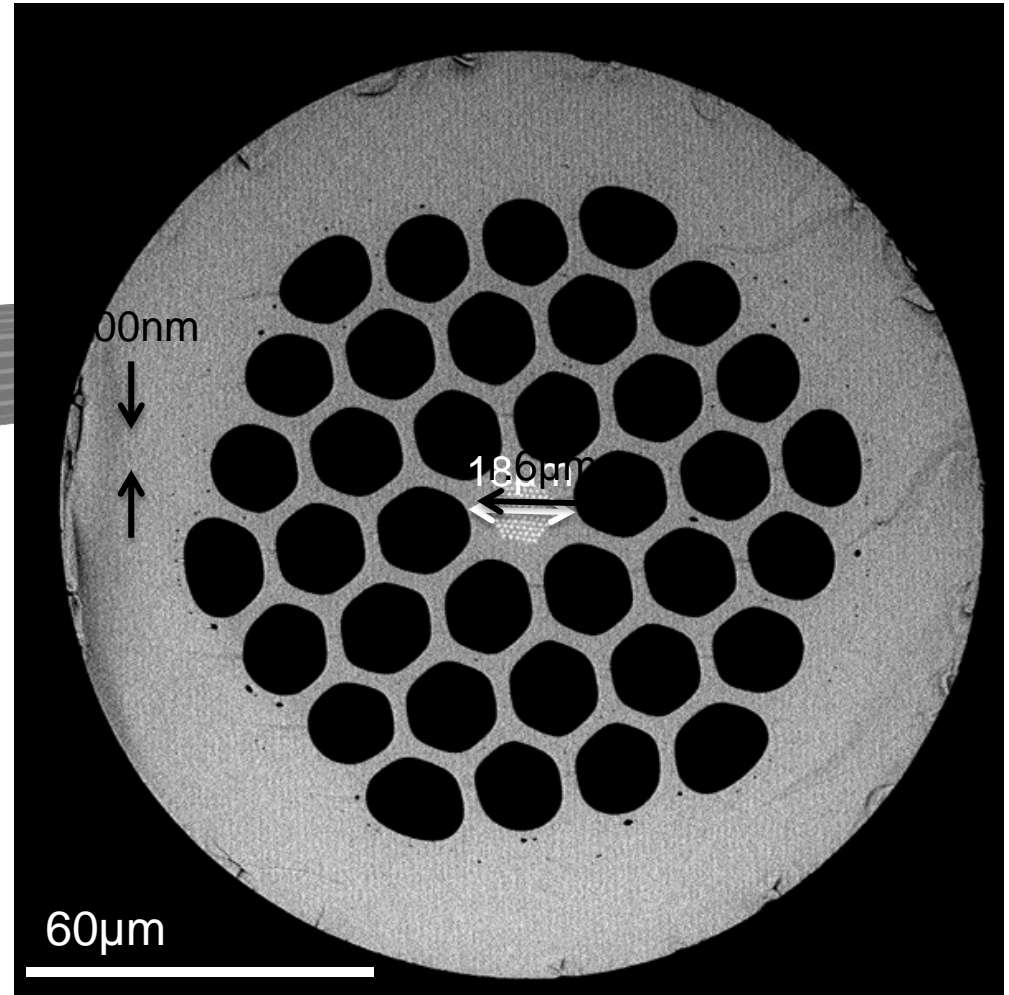
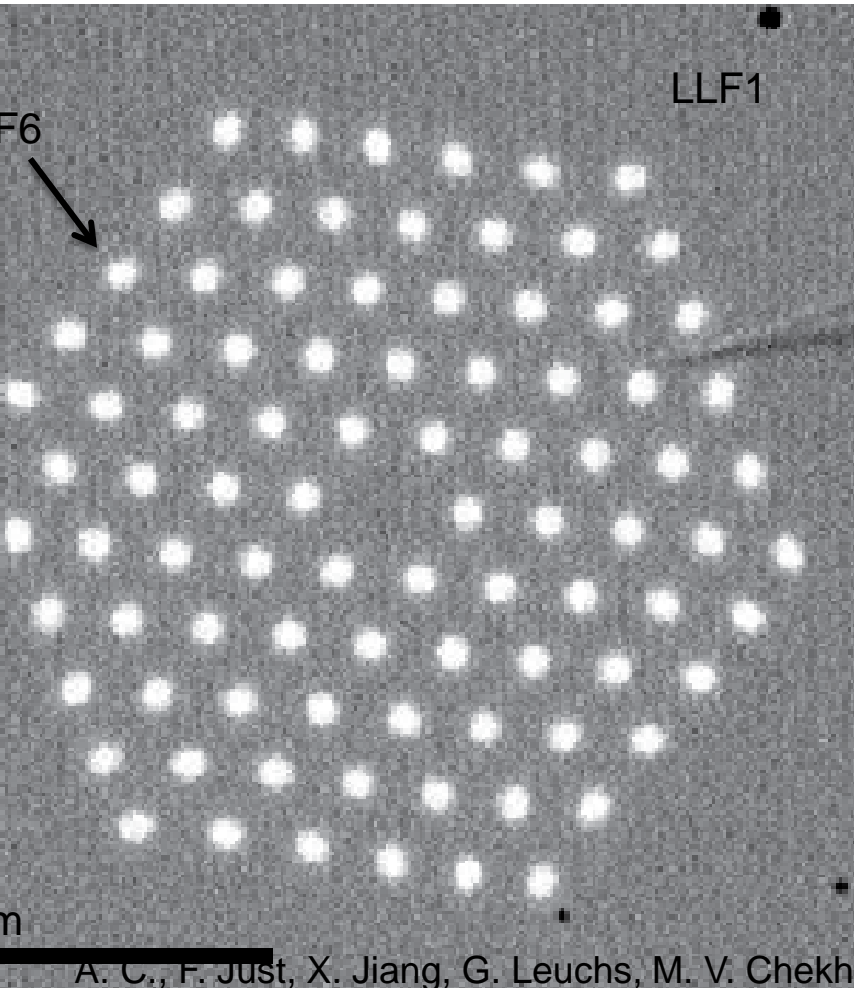
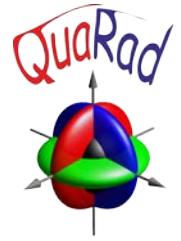


