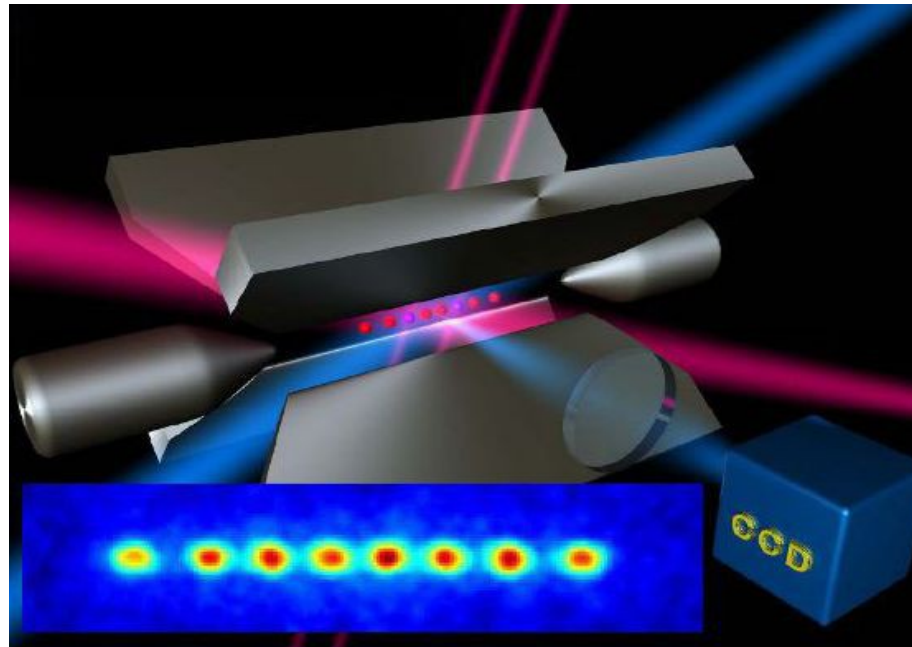


# Single atom – light interactions in free space

*Lukáš Slodička*

Department of Optics, Faculty of Science, Palacký University,  
Olomouc, Czech Republic

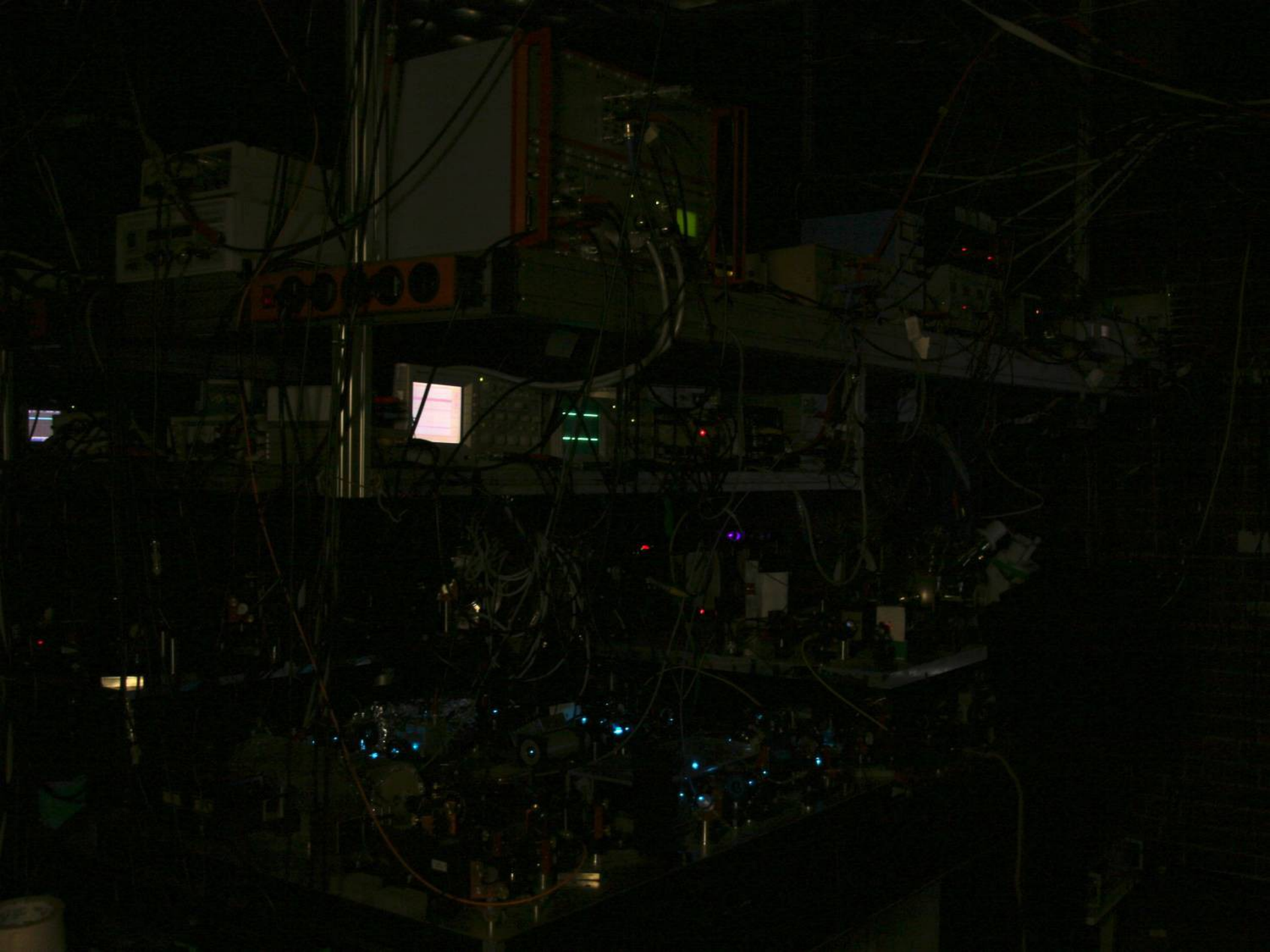


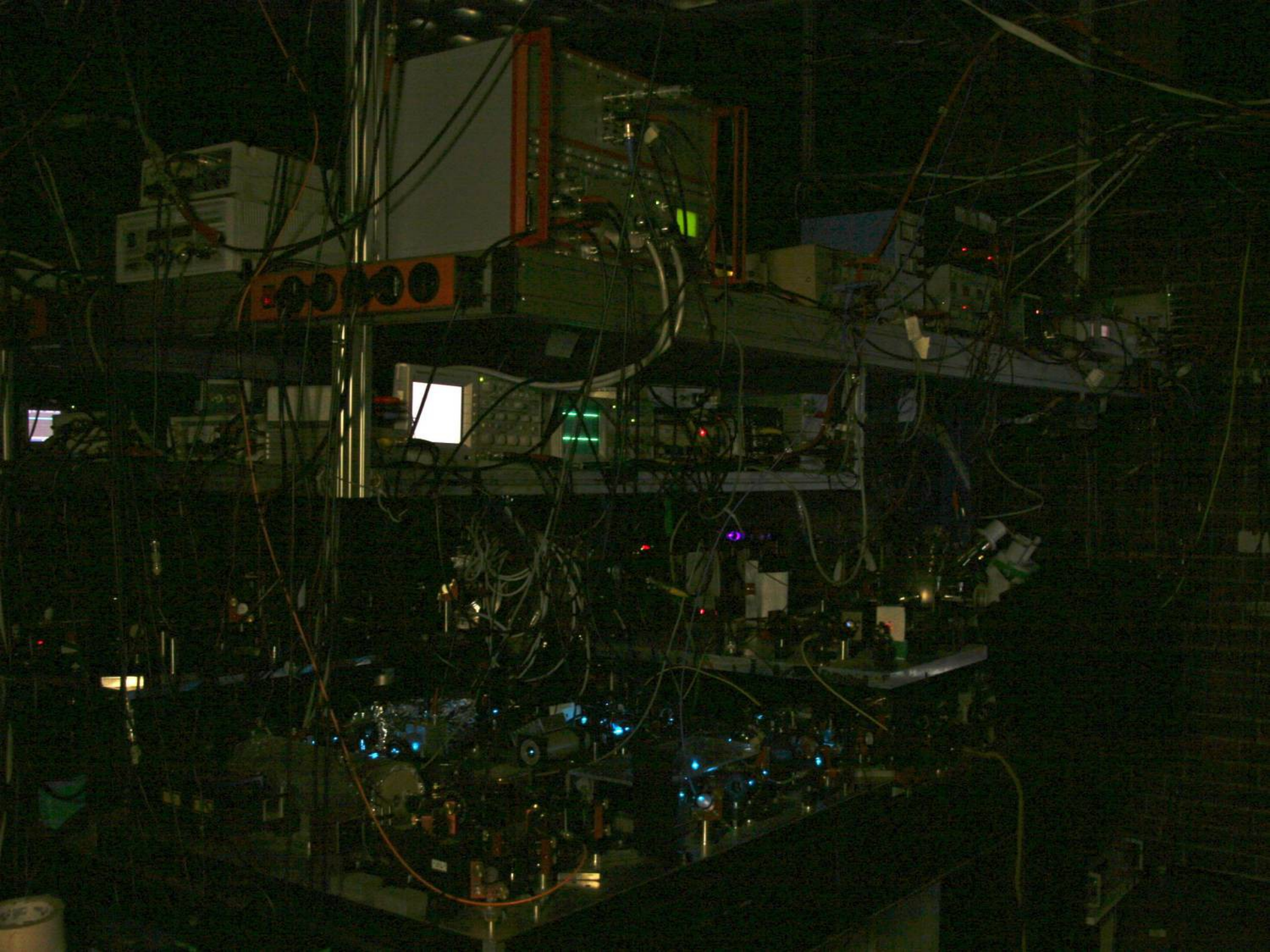
MU, Brno, 20. 5. 2014

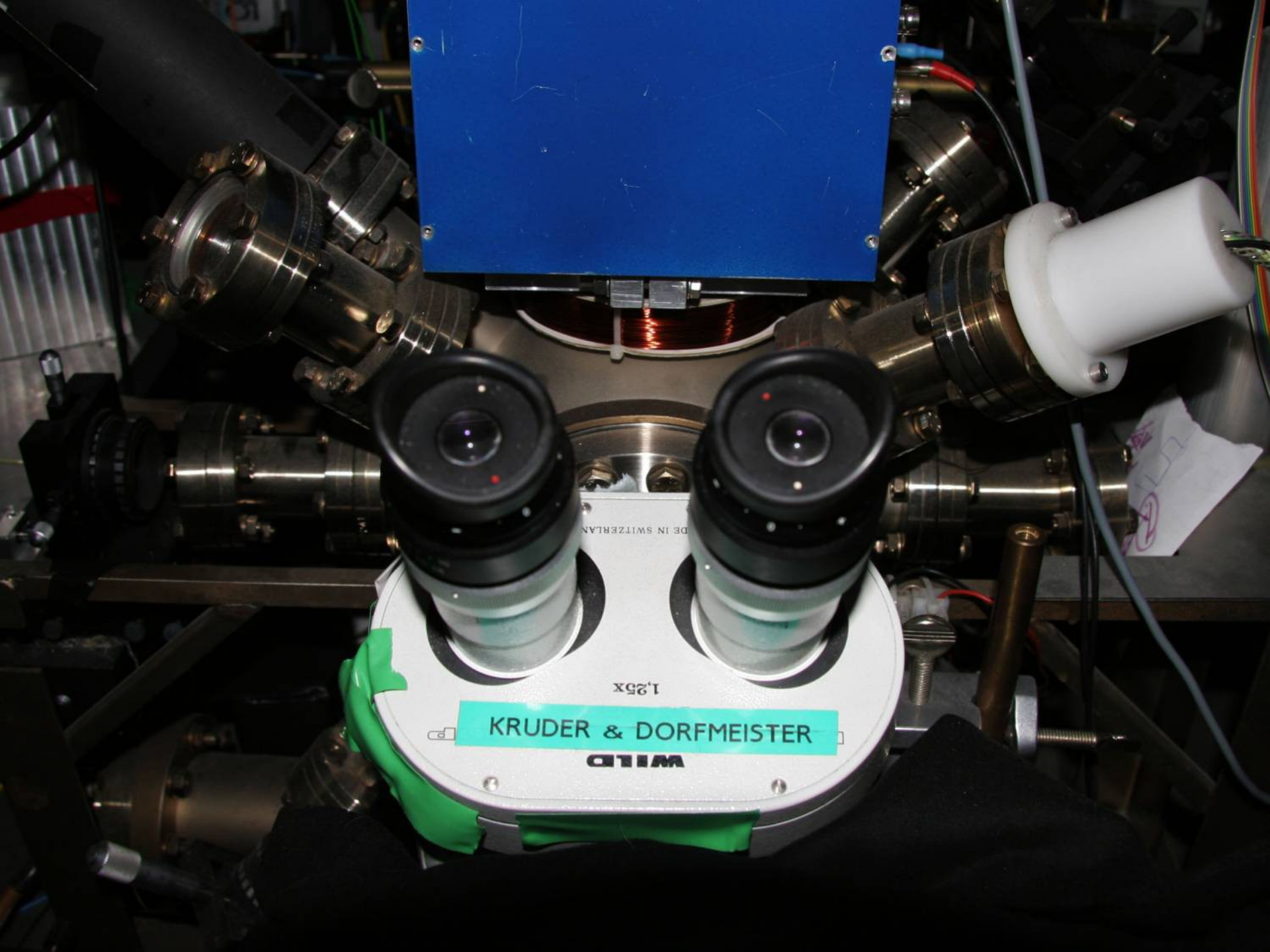


INVESTICE DO ROZVOJE VZDĚLÁVÁNÍ









1,25x  
KRUDER & DORFMEISTER  
WILD

DE IN SWITZERLAN

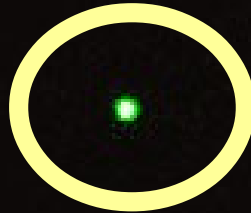


# Observation of a single isolated atom!

*We never experiment with just one electron or atom or (small) molecule. In thought-experiments we sometimes assume that we do; this invariably entails ridiculous consequences.*

**E. Schrödinger**

British Journal of the Philosophy  
of Science III (10), (1952)



What do we actually see?

