



Quantum  
Radiation  
group

Max-Planck Institute  
for the Science  
of Light



# TRANSVERSE ENTANGLEMENT OF BIPHOTONS

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european  
social fund in the  
czech republic



EUROPEAN UNION



MINISTRY OF EDUCATION,  
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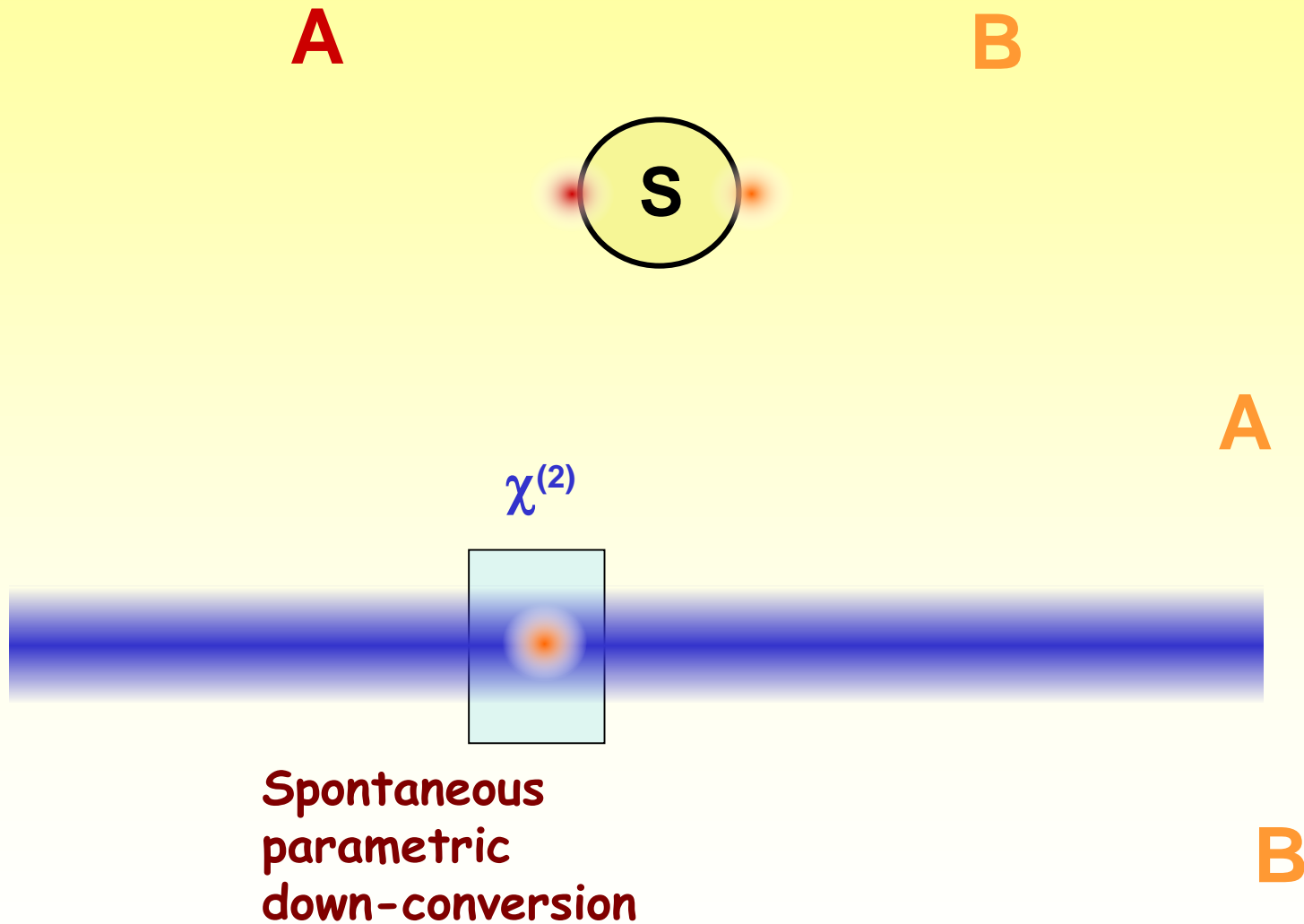