# Luminescence





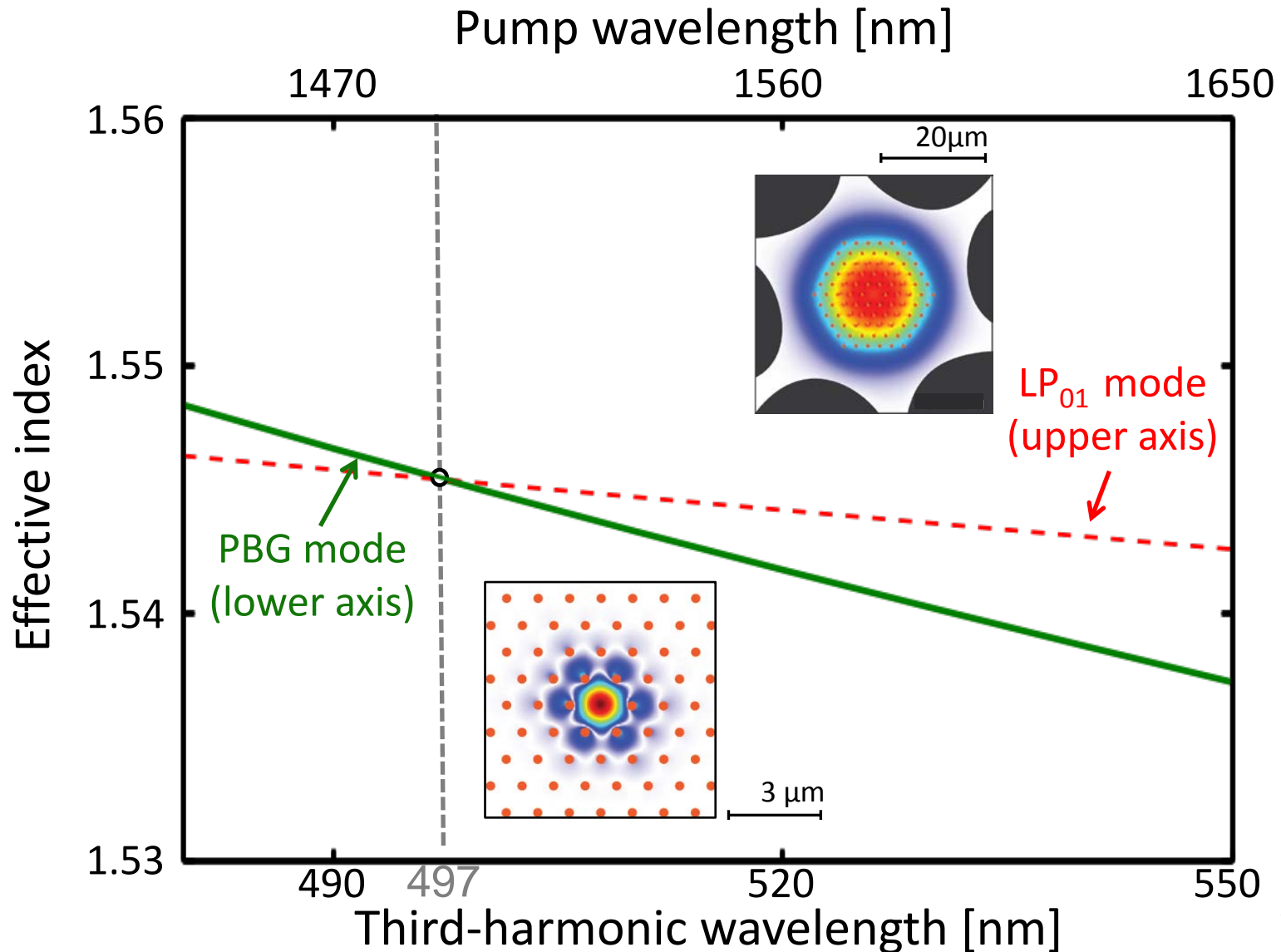
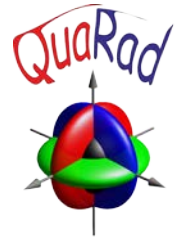
# Hybrid Fibre



A. C., F. Just, X. Jiang, G. Leuchs, M. V. Chekhova, P. St.J. Russell, and N. Y. Joly, *Optica* **3** (9) 952-955 (2016).



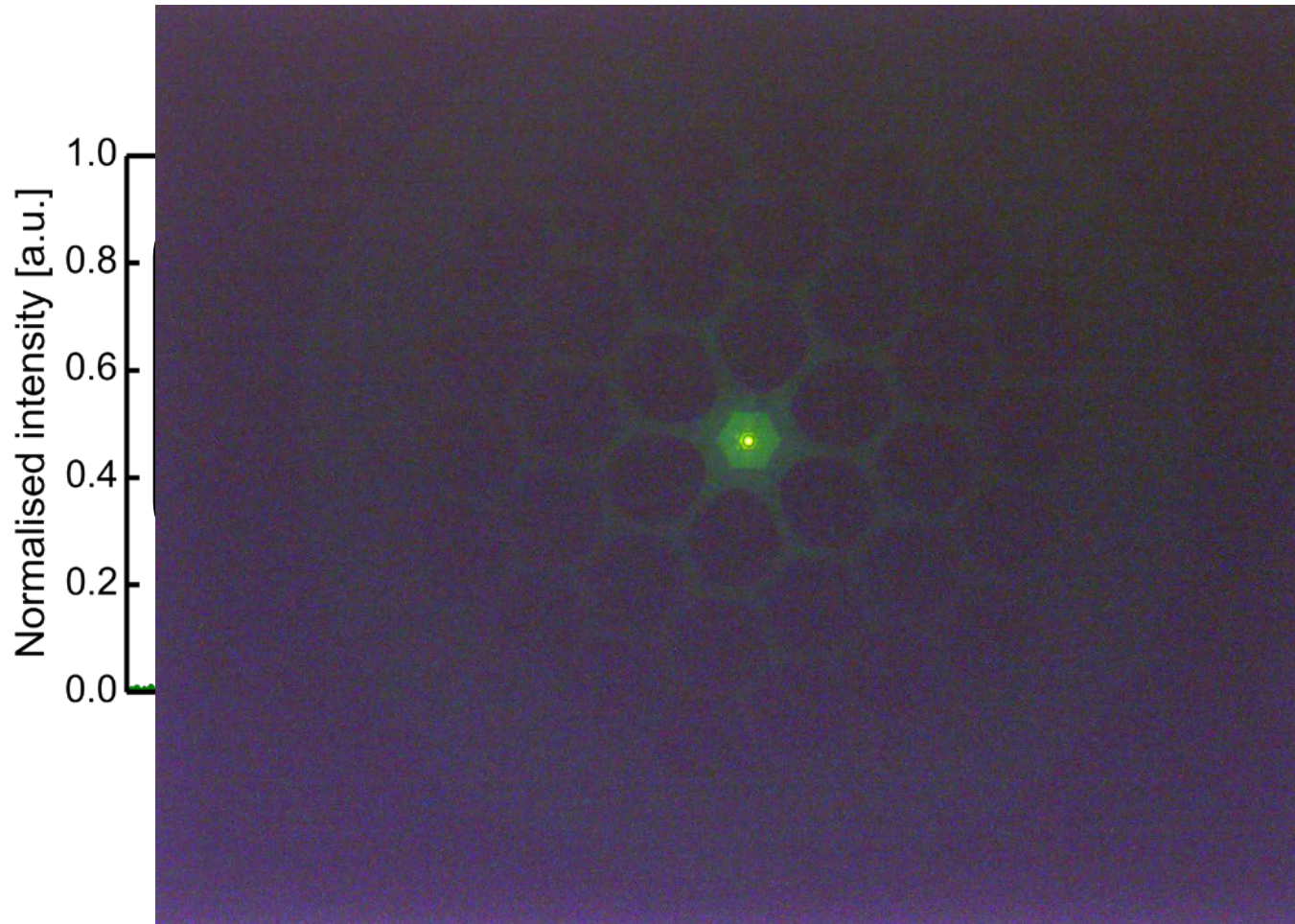
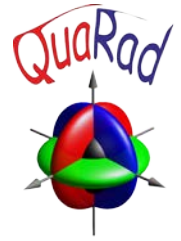
# Third-harmonic generation