# Observation of a single atom in free space

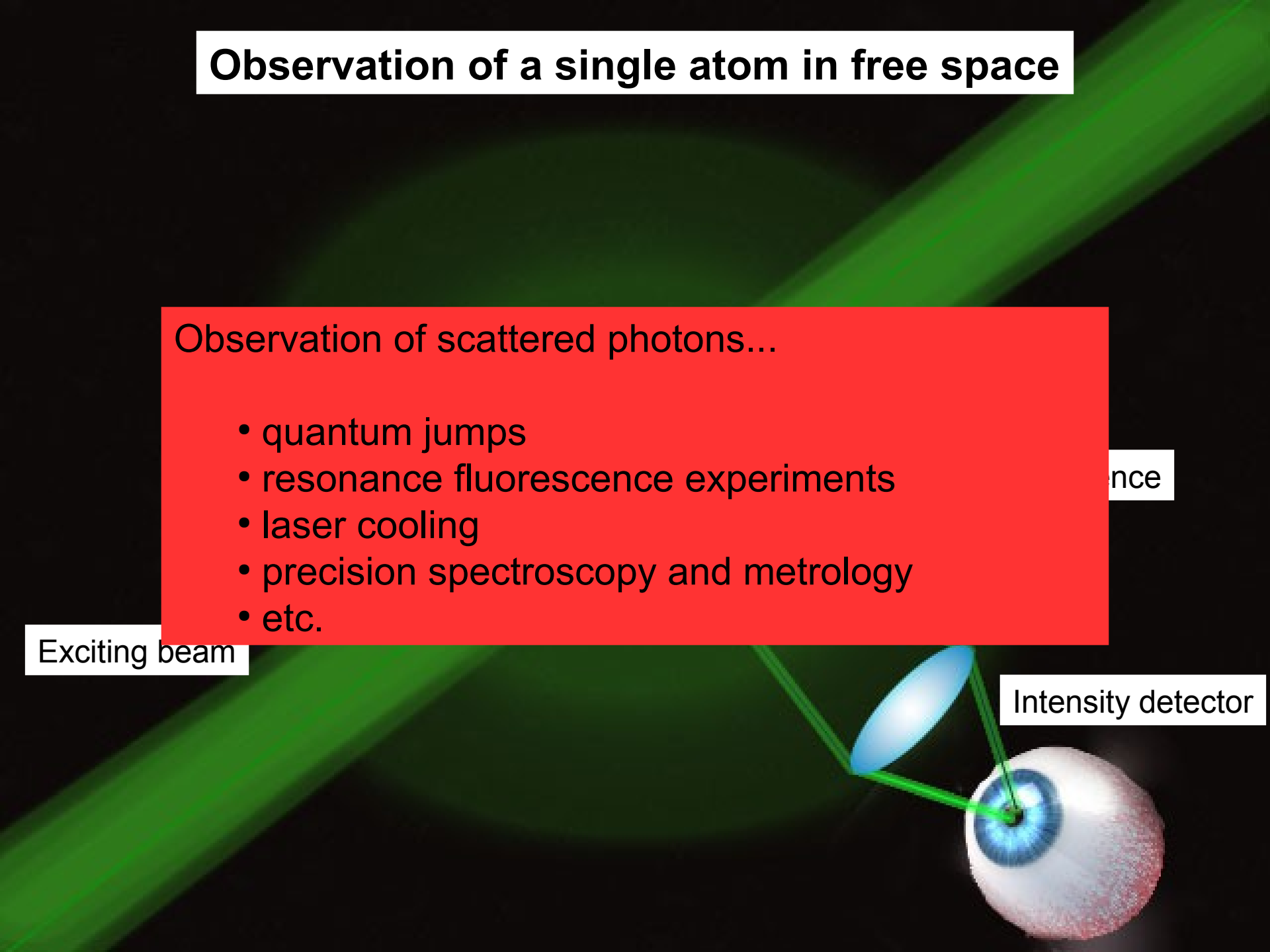
Observation of scattered photons...

- quantum jumps
- resonance fluorescence experiments
- laser cooling
- precision spectroscopy and metrology
- etc.

Exciting beam

Intensity detector

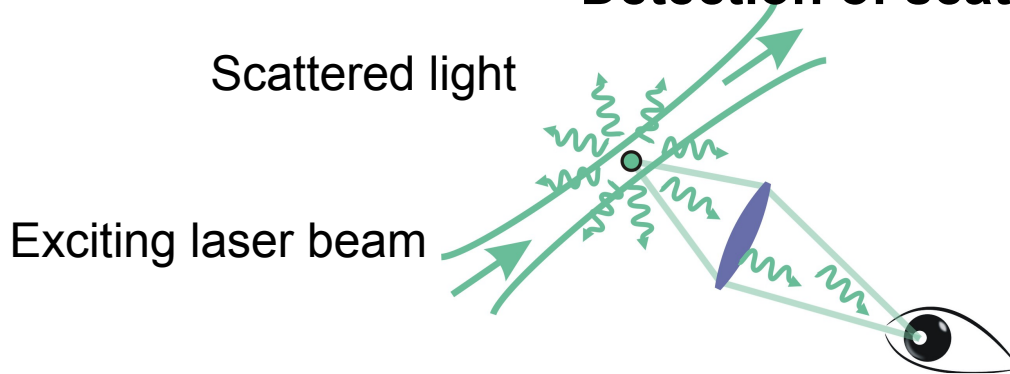
ence





# Observation of single atom in free space

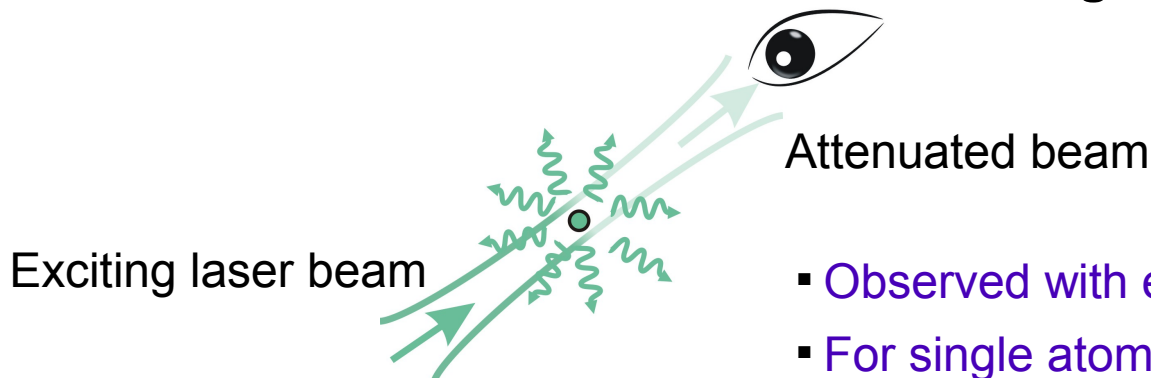
## Detection of scattered light



- Resonance fluorescence experiments
- Quantum jumps spectroscopy

## Distribution of entanglement by mere observation of scattered photon?

## Detection of exciting beam

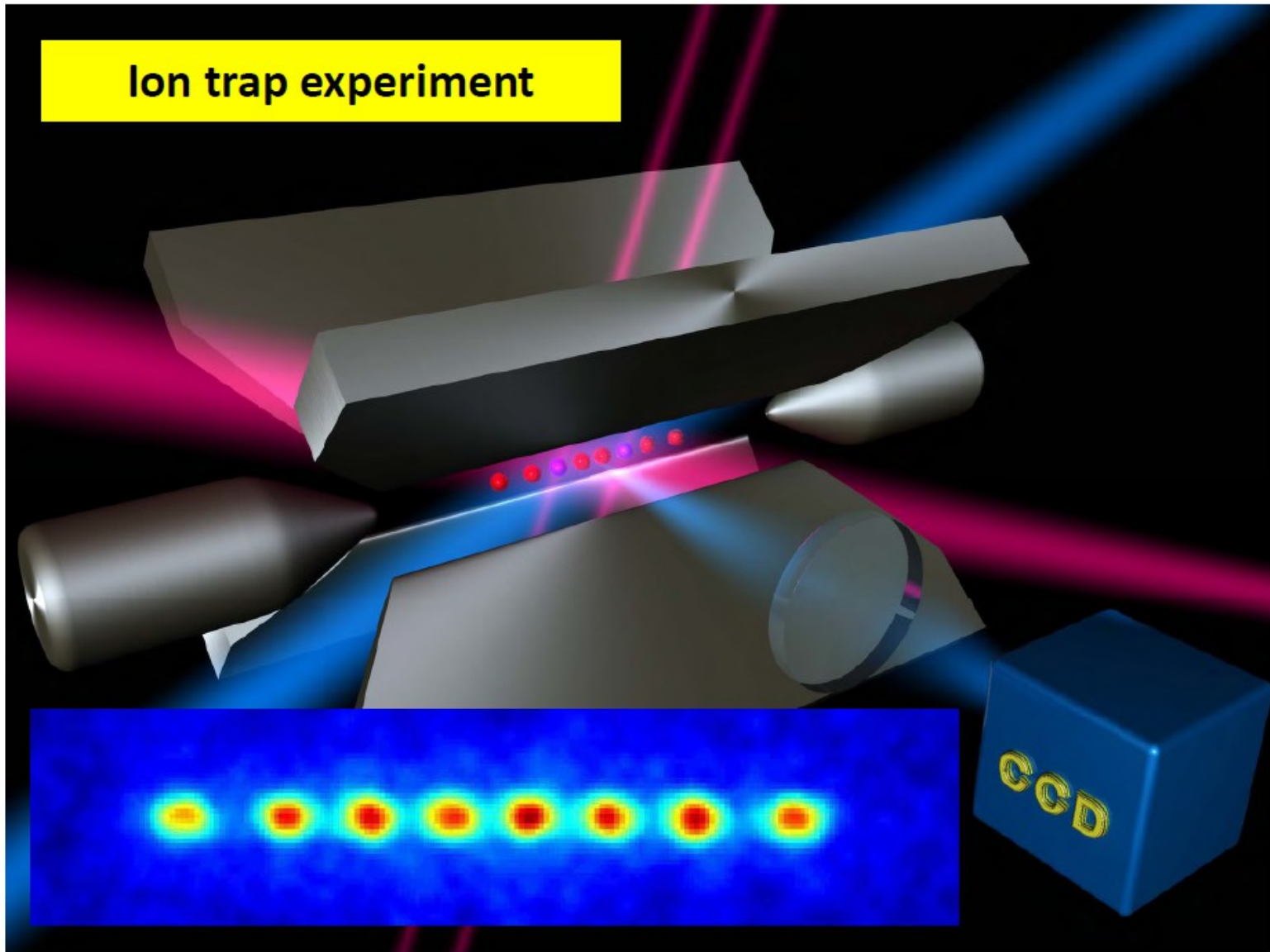


- Observed with ensembles or atoms in cavities
- For single atoms in free space usually negligible

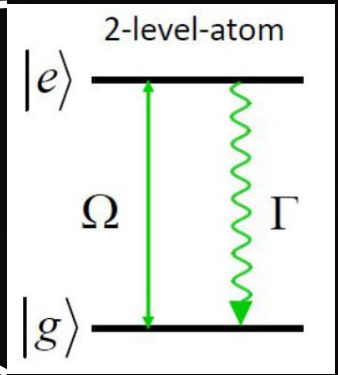
**Can we see a "shadow" of a single atom?**

# Ion trapping basics

Ion trap experiment

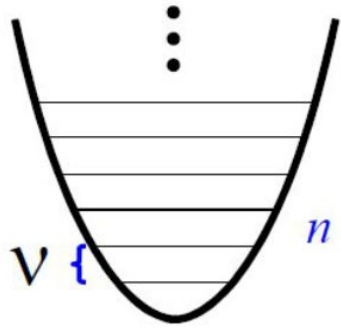


Single charged atom  
with electronic level structure

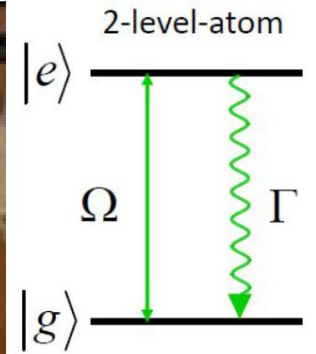


# Generation of trapping potential – Paul trap

harmonic trap

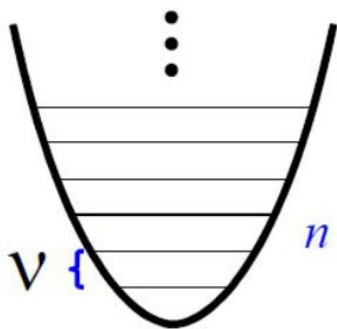


Single charged atom



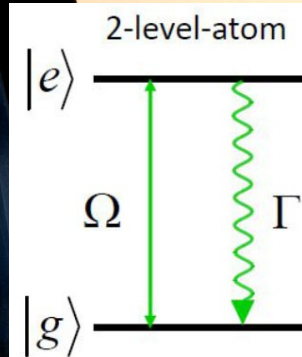
Paul trap

harmonic trap



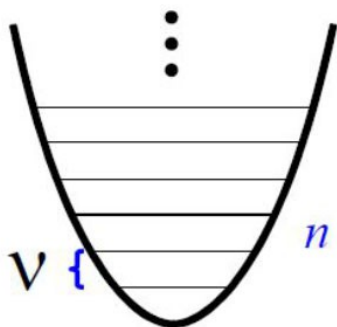
Vacuum, magnetic cage  
- isolation from environment

Single charged atom



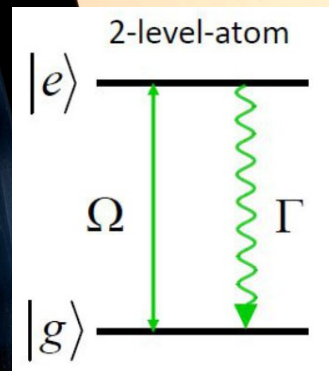
Paul trap

harmonic trap



Vacuum

Single charged atom



Exciting laser beams

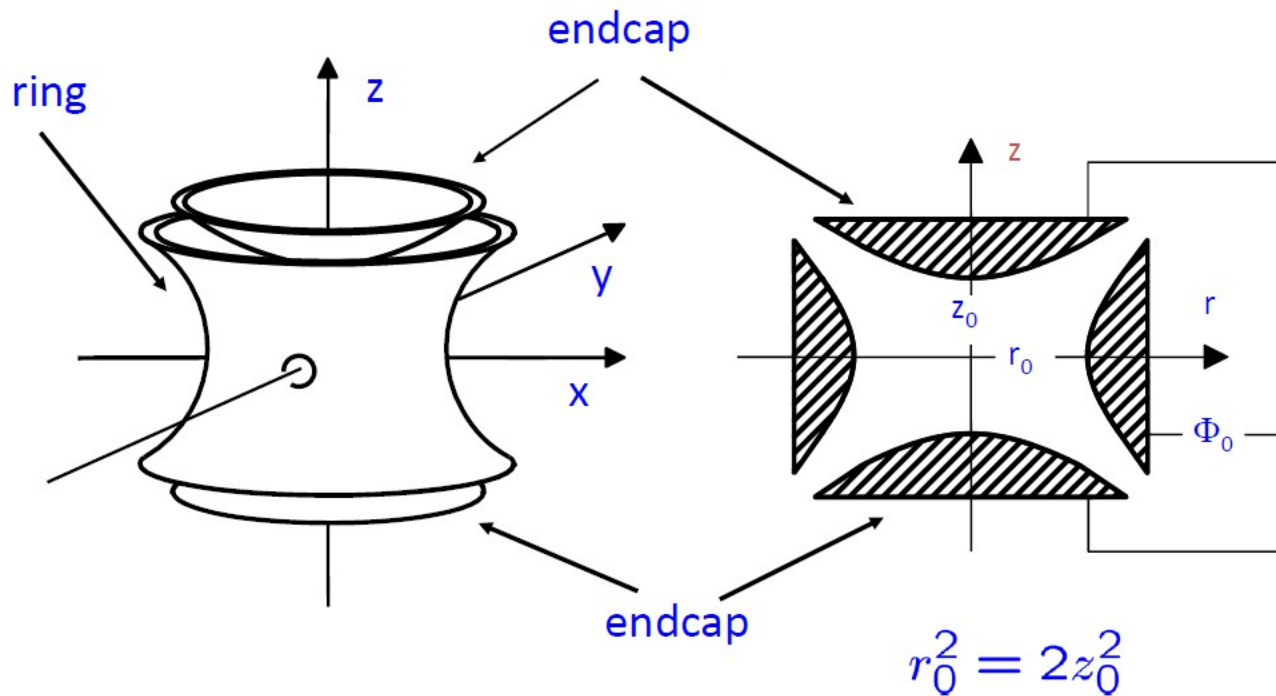
# Ion trapping basics

## Paul trap

### Do it dynamically → Paul trap

time depending potential  $\Phi(\vec{r}, t) = \Phi_0(t) \cdot (x^2 + y^2 - 2z^2)$

with  $\Phi_0(t) = (U + V \cos(\Omega_{RF}t)) / \tilde{r}^2$



- Effectively harmonic in all three dimensions

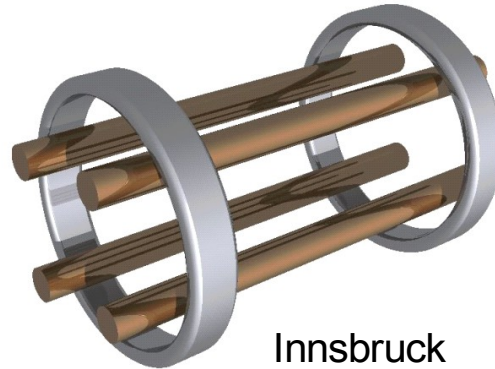
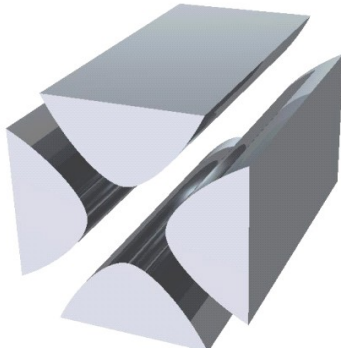