OP Education  
for Competitiveness

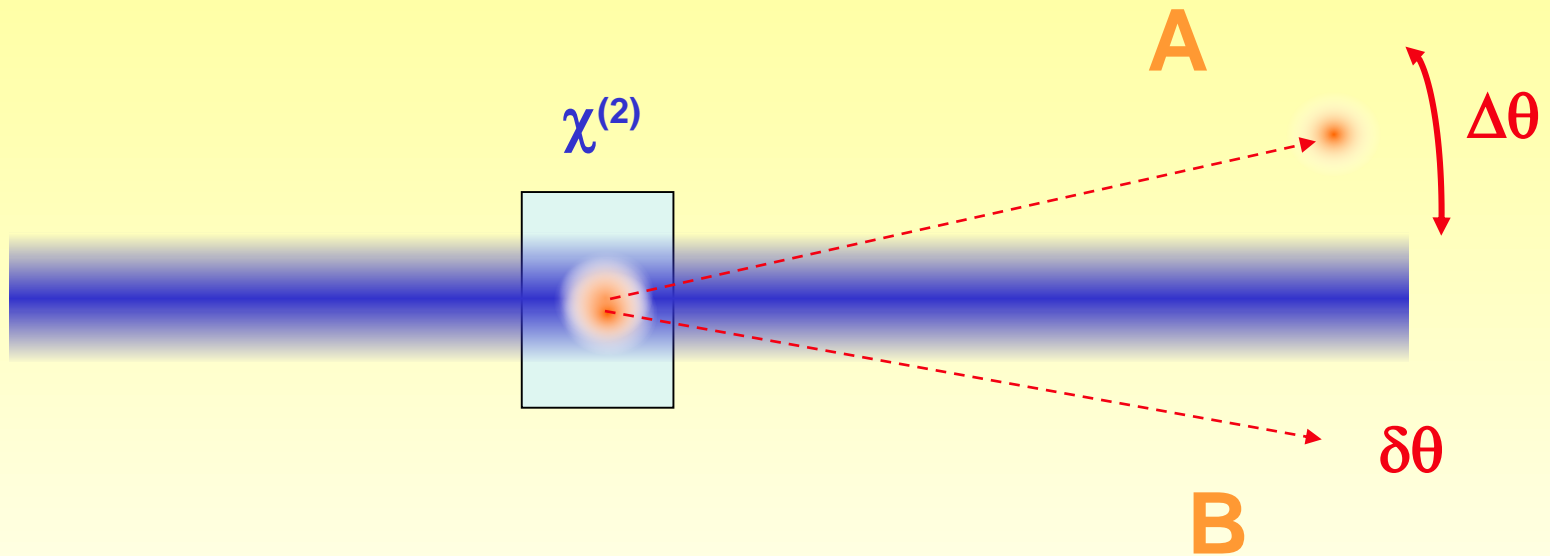
INVESTMENTS IN EDUCATION DEVELOPMENT



# BIPHOTONS



# TRANSVERSE ENTANGLEMENT

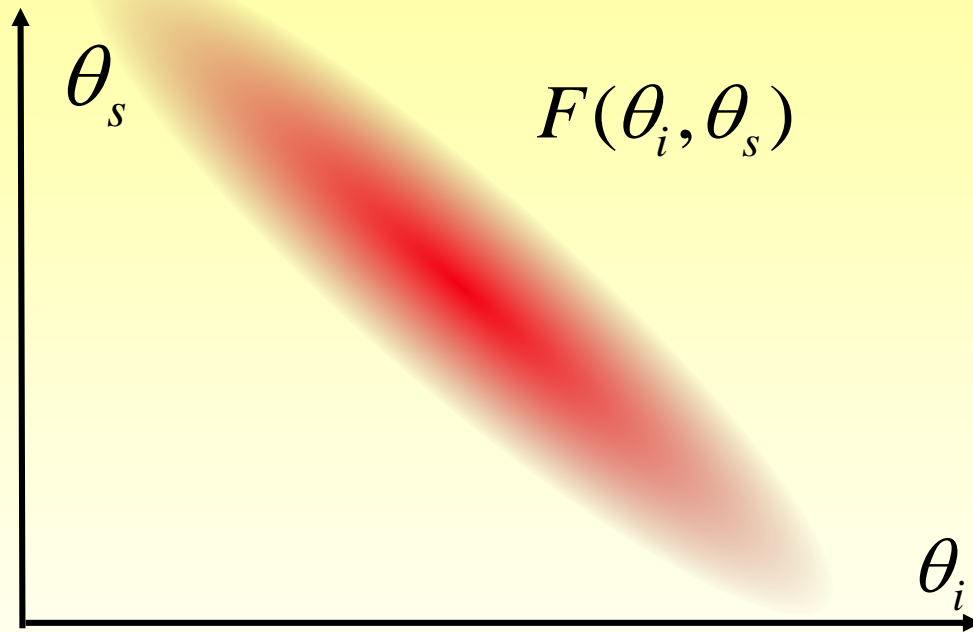


Entanglement:  $\Delta\theta \gg \delta\theta$

Uncertainty for one subsystem plus correlations between the two subsystems

# TWO-PHOTON AMPLITUDE

$$|\Psi\rangle = \iint d\theta_i d\theta_s F(\theta_i, \theta_s) a^\dagger(\theta_i) a^\dagger(\theta_s) |\text{vac}\rangle$$