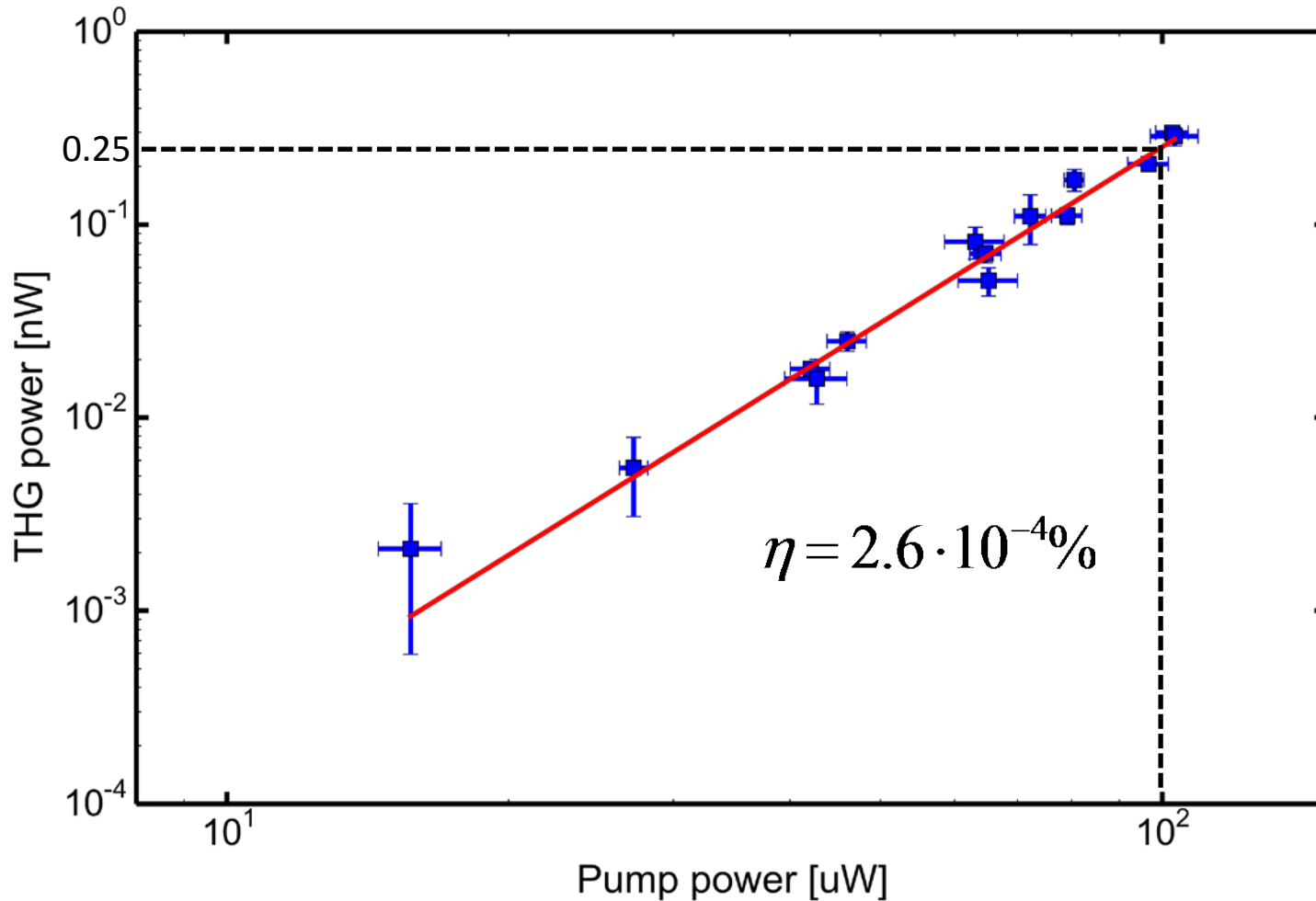
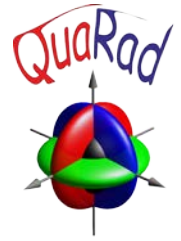
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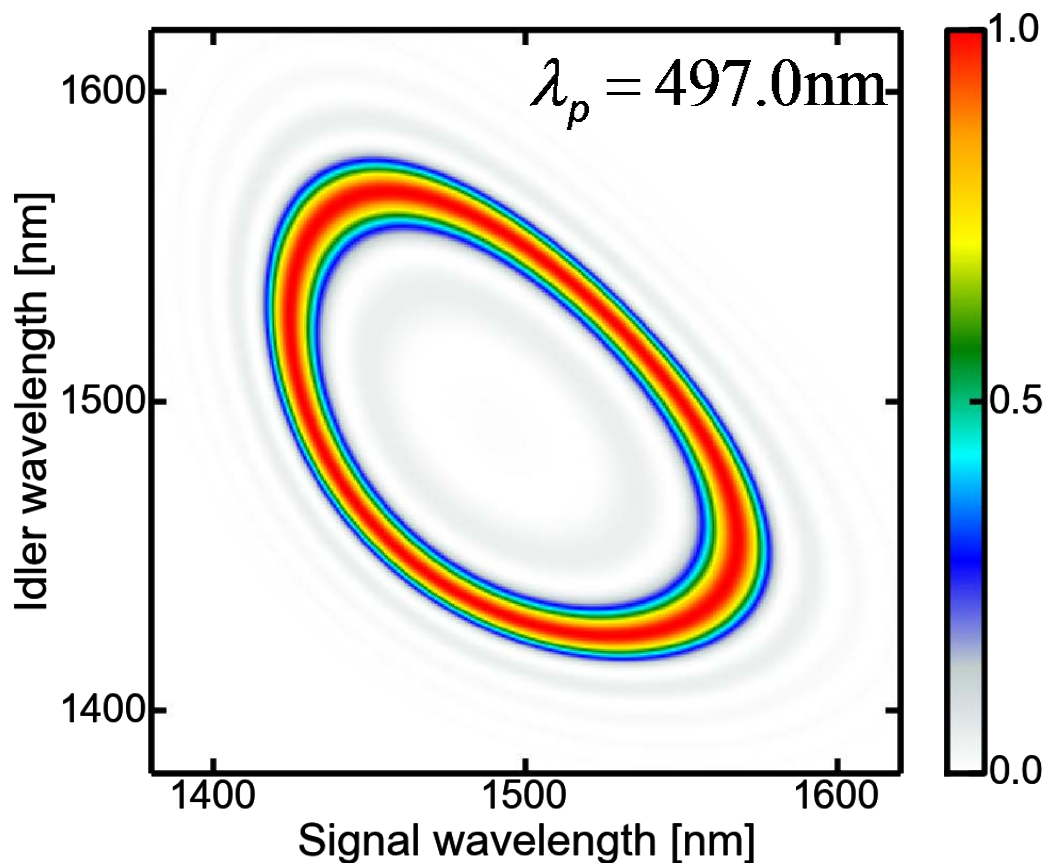