W. Paul

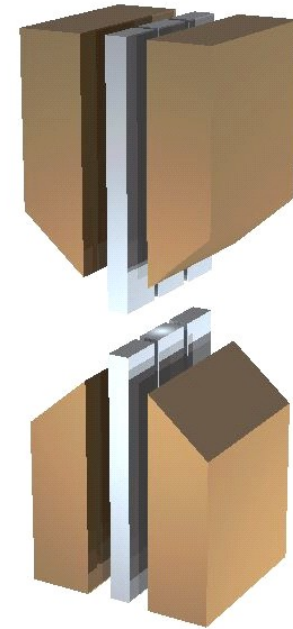
# Ion trapping basics

## Linear Paul traps

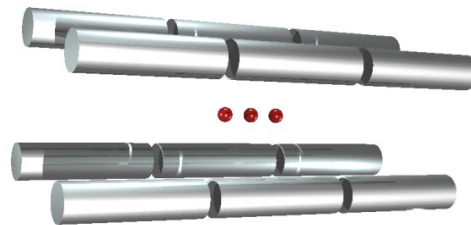
Paul mass filter



Innsbruck



Munich



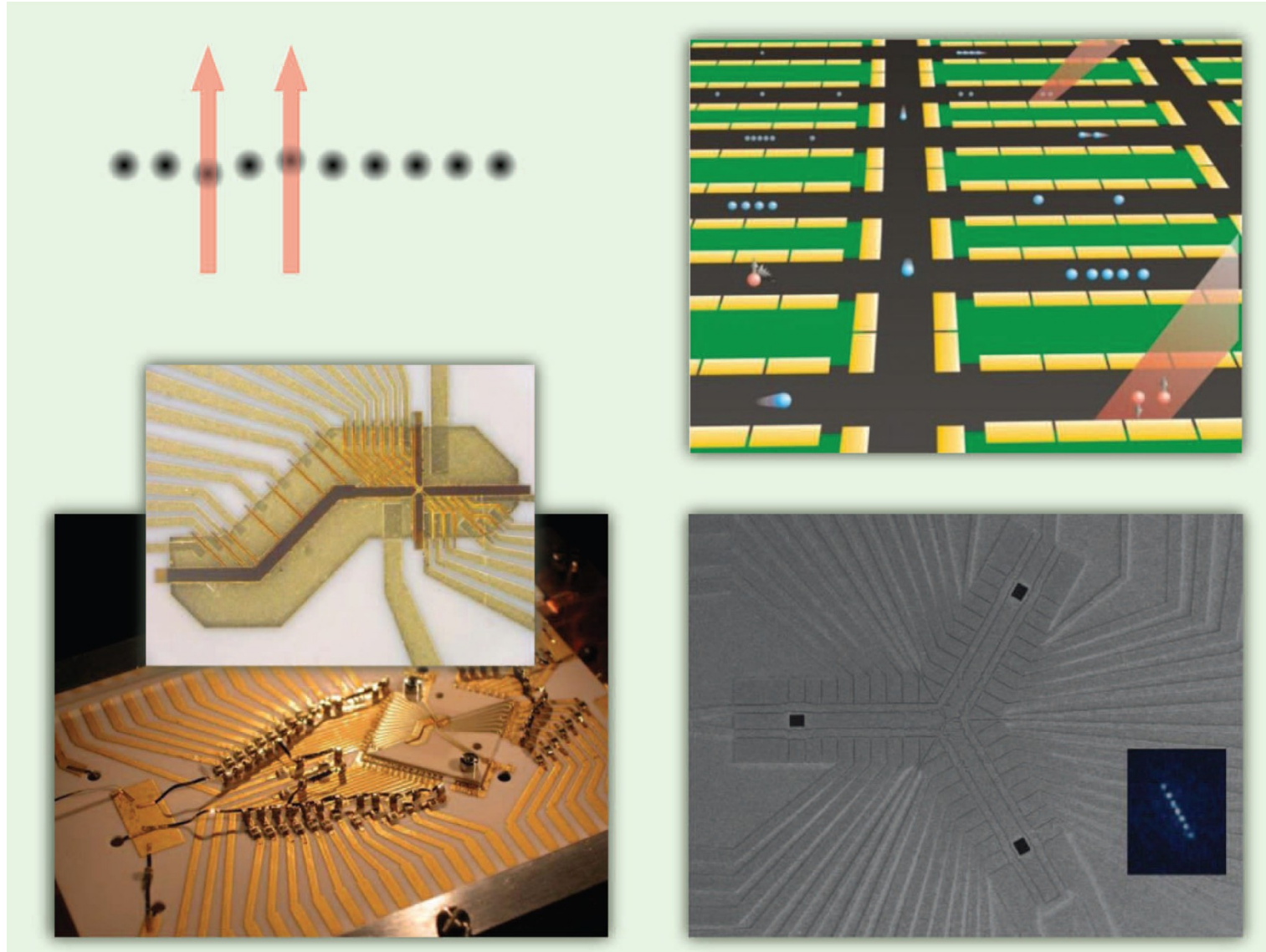
Boulder, Mainz, Aarhus



# Ion trapping basics

## Quantum charge-coupled device

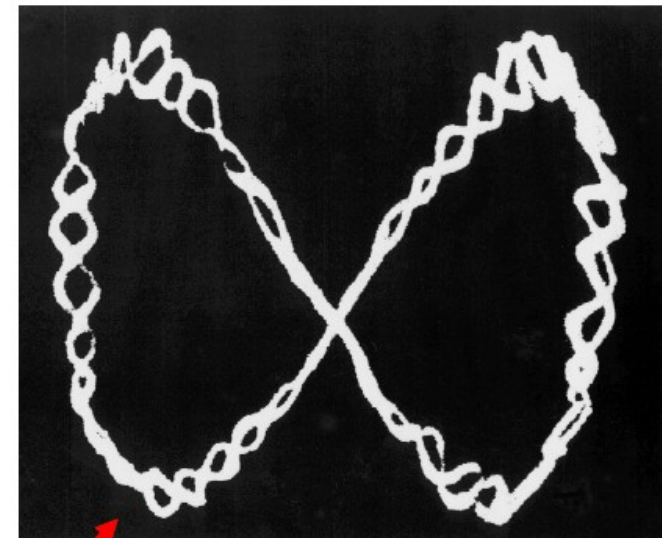
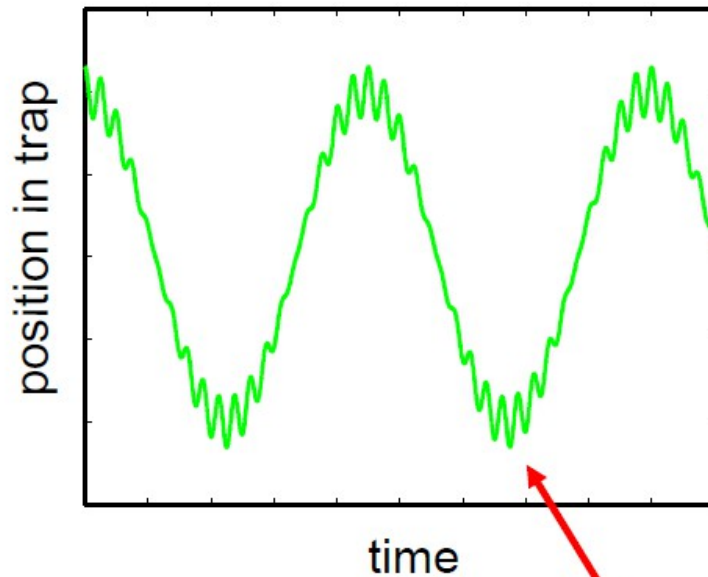
Kielpinsky, Monroe, Wineland (NIST)



# Ion trapping basics

## Classical ion motion

$$r_i(t) \propto \cos\left(\beta_i \frac{\omega_{\text{rf}}}{2} t\right) \left(1 - \frac{q_i}{2} \cos(\omega_{\text{rf}} t)\right)$$

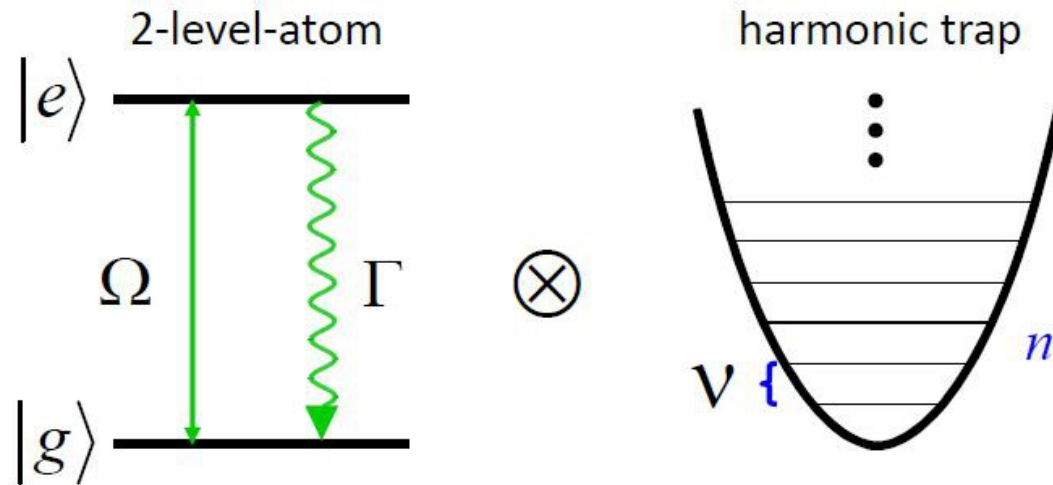


Wuerker, Shelton, Langmuir,  
J. Appl. Phys. **30**, 342 (1959)