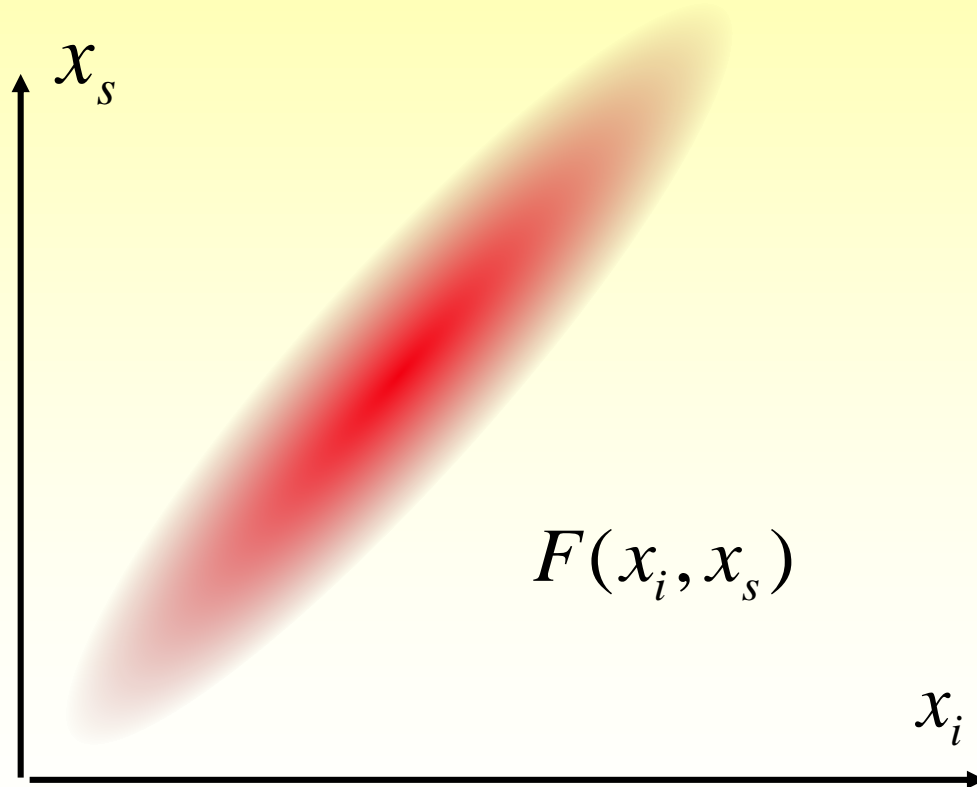


$$F(\theta_i, \theta_s) = \sum_n \sqrt{\lambda_n} \varphi_n(\theta_i) \chi_n(\theta_s), \quad \sum_n \lambda_n = 1, \quad K = \left[ \sum_n \lambda_n^2 \right]^{-1}$$

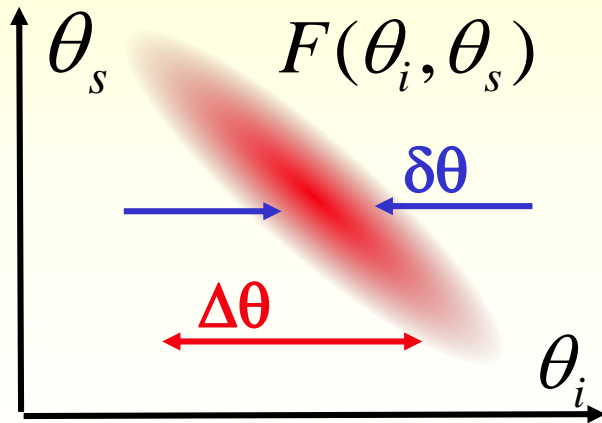
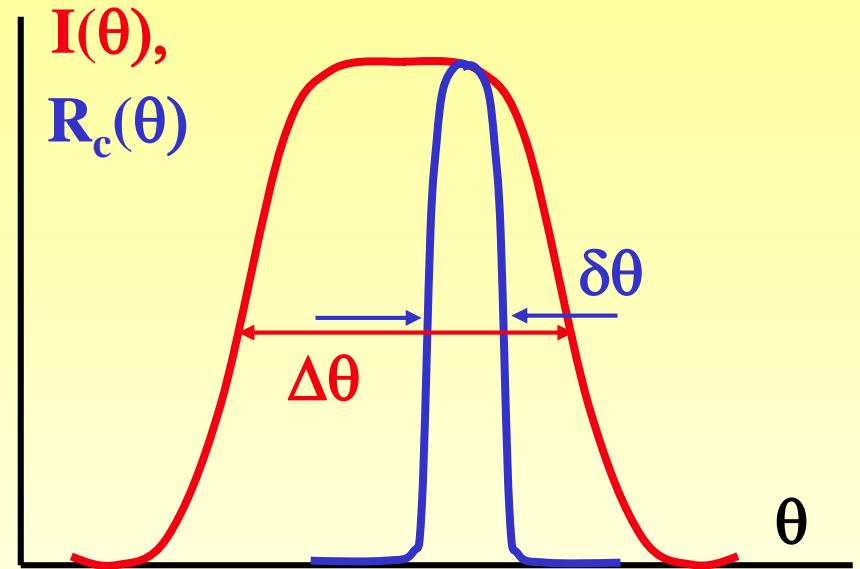
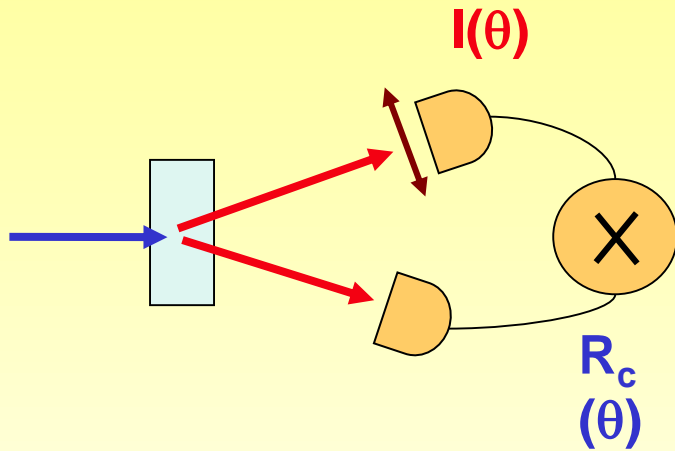
**The Schmidt number**