# Third-harmonic generation



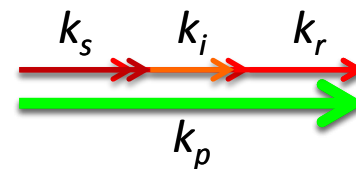


# Photon triplet generation



Phase matching function:

$$\text{sinc}^2(\Delta kL/2)$$



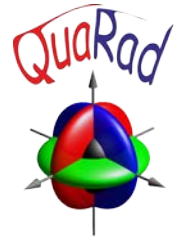
$$L = 10\text{cm}$$

$$P_{3\omega} = 200\text{mW}$$

$$N_{\omega} \approx 50 \text{ triplets/s}$$



# Hollow core fibres

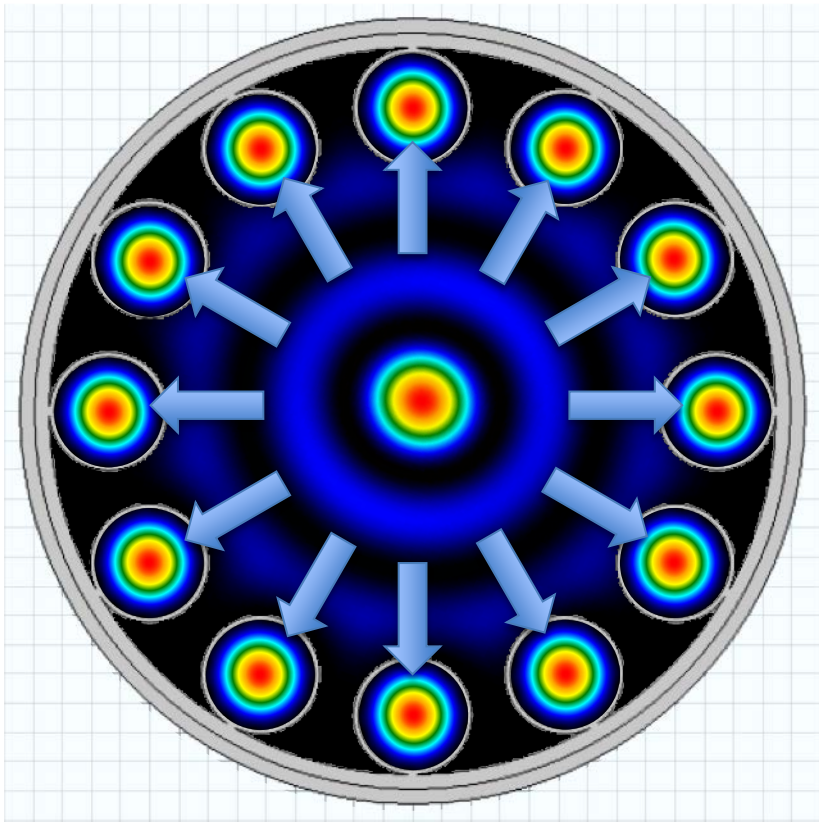
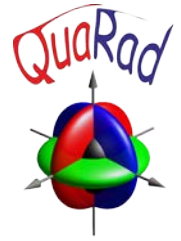


## Features:

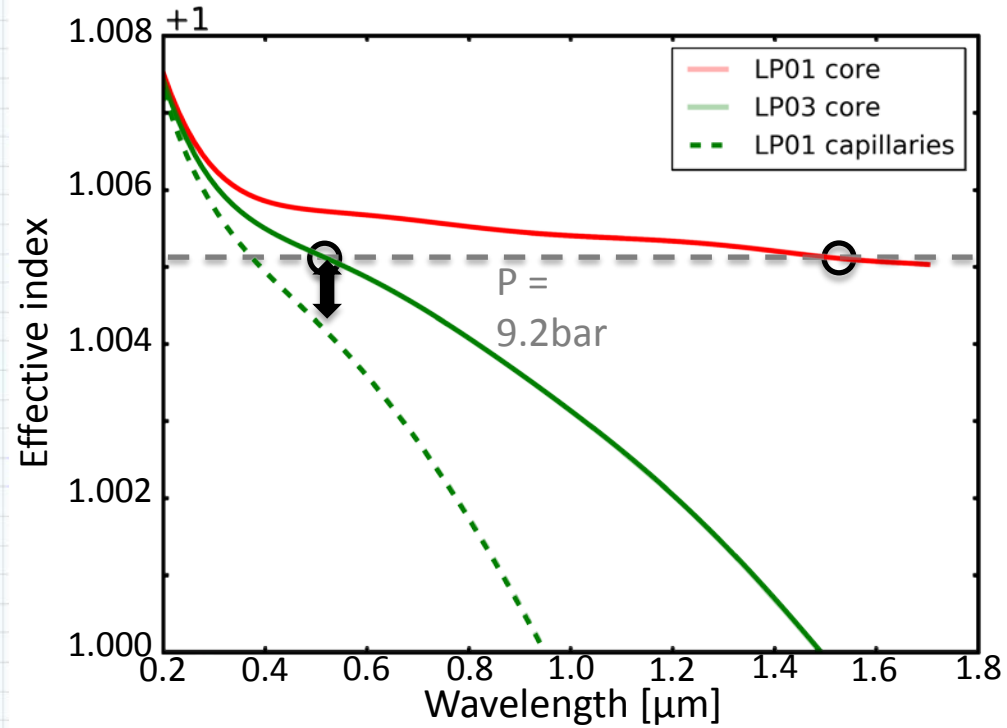
- Pressure controlled phase-matching.
- Filled with noble gas as nonlinear material.
- Very high damage threshold.
- Almost no luminescence