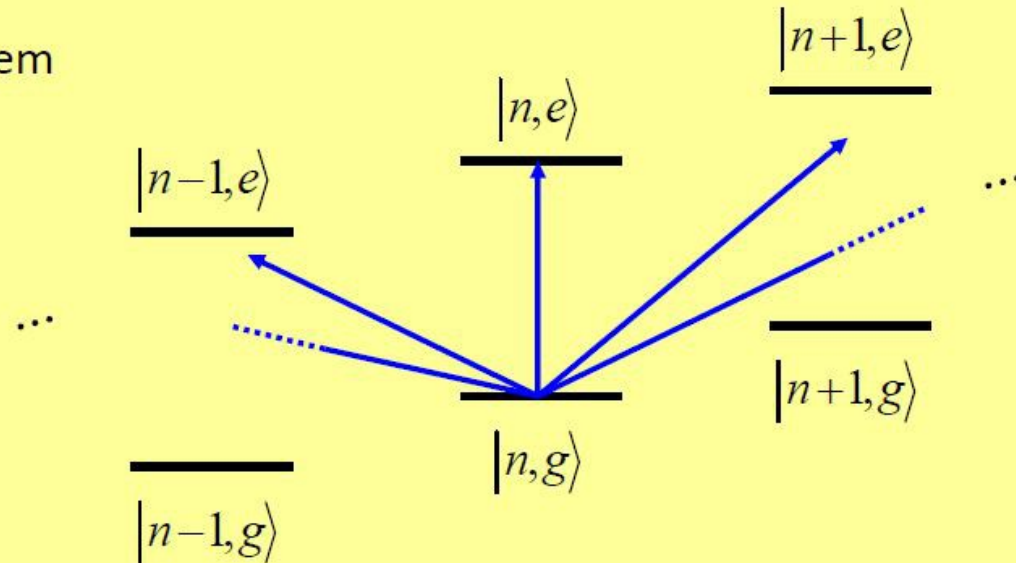
micromotion

# Ion trapping basics

## Quantized motion

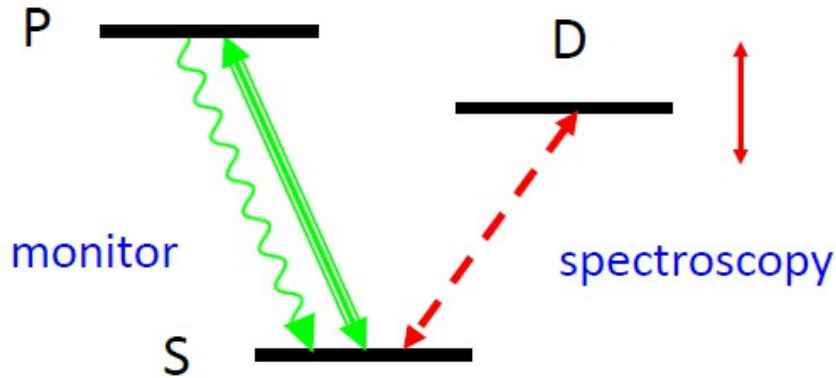


coupled system

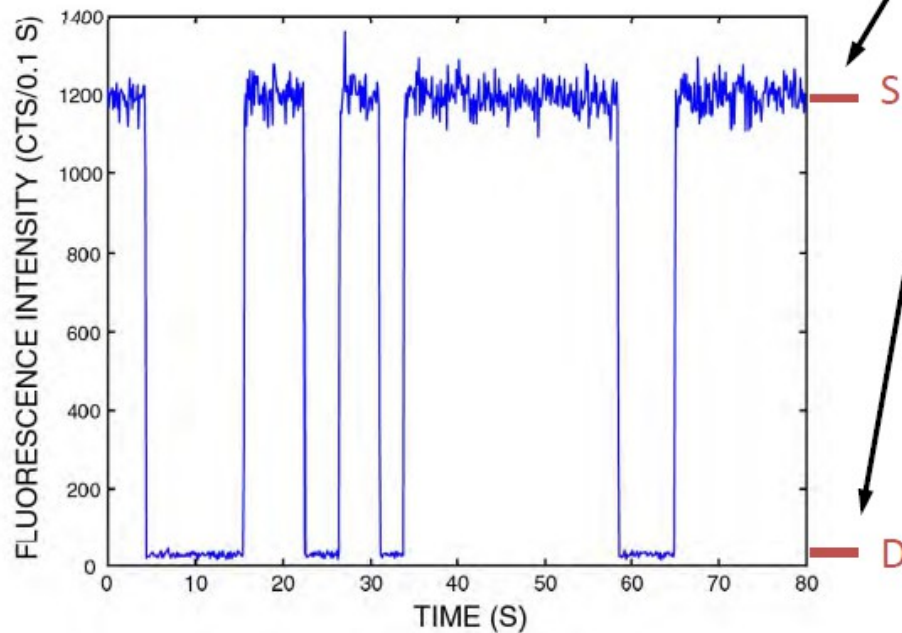


# Ion trapping basics

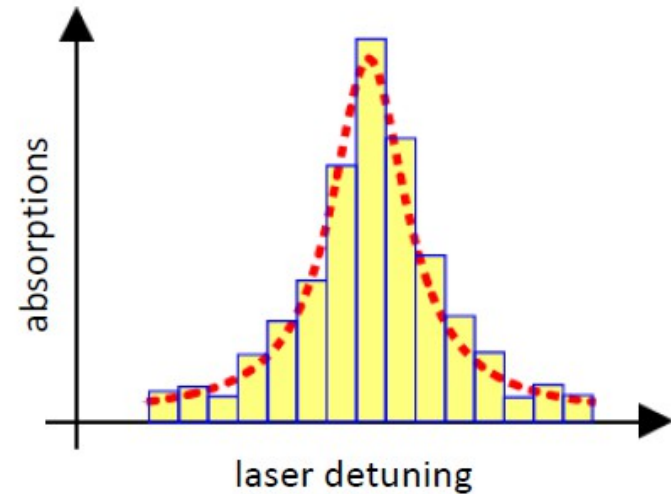
## Spectroscopy - electron shelving method



absorption and emission cause fluorescence steps  
(digital quantum jump signal)

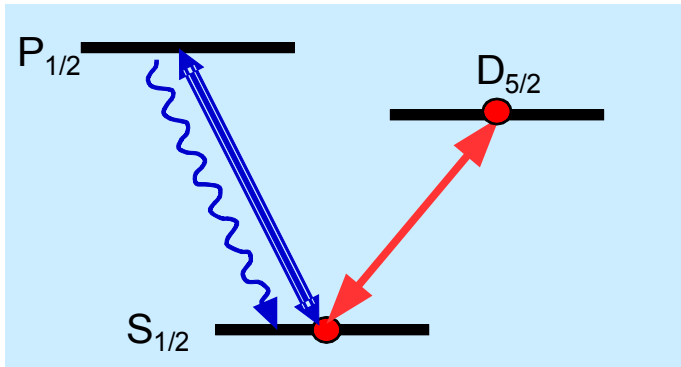


histogram of absorption events



# Ion trapping basics

## Electron shelving

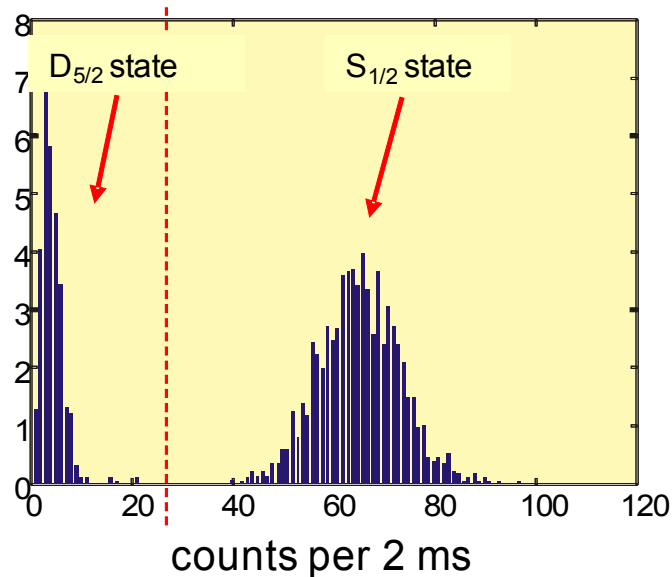


1. Initialization in a pure quantum state

2. Quantum state manipulation on  $S_{1/2} - D_{5/2}$  transition

3. Quantum state measurement by fluorescence detection

One ion : Fluorescence histogram



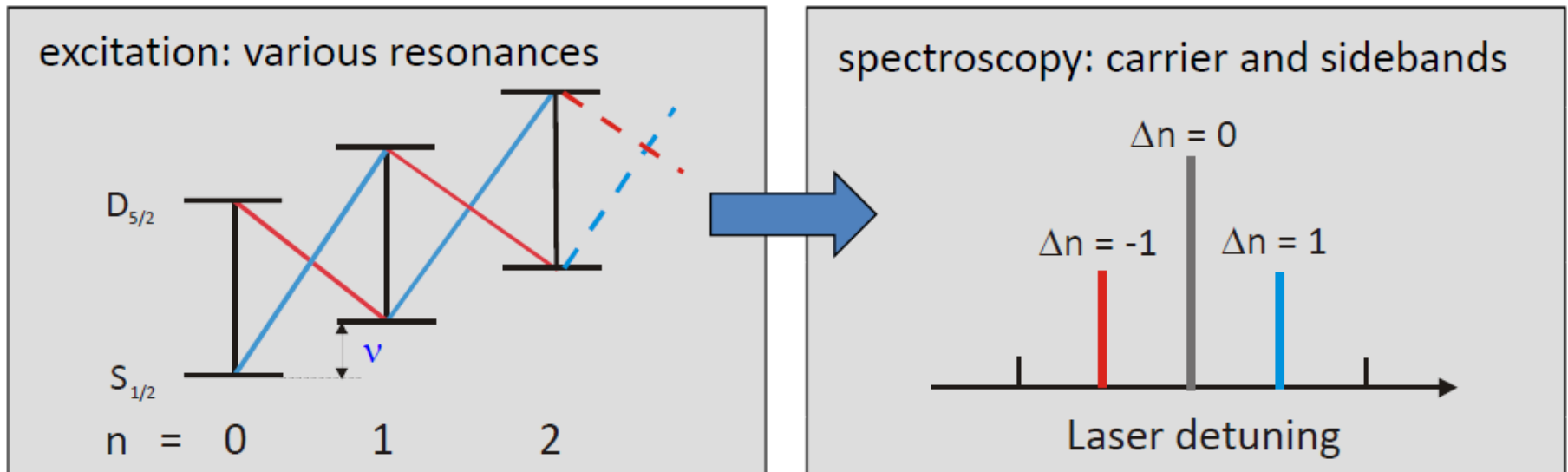
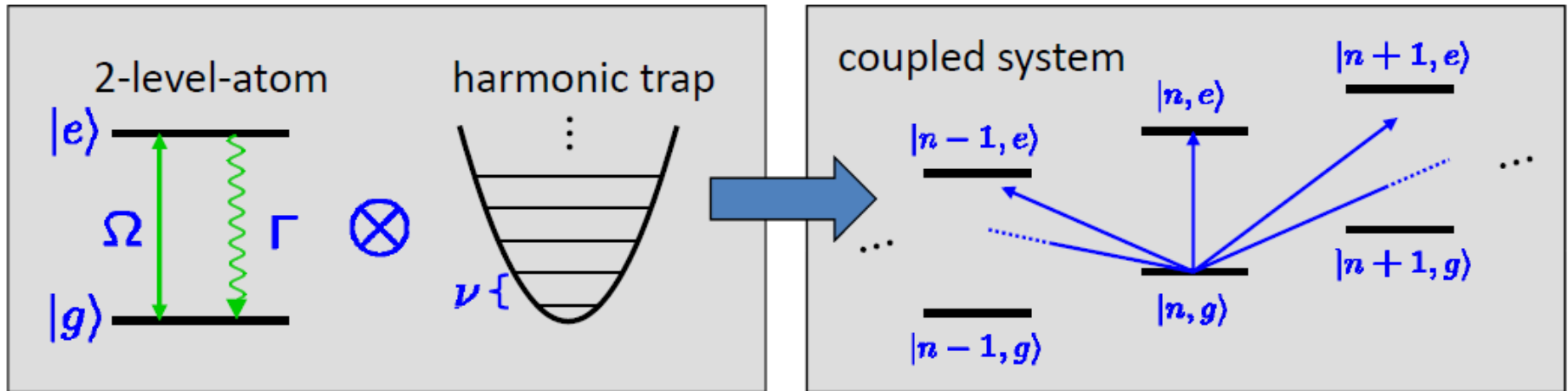
50 experiments / s

Repeat experiments  
100-200 times

**Detection efficiency → 100 %**

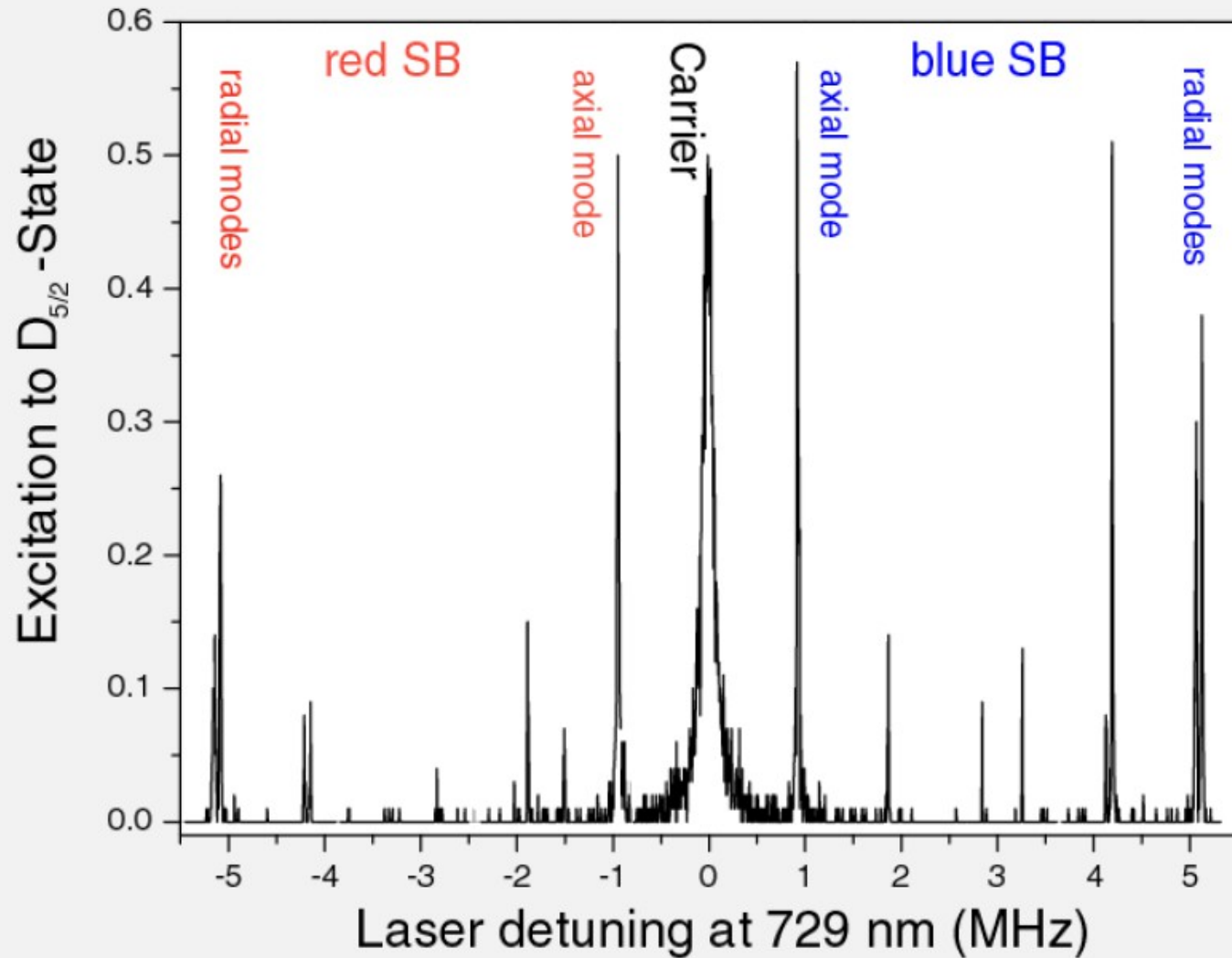
# Ion trapping basics

## Laser – ion interactions in Lamb-Dicke regime



# Ion trapping basics

## Excitation spectrum



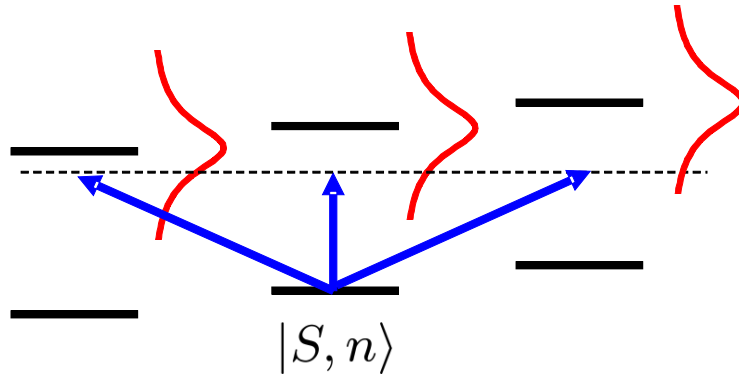
$$\omega_{\text{ax}} = 1.0 \text{ MHz}$$

$$\omega_{\text{rad}} = 5.0 \text{ MHz}$$

# Ion trapping basics

## Laser cooling of ions

### Doppler cooling

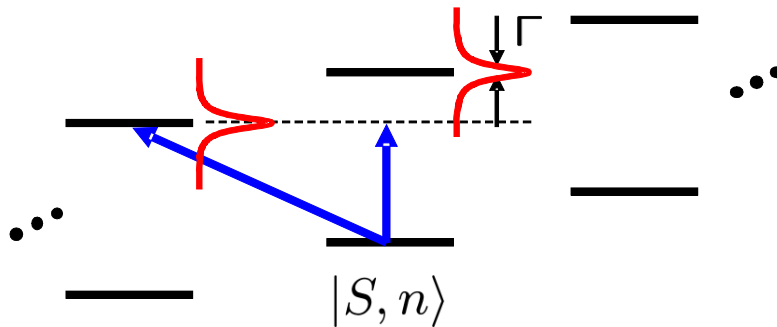


$\nu \ll \Gamma$  **weak** confinement,  
Doppler cooling

$$\langle n \rangle = \frac{\Gamma}{2\nu} > 1$$

if laser detuned by  $\Delta = -\Gamma/2$

### Sideband cooling



$\nu \gg \Gamma$  **strong** confinement,  
sideband cooling

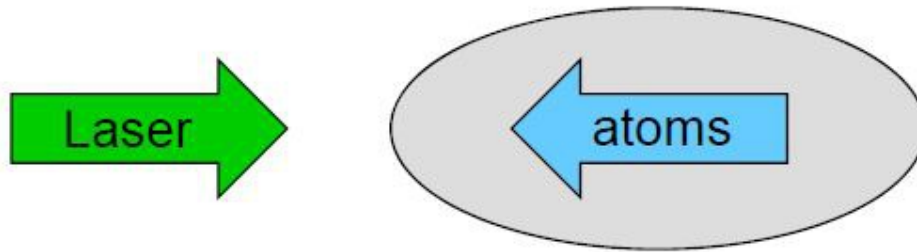
$$\langle n \rangle = \frac{\Gamma^2}{4\nu^2} \ll 1$$