# TWO-PHOTON AMPLITUDE: NEAR FIELD

$$|\Psi\rangle = \iint dx_i dx_s F(x_i, x_s) a^+(x_i) a^+(x_s) |\text{vac}\rangle$$



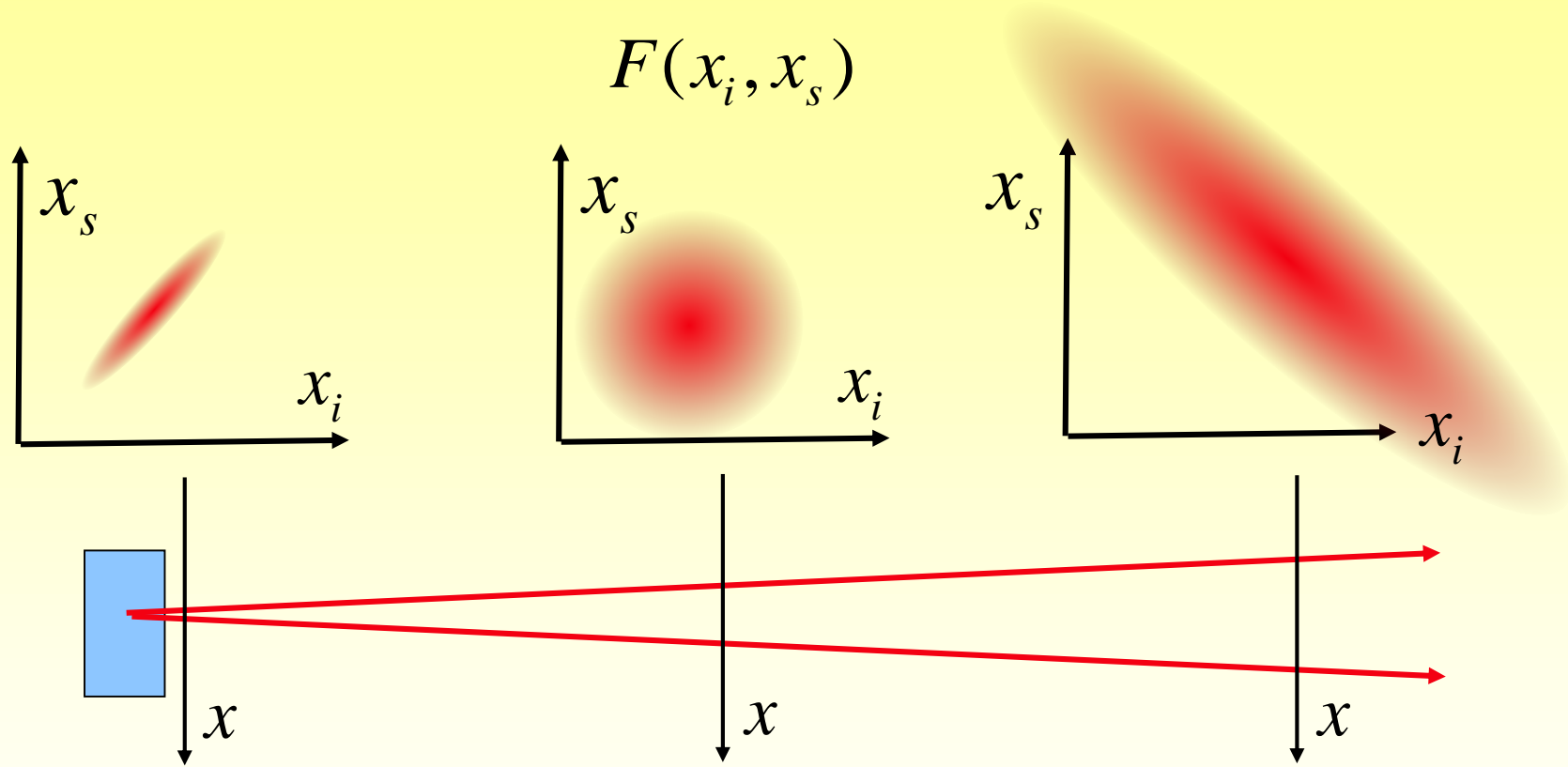
# FEDOROV RATIO



Fedorov ratio:  $R = \Delta\theta / \delta\theta$

Valid only for pure states;  
For Gaussian TPAs  
coincides with the Schmidt  
number