# Hollow core fibre

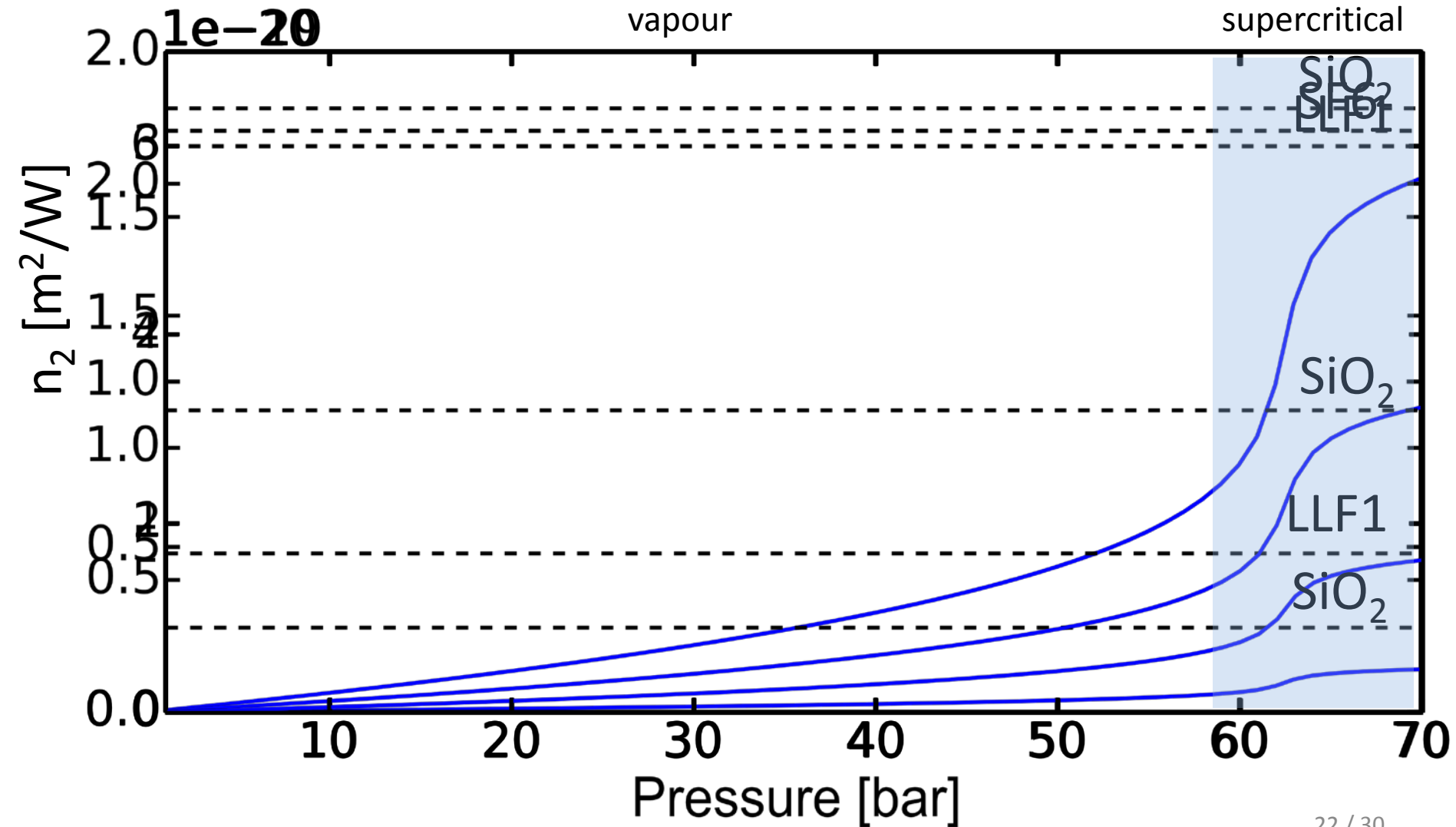
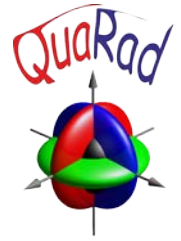