if laser detuned by  $\Delta = -\nu$

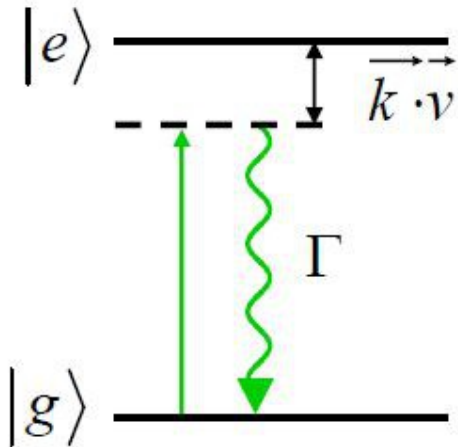
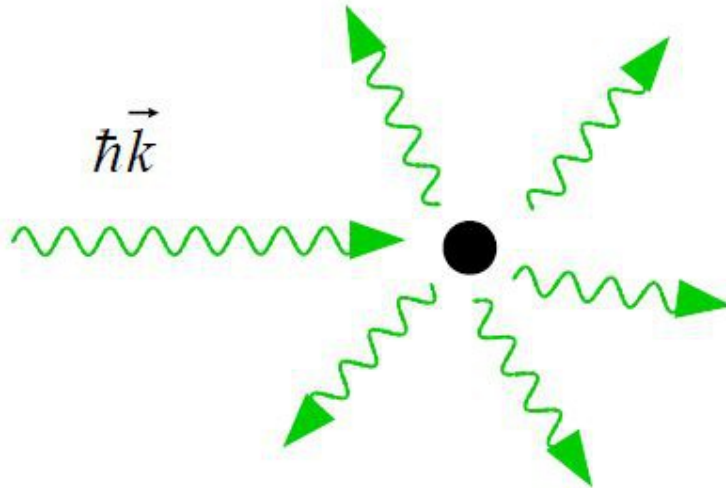


# Ion trapping basics

## Doppler cooling



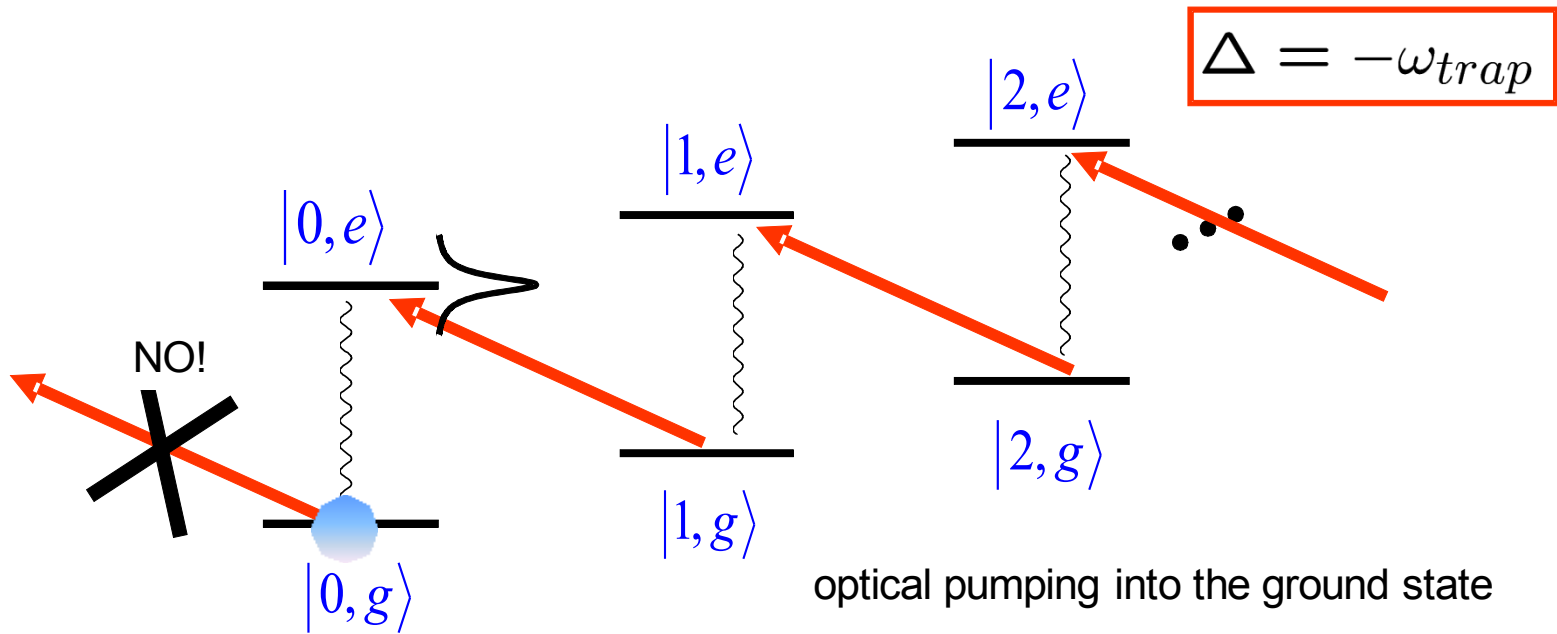
momentum transfer  $\hbar\vec{k}_{abs}$ ,  $-\hbar\vec{k}_{em}$



$$\Delta\vec{p} = n\hbar\vec{k}_{abs} + \underbrace{\sum \hbar\vec{k}_{em}}_{=0}$$

Doppler cooling limit:

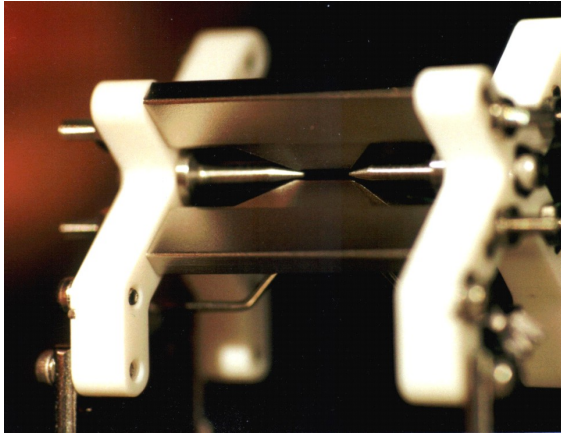
$$E_D = \hbar \frac{\Gamma}{2}$$



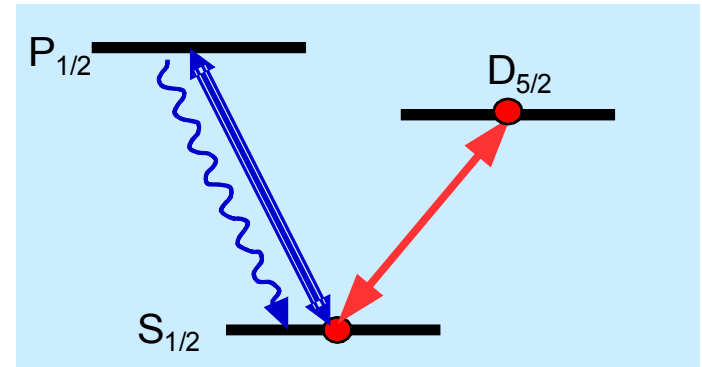
**Signature:** no further excitation possible  
„dark state“  $|0\rangle$

# Summary – ion trapping basics

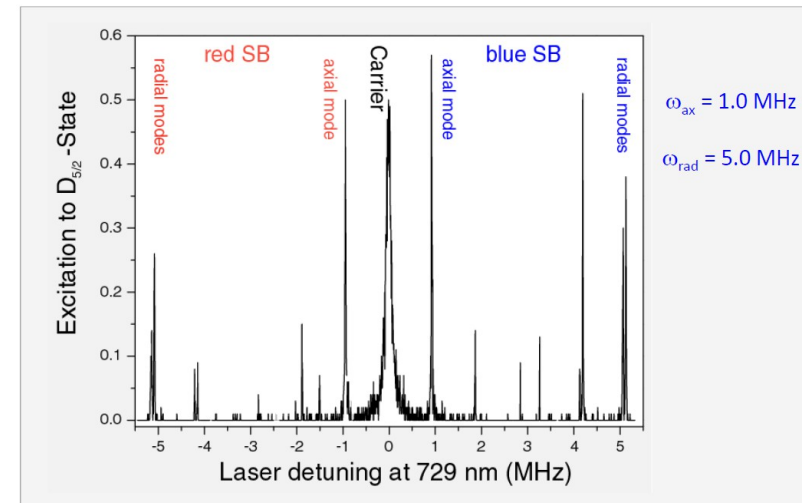
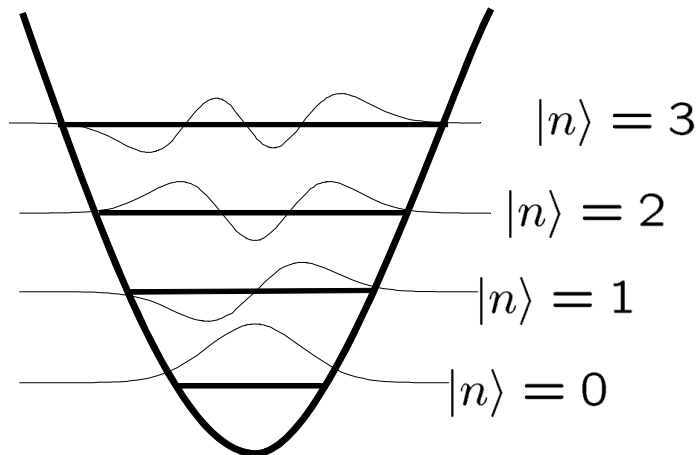
Trapping of charged particles → Paul traps



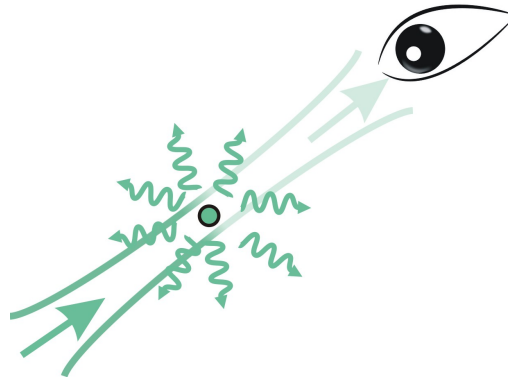
Precise spectroscopy → electron shelving



Ion's motion → Quantum harmonic oscillator

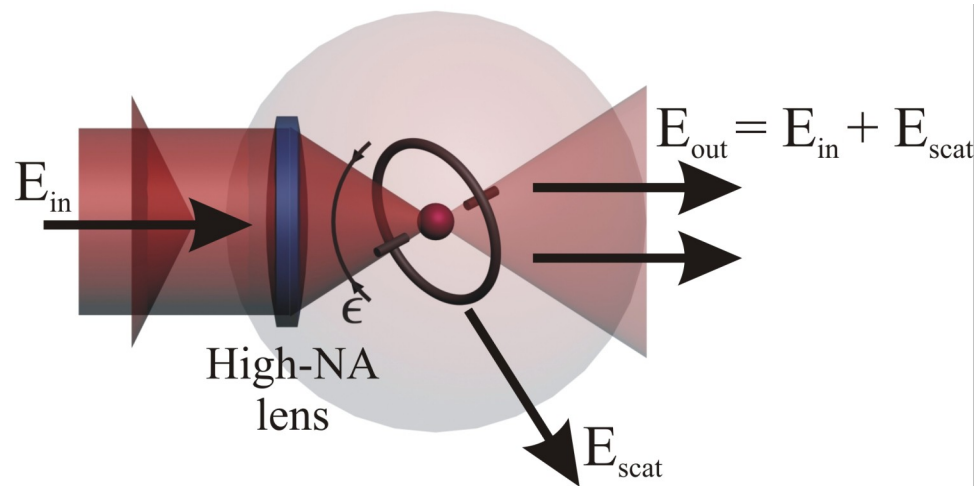


Can we see a "shadow" of a single atom?



# Extinction

## Extinction from single atom in free space



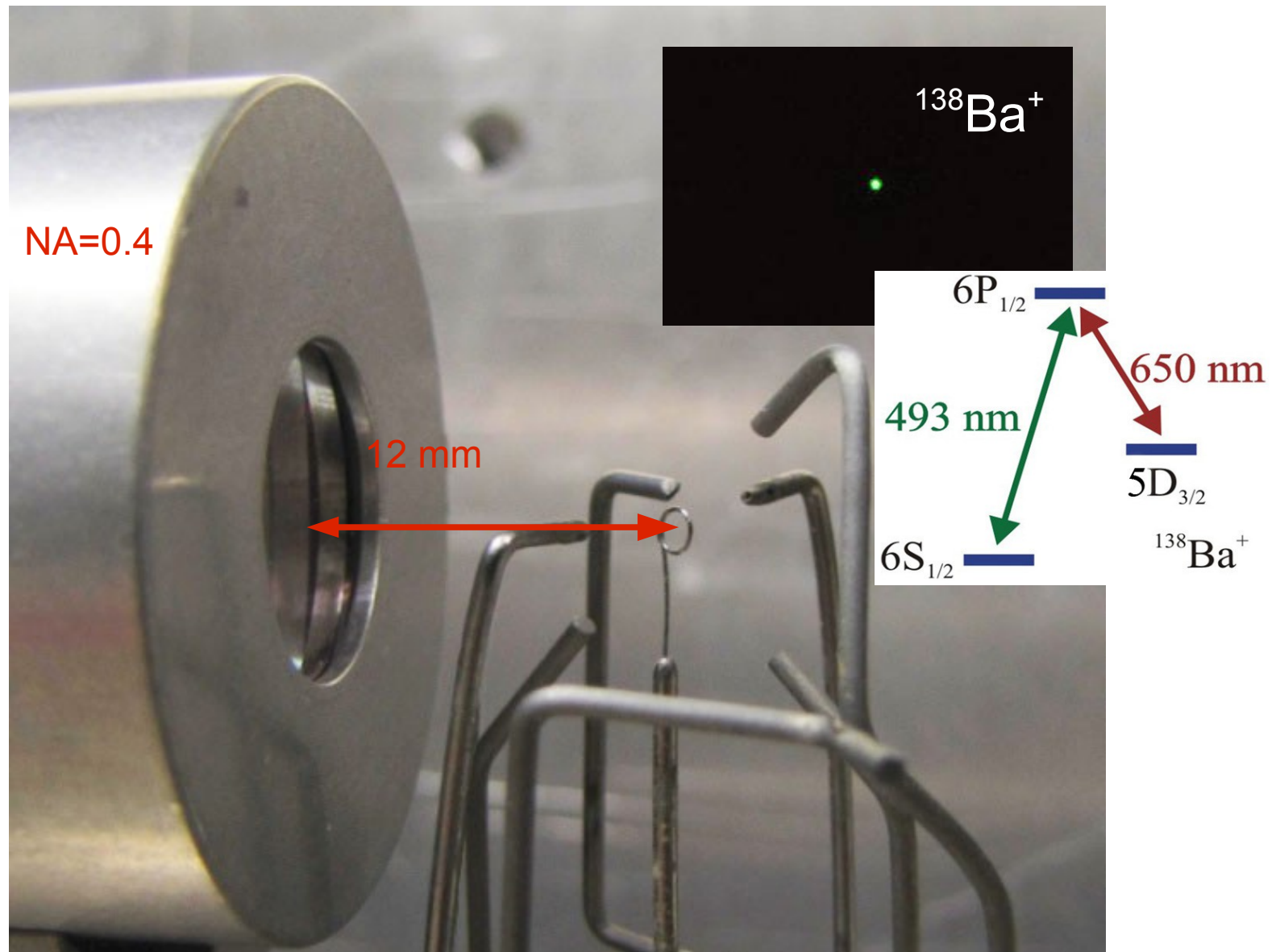
- Destructive interference of scattered and transmitted fields!
- In the weak probe limit