# FROM NEAR TO FAR FIELD

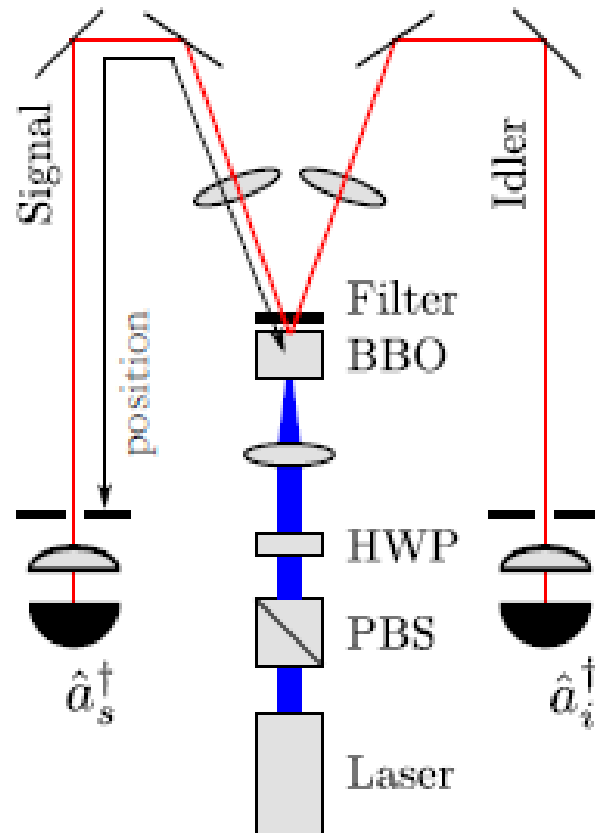
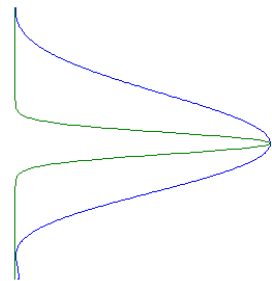
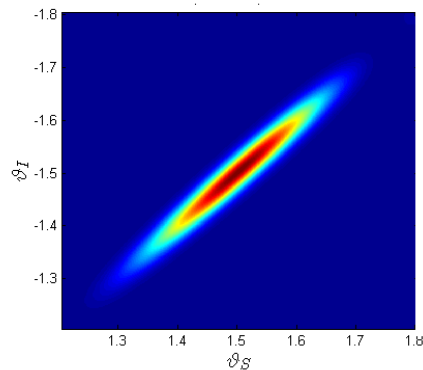


The Fedorov ratio becomes unity between near and far field. But entanglement cannot disappear!