Xenon filled fibre





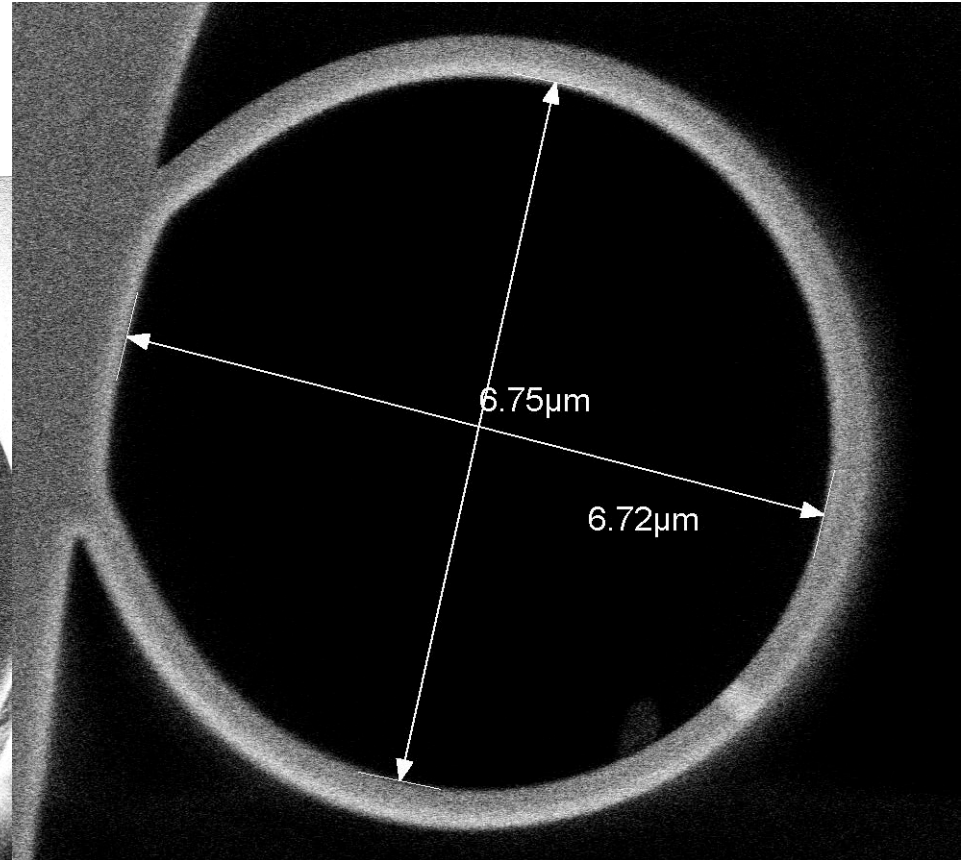
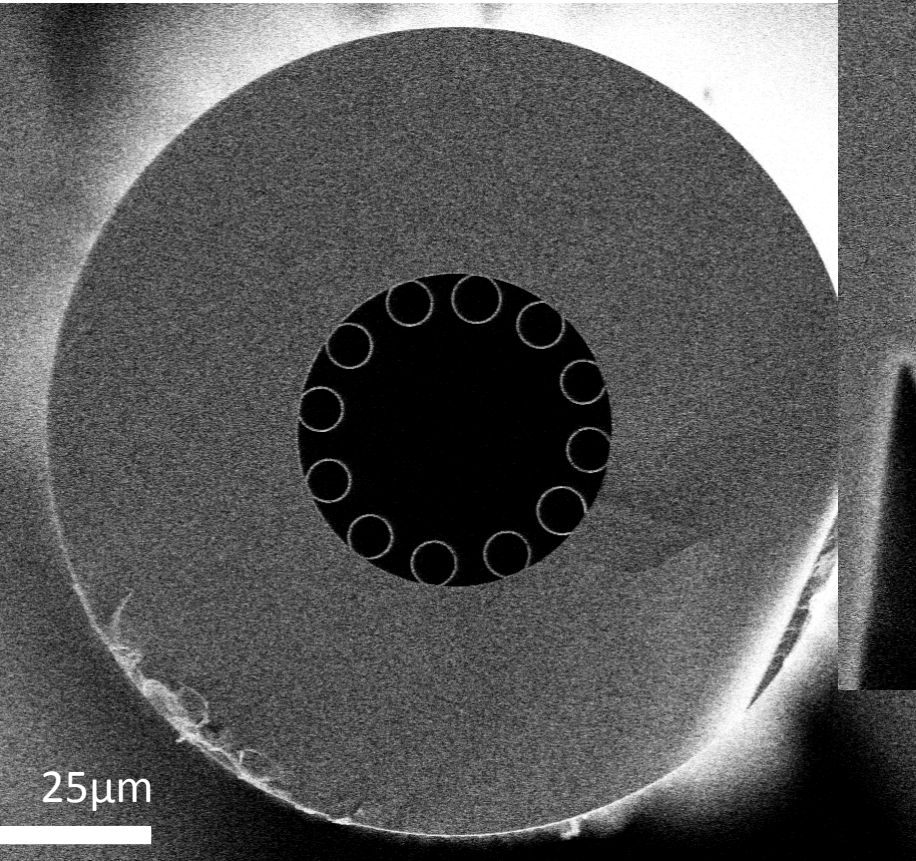
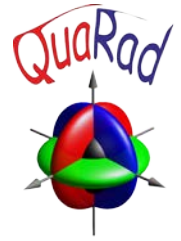
# Xenon nonlinearity





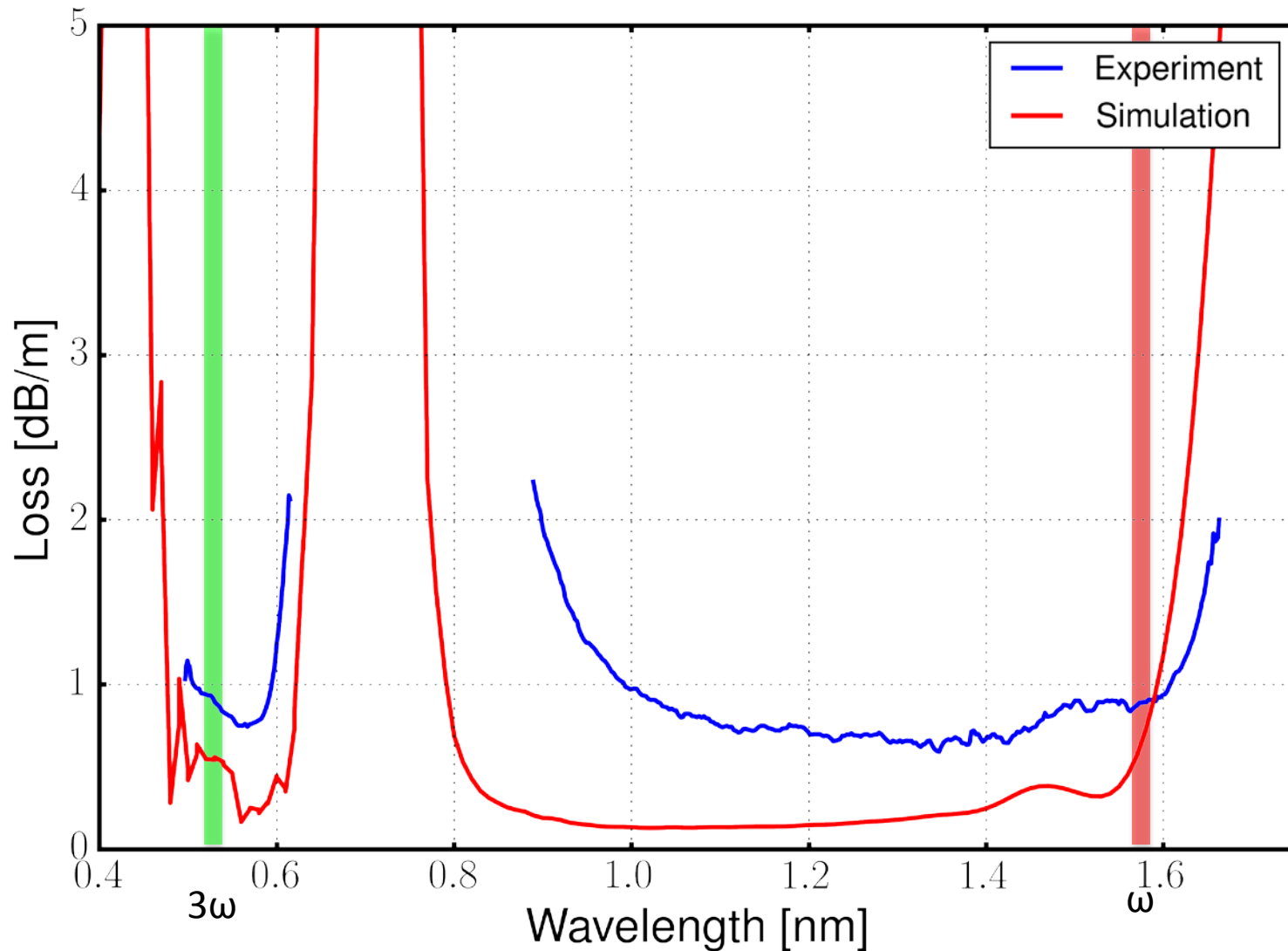
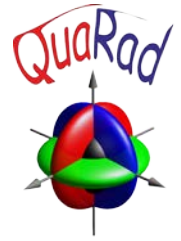