$$T = |1 - 2\epsilon|^2$$

**Full reflection for lens covering half of the full solid angle!**

# Extinction

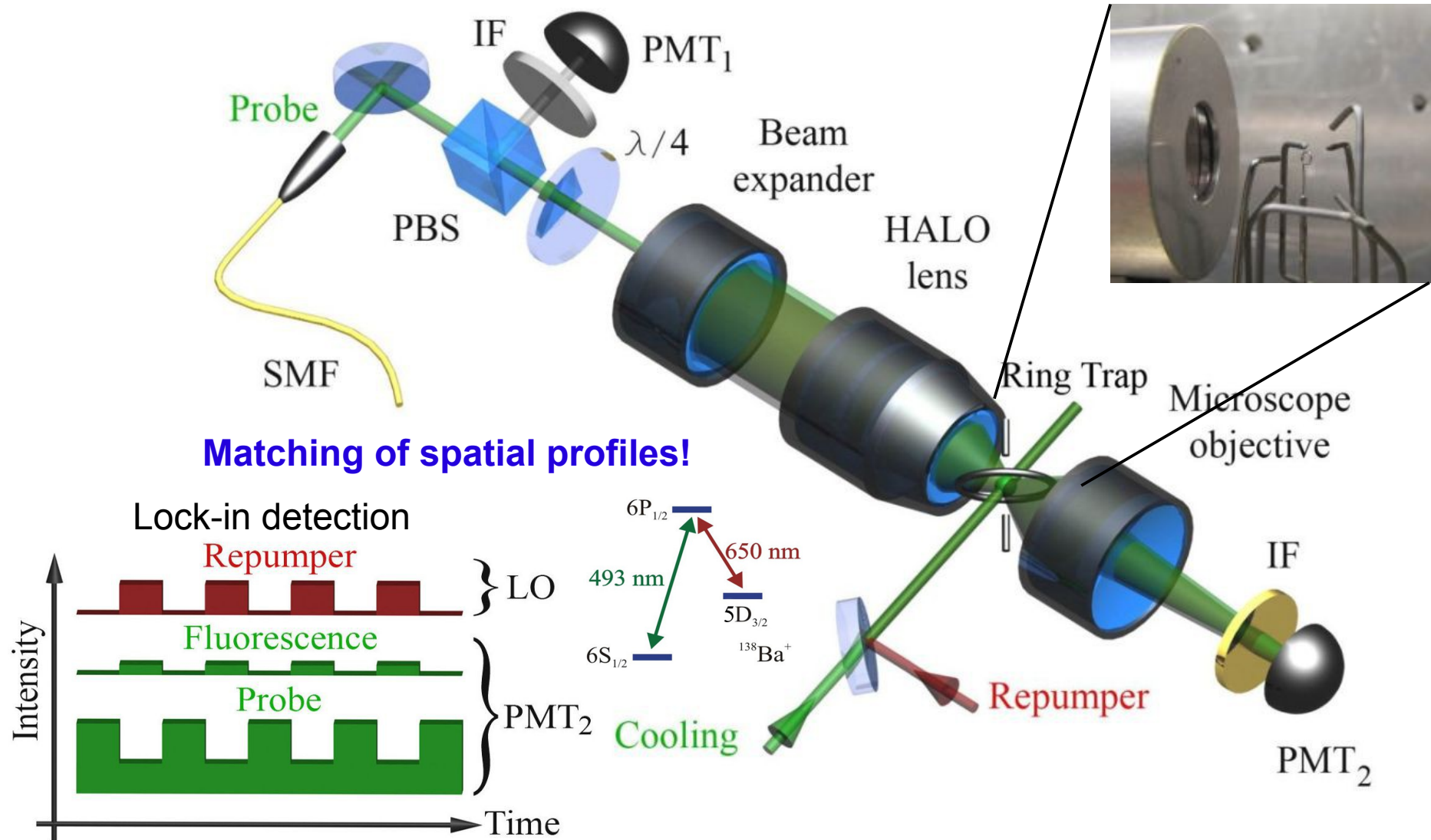
## Ring trap



# Extinction

## Extinction from single atom in free space

### Experimental setup



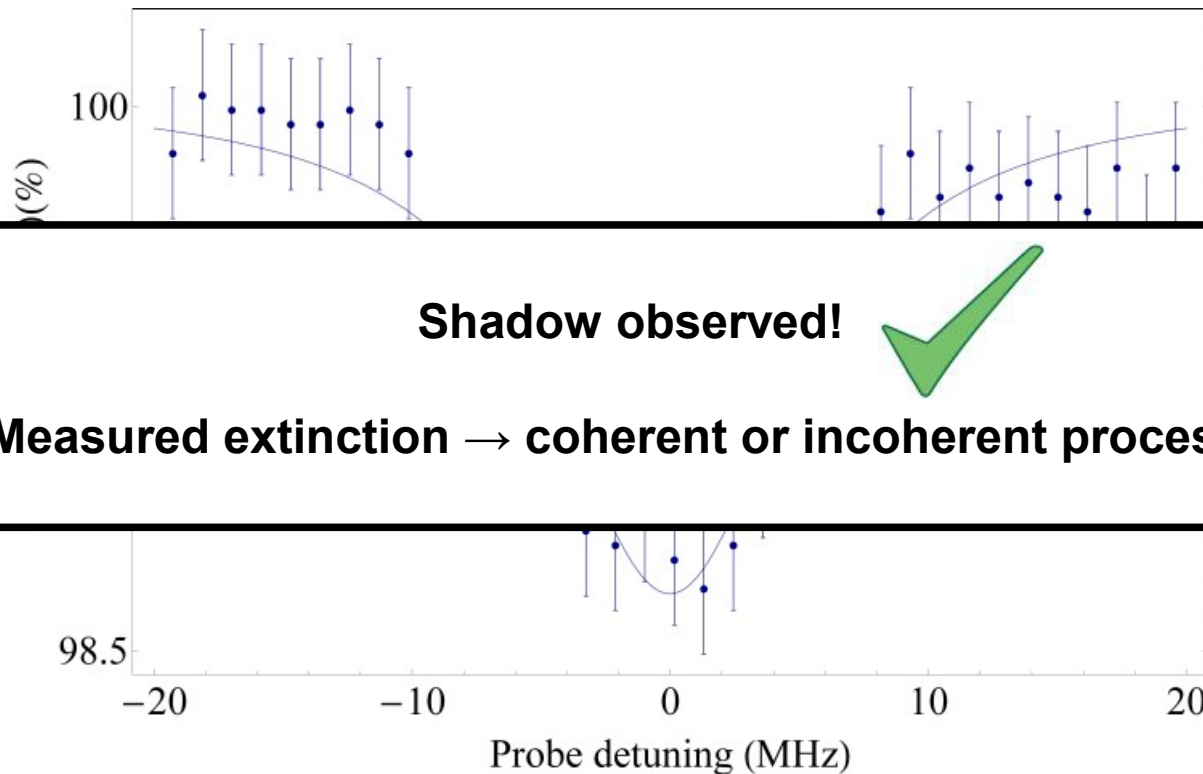
# Extinction

## Extinction from single atom in free space

### Results

#### Extinction of 1.35%

Good agreement with our effective solid angle  $\varepsilon \sim 0.01$ !



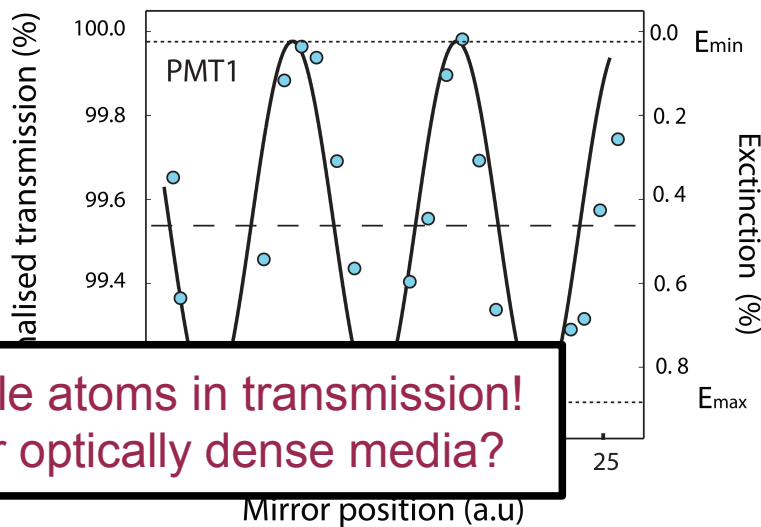
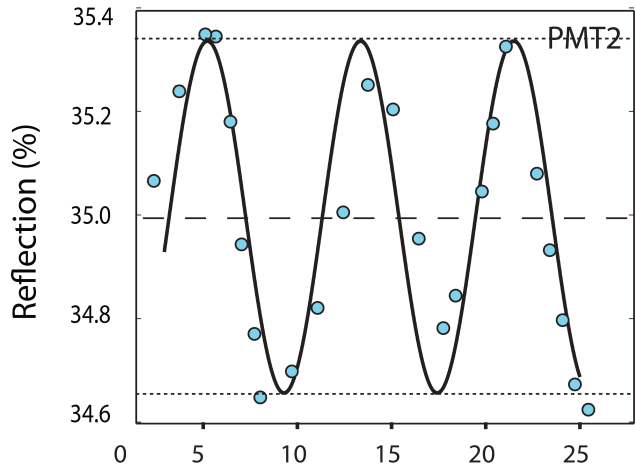
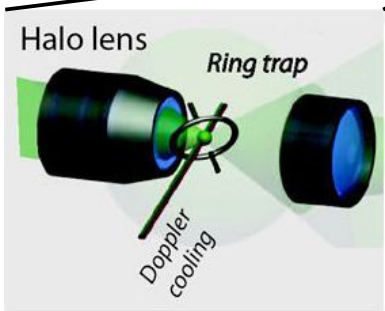
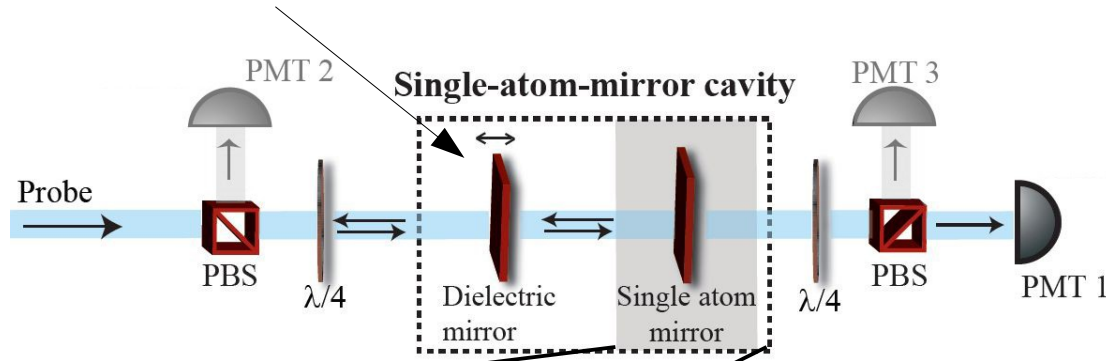


# Extinction

## Single-atom-mirror

Fabry-Pérot like cavity setup formed by single atom and dielectric mirror

$$|r|^2 = 1 - |t|^2 = 0.35$$



G. Hétet, L. Slodička, M. Hennrich, and R. Blatt,  
 Phys. Rev. Lett. **107**, 103602 (2011)

We can now observe properties of single atoms in transmission!  
 Can we now observe effects typical for optically dense media?

Merging  
 and free-space coupling

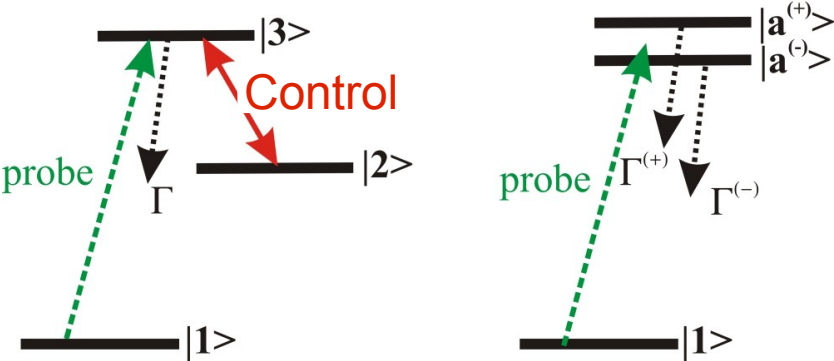
Mirror position (a.u.)