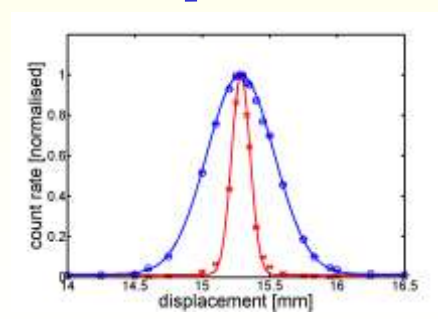
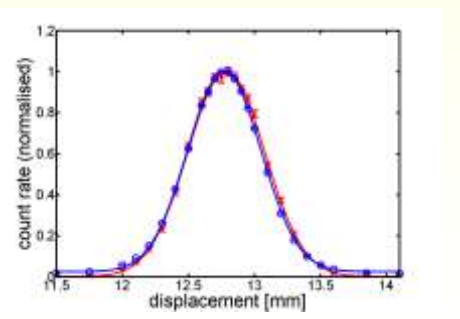
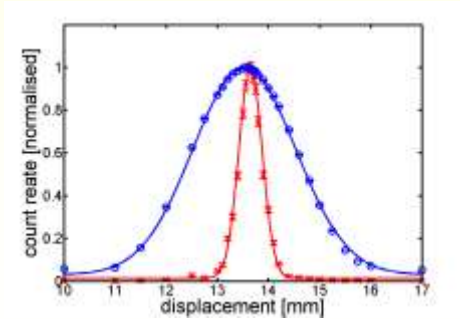
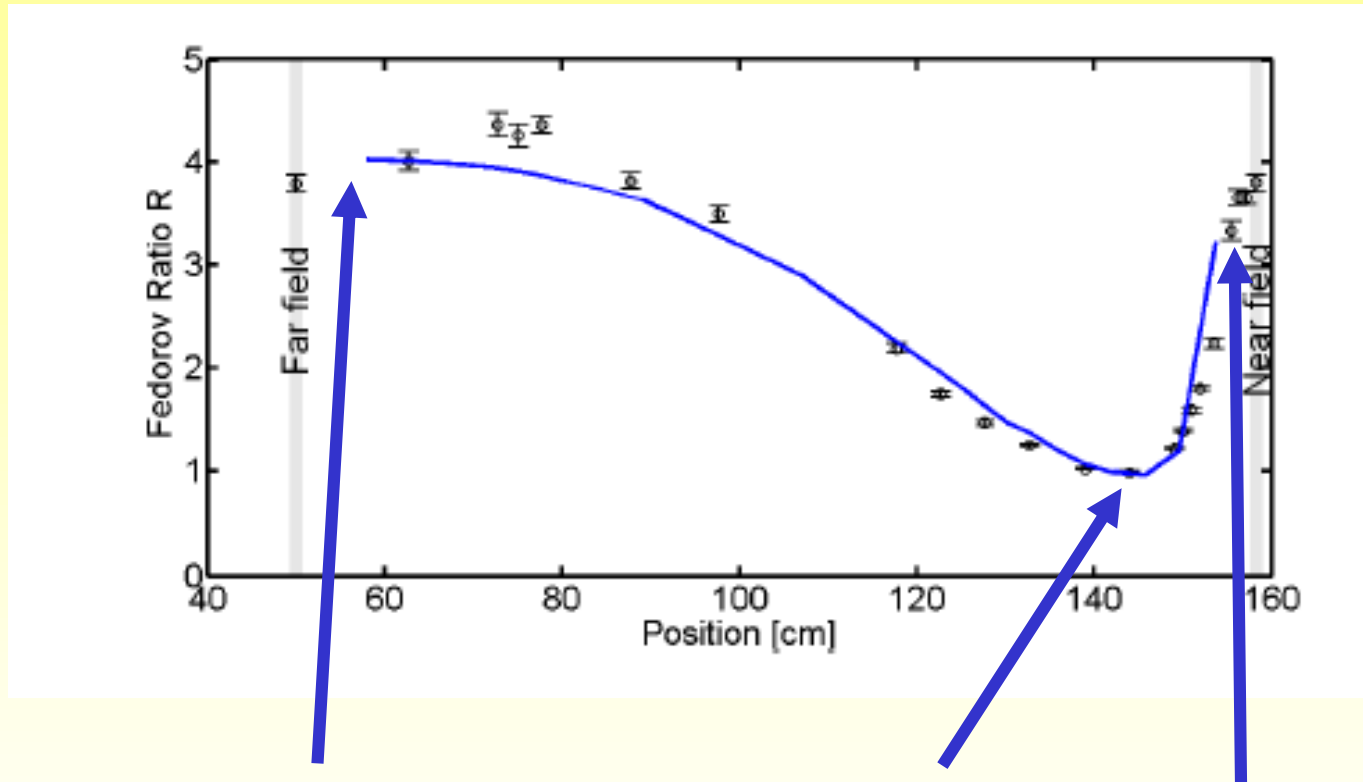


# EXPERIMENT

We measure the Fedorov ratio at different distances from the crystal, passing from the far field to the near field