# Single-ring fibre





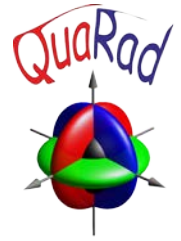
# Measurement losses



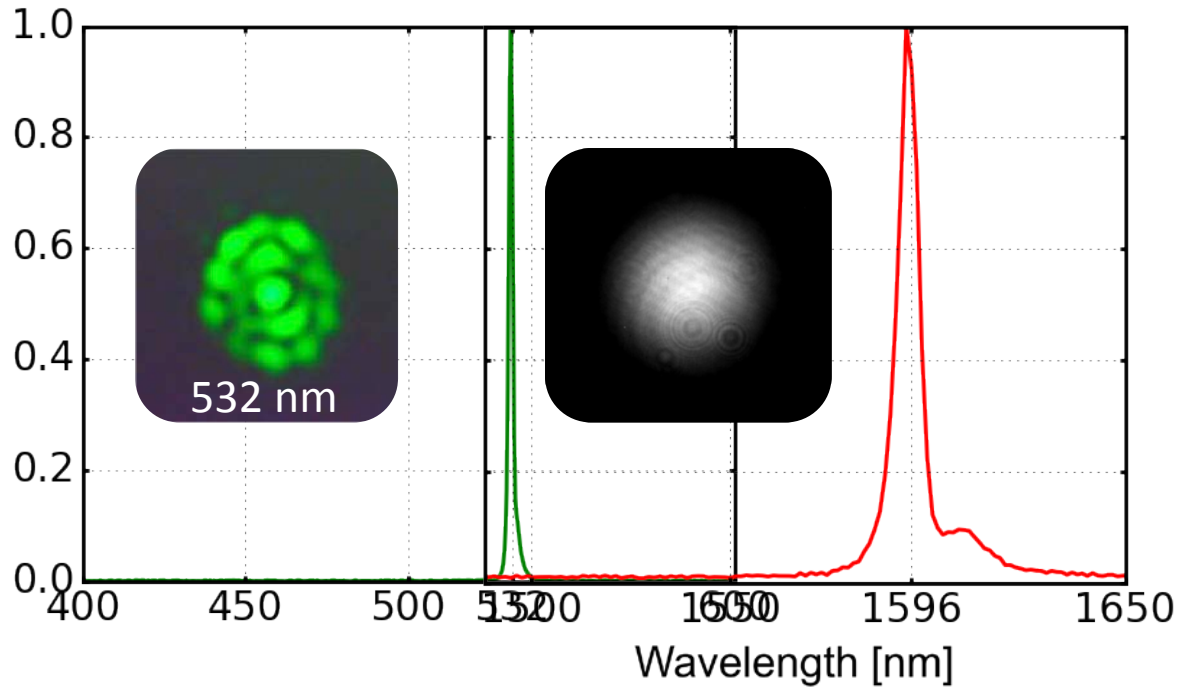




# Third-harmonic generation

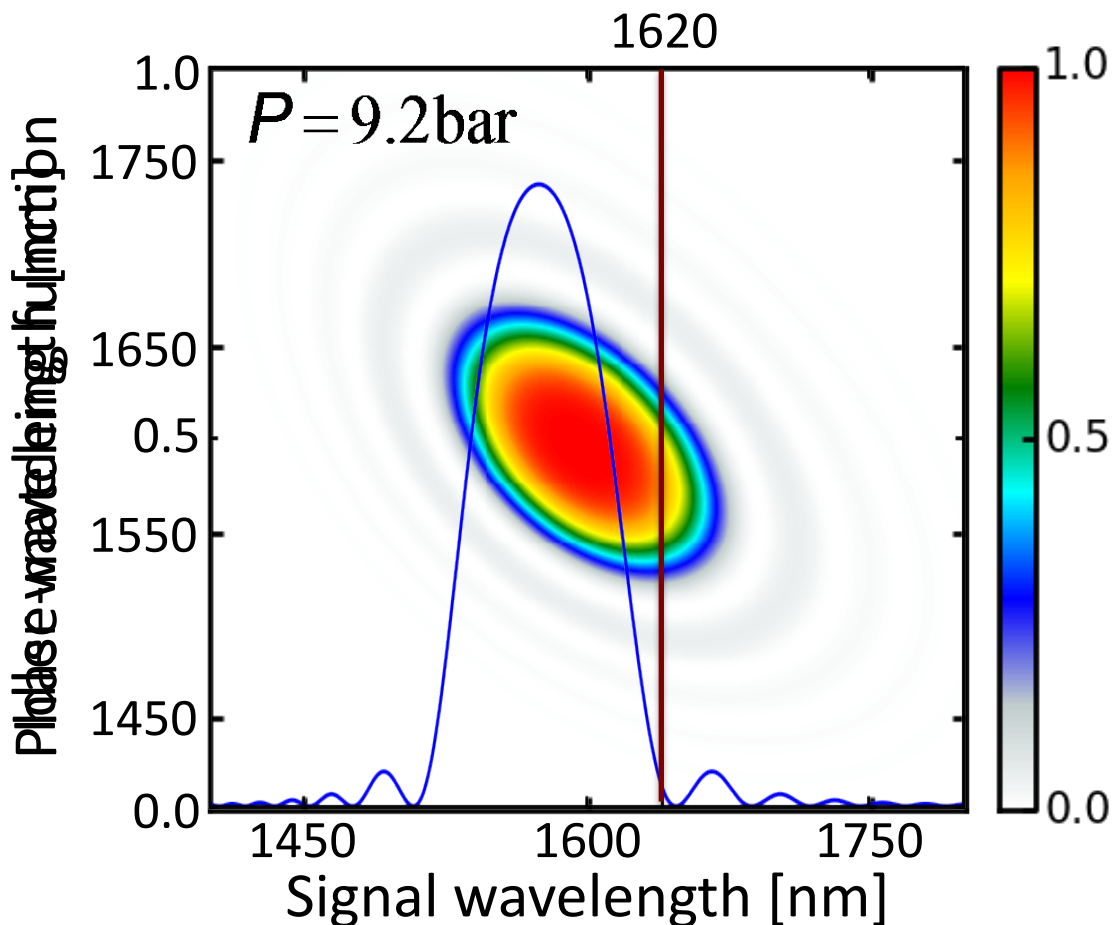


P = 9.2bar



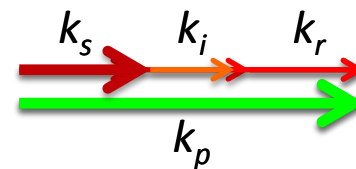


# Photon triplet generation



Phase matching function:

$$\text{sinc}^2(\Delta kL / 2)$$



$$L = 1 \text{ m}$$

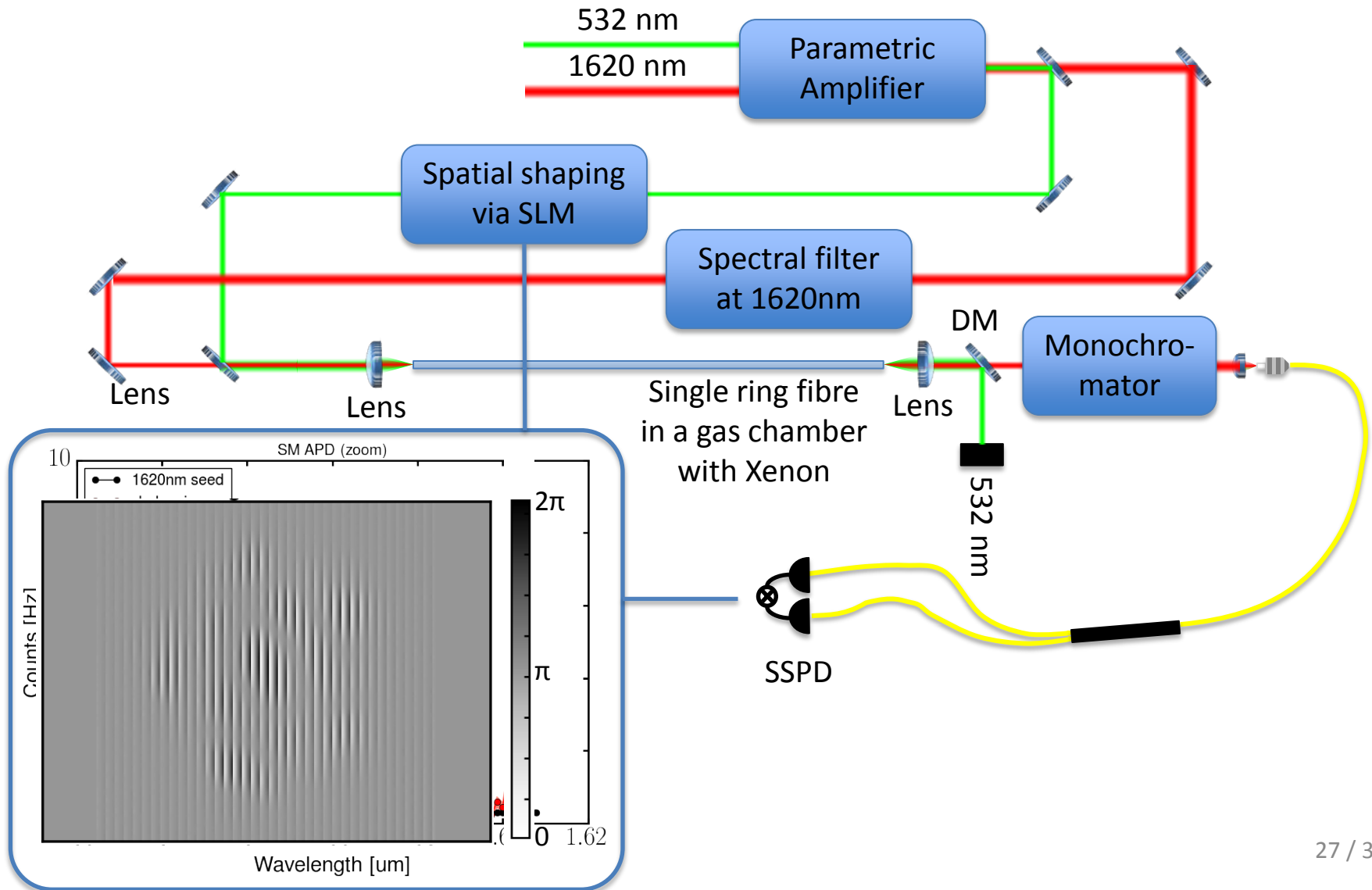
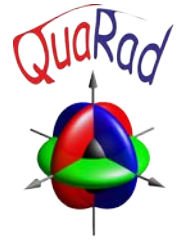
$$P_{3\omega} = 0.5 \text{ W, } 1 \text{ kHz, } 20 \text{ ps}$$

$$P_{\text{seed}} = 10 \text{ mW}$$

$$N_{\omega} \approx 100 \text{ triplets/s/h}$$

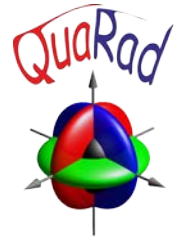


# Set-up





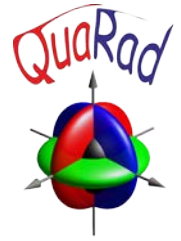
# Future prospects



- Higher confinement
- Alkali vapour + Xe
- Smaller core
- Higher overlap
- Higher pressure ( $\chi^{(3)}$ )
- Higher  $\chi^{(3)}$
- Phase-matching between fundamental modes



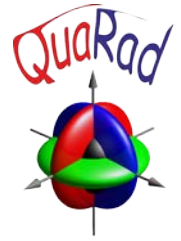
# Summary



|                    | Hybrid fibre                            | Single-ring fibre                       |
|--------------------|---|---|
| Overlap integral   | $0.003 \mu\text{m}^{-2}$                | $8.4 \cdot 10^{-6} \mu\text{m}^{-2}$    |
| Nonlinearity       | $6 \cdot 10^{-20} \text{ m}^2/\text{W}$ | $4 \cdot 10^{-22} \text{ m}^2/\text{W}$ |
| Phase matching     | fixed                                   | tuneable                                |
| Damage threshold   | low                                     | high                                    |
| Length             | limited by construction                 | limited by gas cell                     |
| Confinement losses | high for visible                        | high                                    |
| Absorption losses  | high above 1.6nm                        | very low                                |



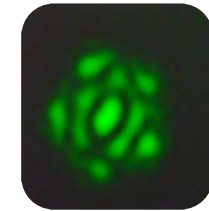
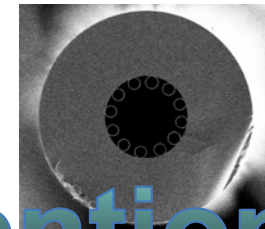
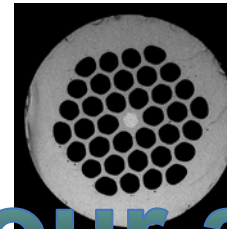
# Conclusions



- Fibre designs:

Hybrid

Single-ring



- Third-harmonic generation:

- Photon triplet generation:



Thank you for your attention!