# Extinction

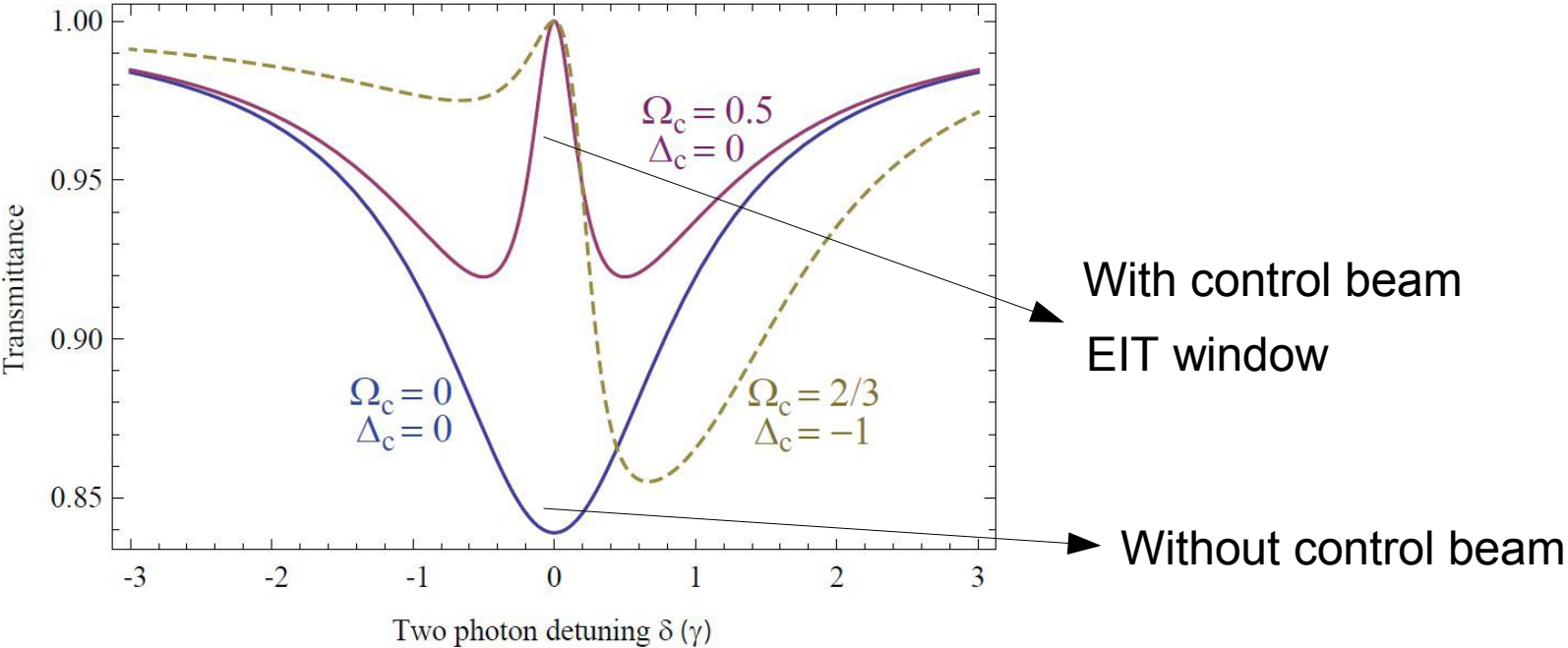
## Electromagnetically induced transparency

Coherent optical process which renders a medium transparent over a narrow spectral range within an absorption line

### Principle

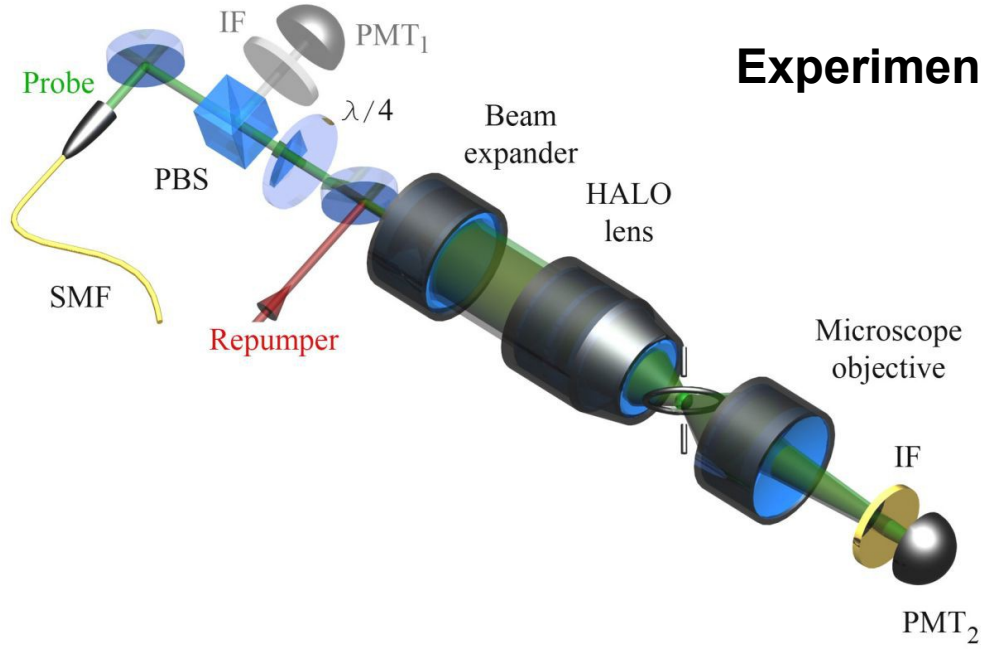


Interference of two decay channels



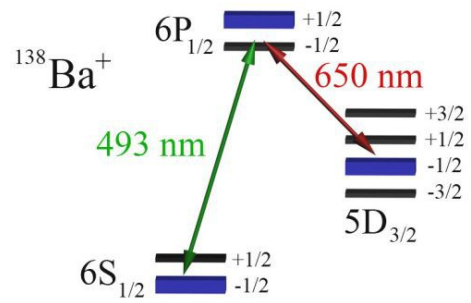
# Extinction

## Electromagnetically induced transparency

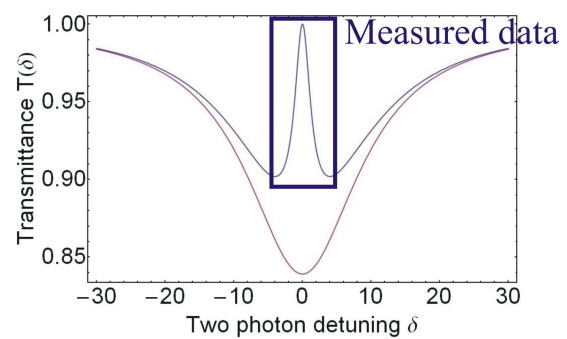
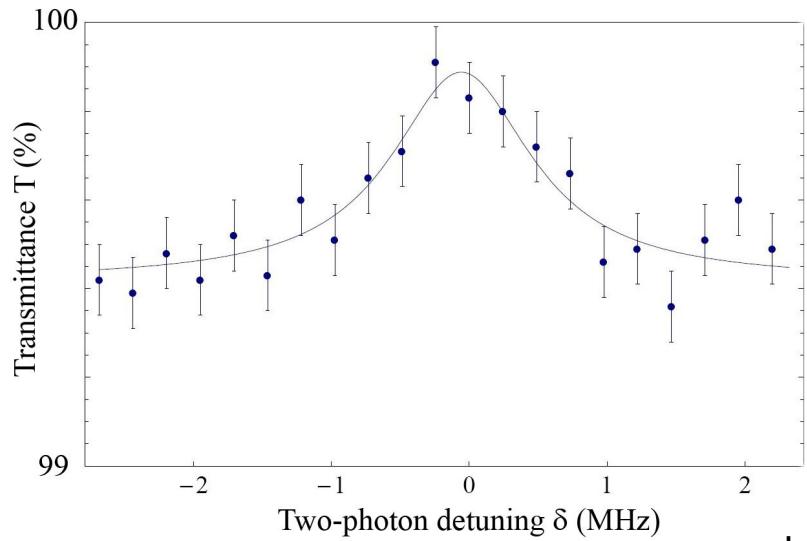


### Experimental setup

- Cooling by the probe beam
- Co-propagation of the beams



### Results

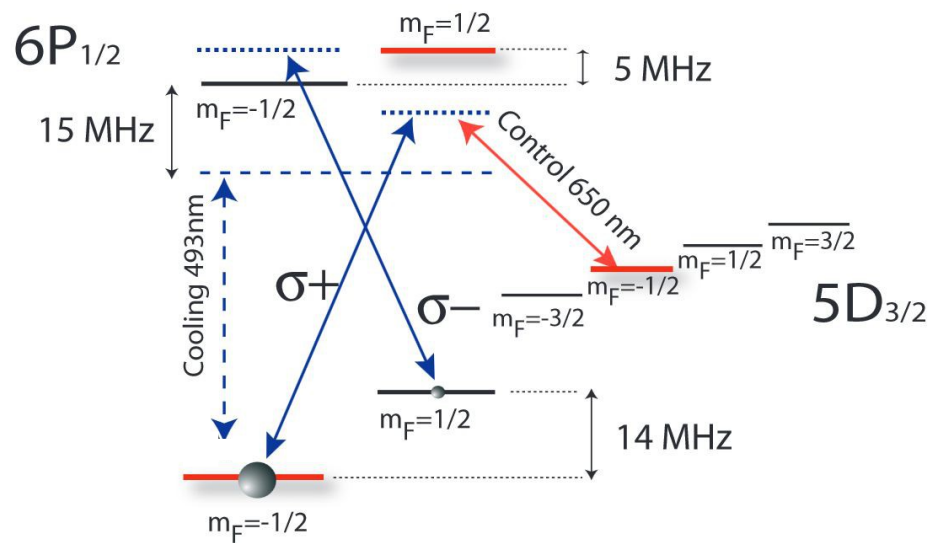
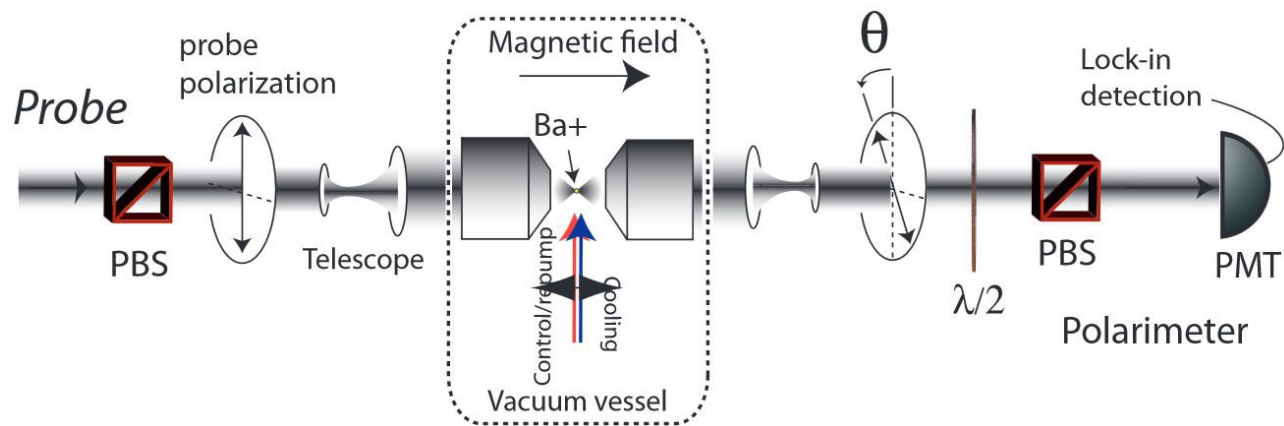


**Extinction suppression of 75%**  
**Subnatural linewidth of 1.2MHz**

# Extinction

## Phase-shift measurements

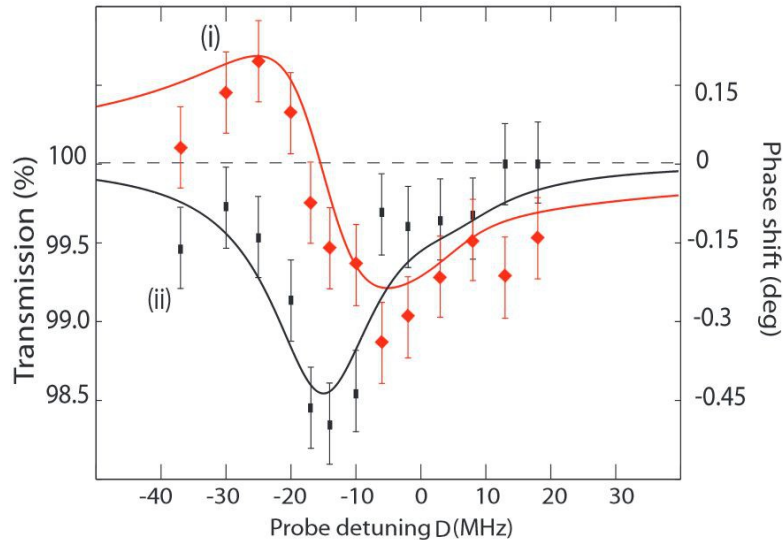
### Experimental setup



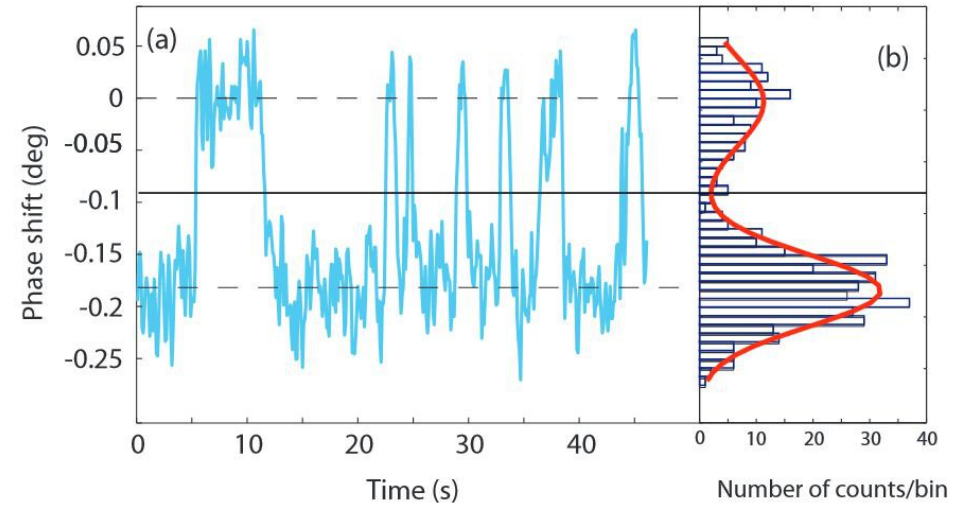
# Extinction

## Phase-shift measurements

### Faraday Rotation



### State read-out



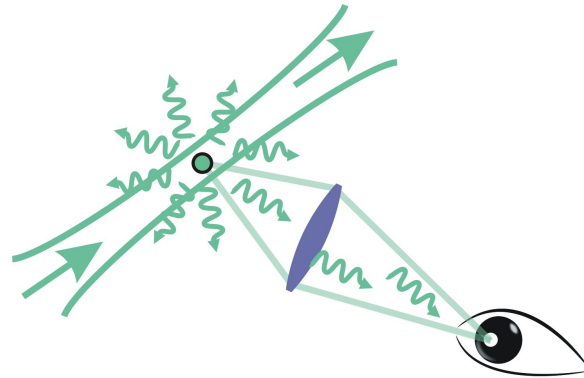
**We can observe extinction from single atom**