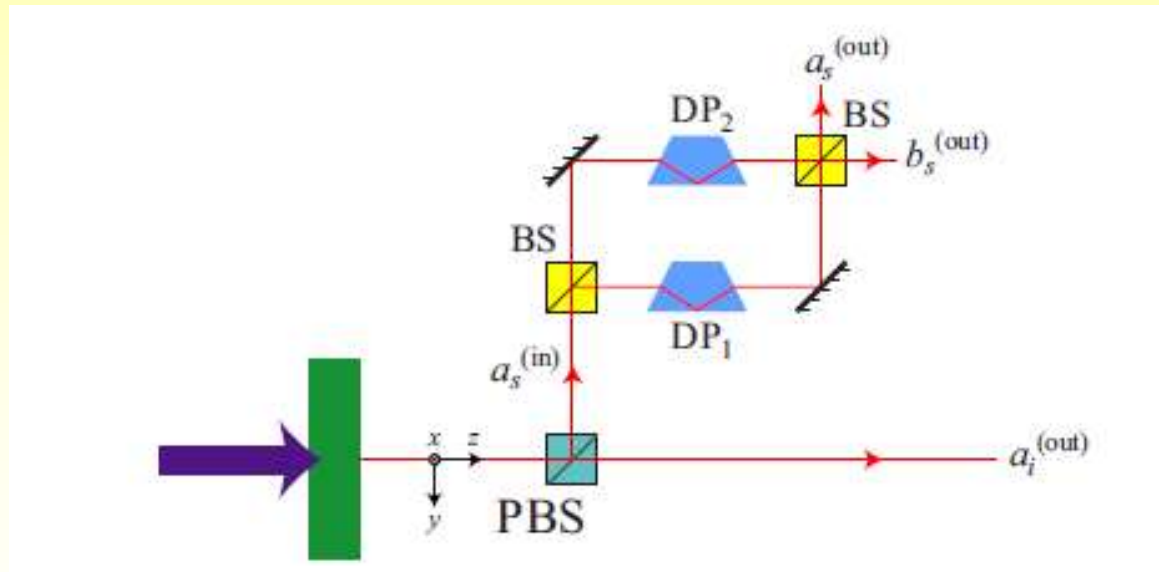


# RESULTS: FEDOROV RATIO

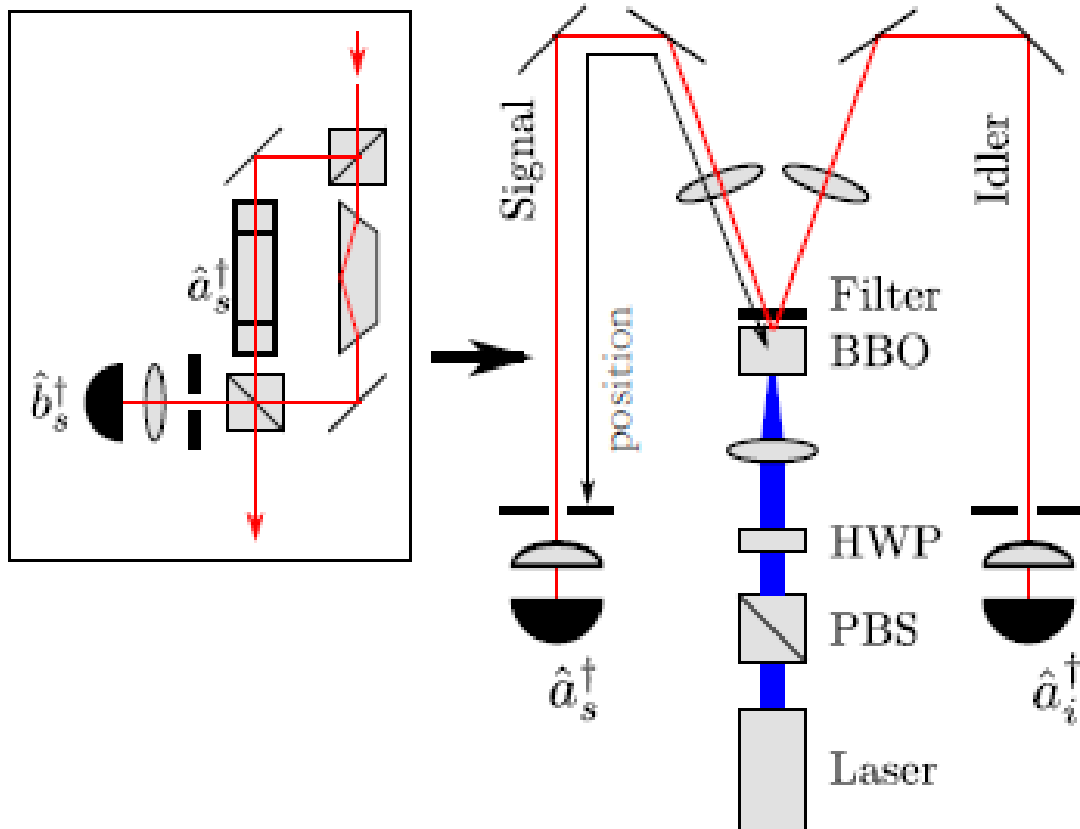


# SCHMIDT NUMBER MEASUREMENT

The Schmidt number gives the number of transverse (spatial) modes. The more modes, the less the spatial coherence. Spatial coherence can be measured through interference.

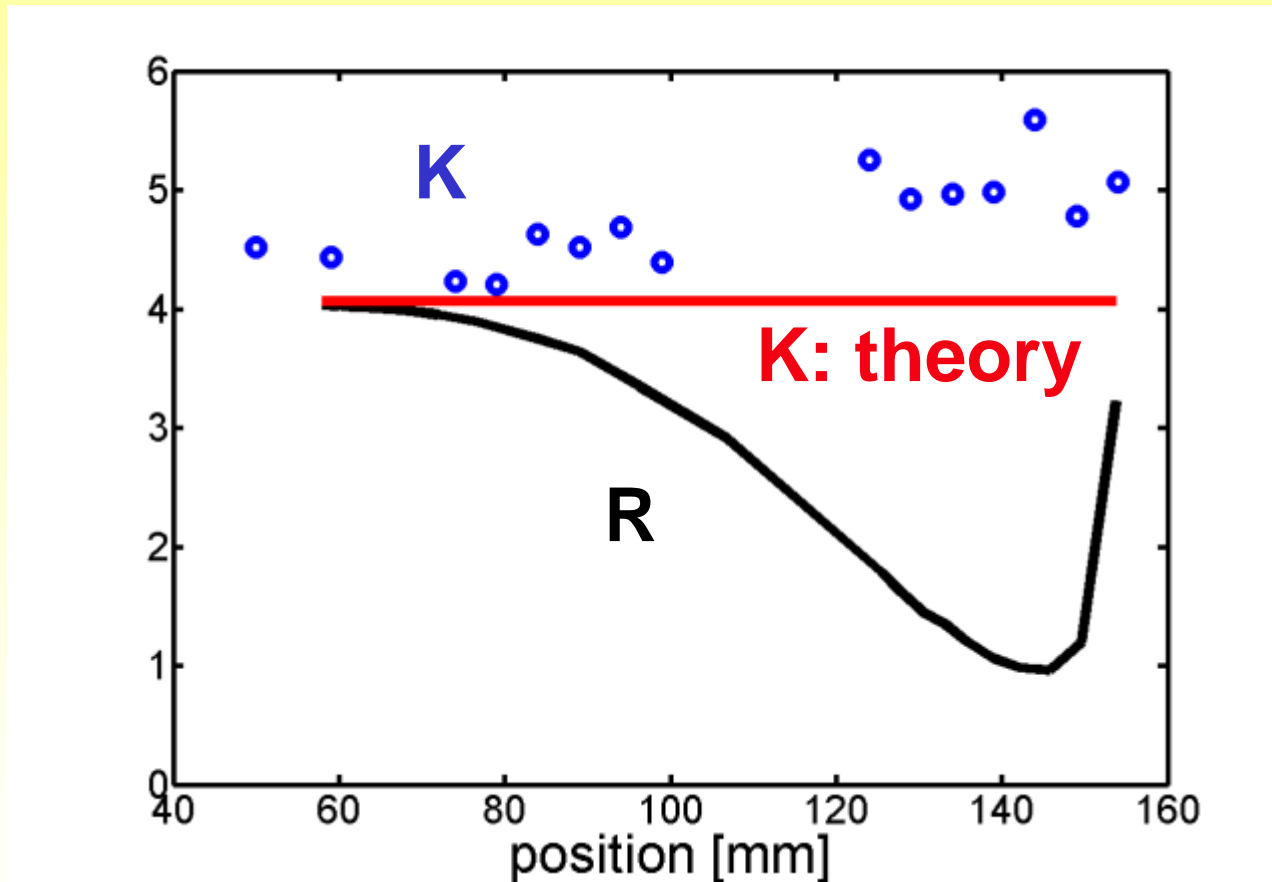


# EXPERIMENT



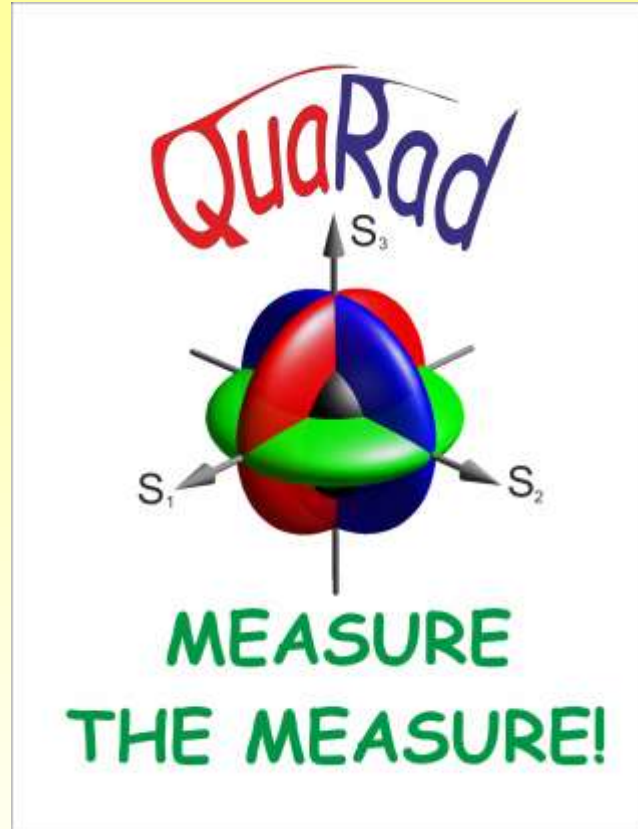
# INTERFEROGRAMS

# RESULTS: THE SCHMIDT NUMBER



# CONCLUSIONS

1. The Fedorov ratio can be used as a measure of entanglement only in the near and far field zones.
2. As a universal measure of entanglement, the Schmidt number can be used. It can be measured as the inverse visibility of interference. And it does not change as the field propagates from near to far zones.



**THANK YOU FOR YOUR ATTENTION!**