**Extinction corresponds to a coherent process**

**We can manipulate it by control beam using EIT**

**We can measure phase shift induced by single atom**

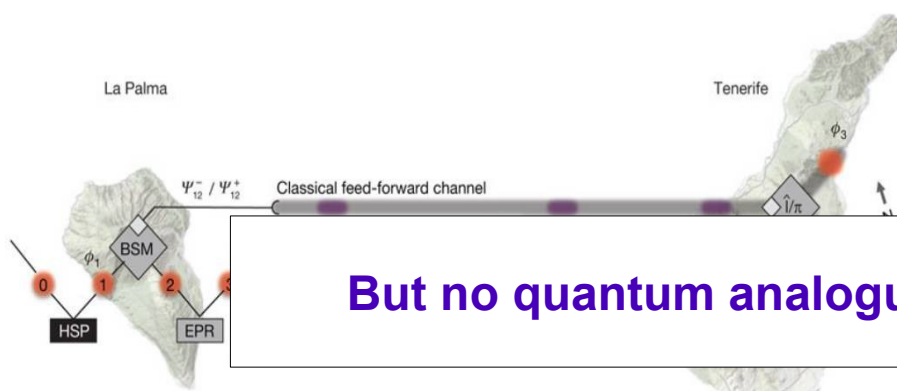
**Quantum communication using detection of scattered fluorescence?**



# Atom-atom entanglement

## Quantum communication

- Absolutely secure communication (Quantum cryptography)
- Faithful transfer of unknown quantum state (Quantum teleportation)



Nature **489**, 269–273 (2012)

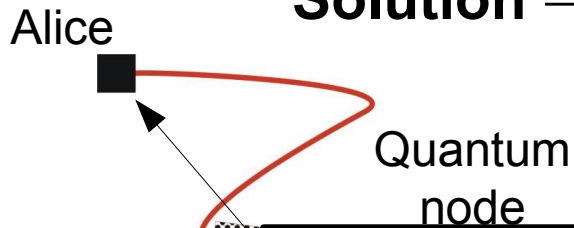


New J. Phys. **13** 123001 (2011)

**But no quantum analogue of classical amplifier!**

**Solution → generation of distant entanglement**

**Nodes ~ light-matter interfaces**



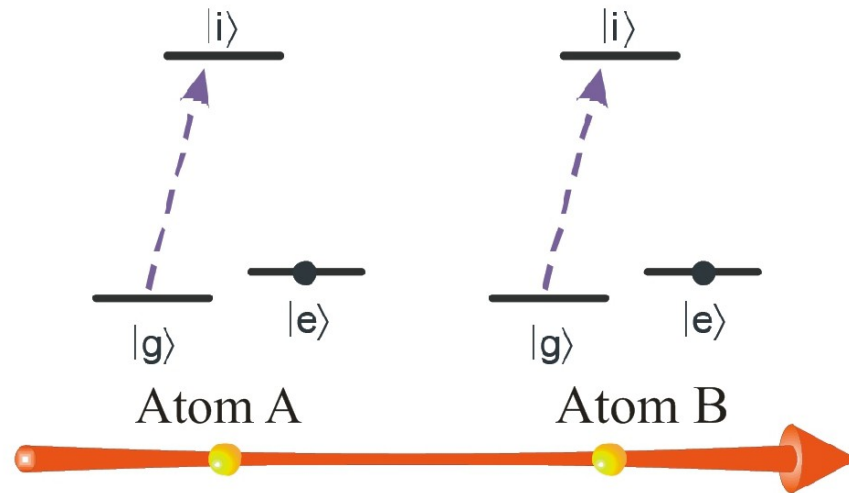
**Distribution of entanglement by mere observation of scattered photon?**

# Atom-atom entanglement

## Single-photon scheme

C. Cabrillo et al. PRA 59, 1025-1033 (1999)

### Initialization and weak excitation



#### 1. Initialization:

atoms (A,B) in the same state  $|gg\rangle$

#### 2. Weak excitation:

with  $p_e \ll 1$  through a spontaneous Raman process

→ *Atom-photon entanglement:*

$$\sqrt{1 - p_e} |g, 0\rangle + \sqrt{p_e} |e, 1\rangle e^{i\phi_D - i\phi_L}$$

Phase acquired from  
atom to detector

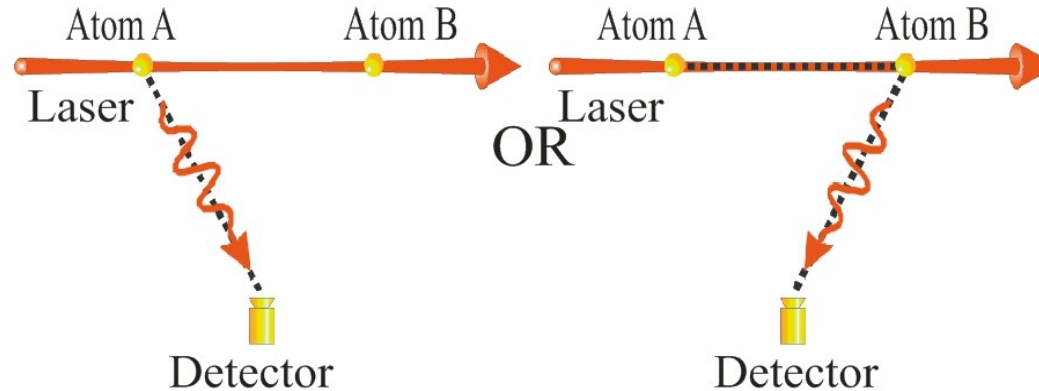
Excitation laser  
phase



# Atom-atom entanglement

## Single-photon scheme

### Projective measurement of a Raman scattered photon



#### 3. Overlapping the corresponding photonic modes

$$(1 - p_e) e^{i(\phi_{L,A} + \phi_{L,B})} |gg, 0\rangle + \sqrt{p_e(1 - p_e)} (e^{i(\phi_{L,A} + \phi_{D,B})} |eg, 1\rangle + e^{i(\phi_{L,B} + \phi_{D,A})} |ge, 1\rangle) + p_e e^{i(\phi_{D,A} + \phi_{D,B})} |ee, 2\rangle$$

#### 4. Projection by detection:

$$|\Psi^\phi\rangle = \frac{1}{\sqrt{2}} (|eg\rangle + e^{i\phi} |ge\rangle)$$

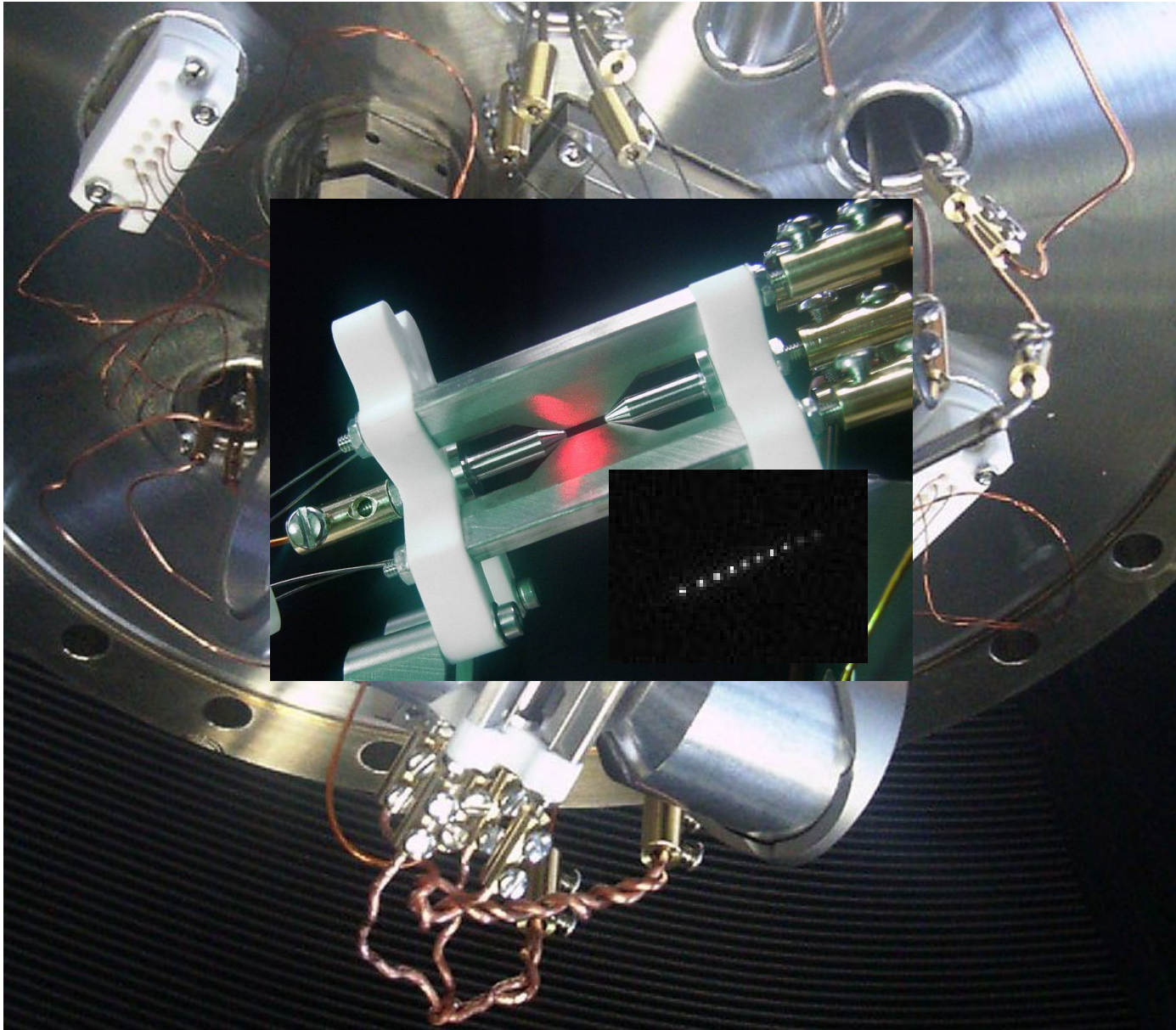
**Interference:** final entangled state depends on distance between atoms

+

**Projective measurement:** detection of a *single* Raman-scattered photon

# Atom-atom entanglement

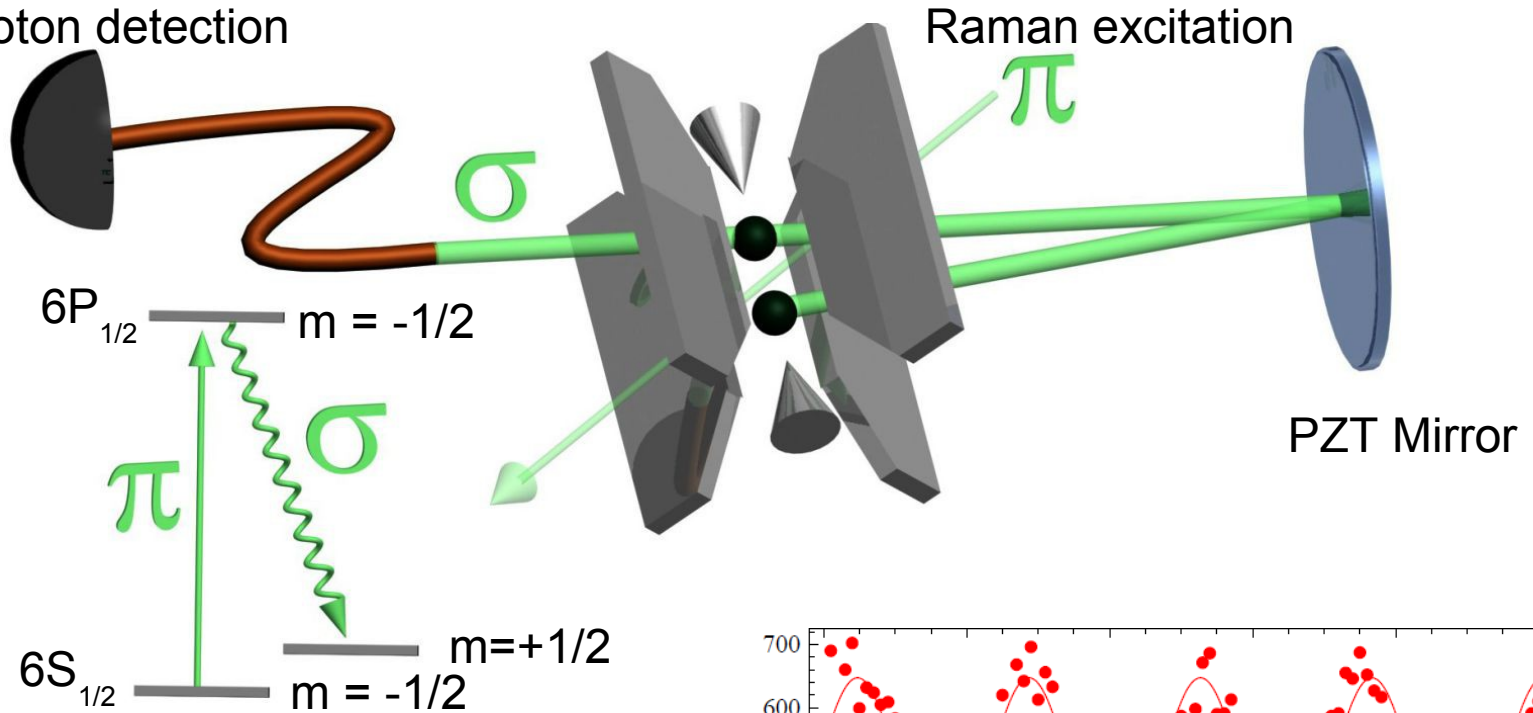
## Linear trap



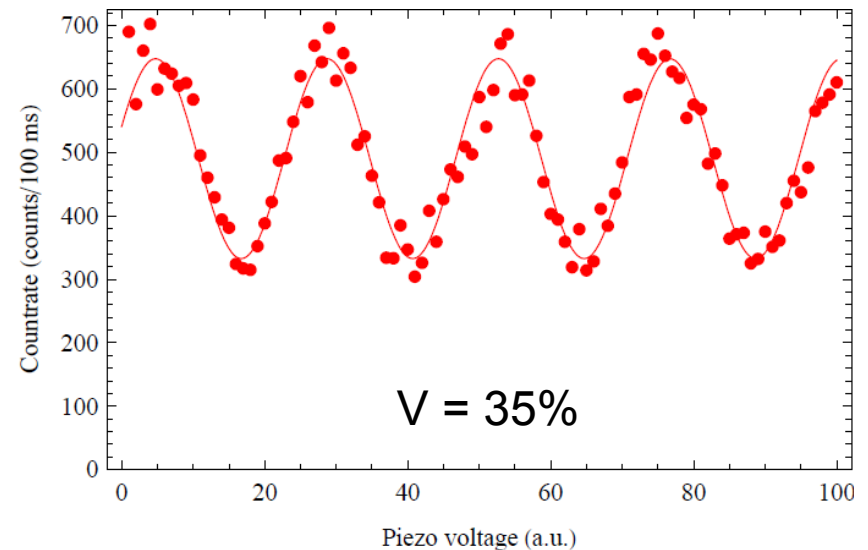
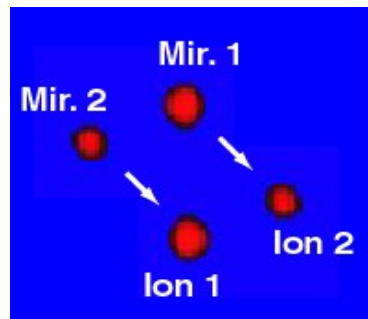
# Atom-atom entanglement

## Experimental setup

Single photon detection



Two ions interfering with their mirror images



We can hold the phase and control the ion-ion distance to within  $\lambda/10$

# Atom-atom entanglement

## Indistinguishability measurements

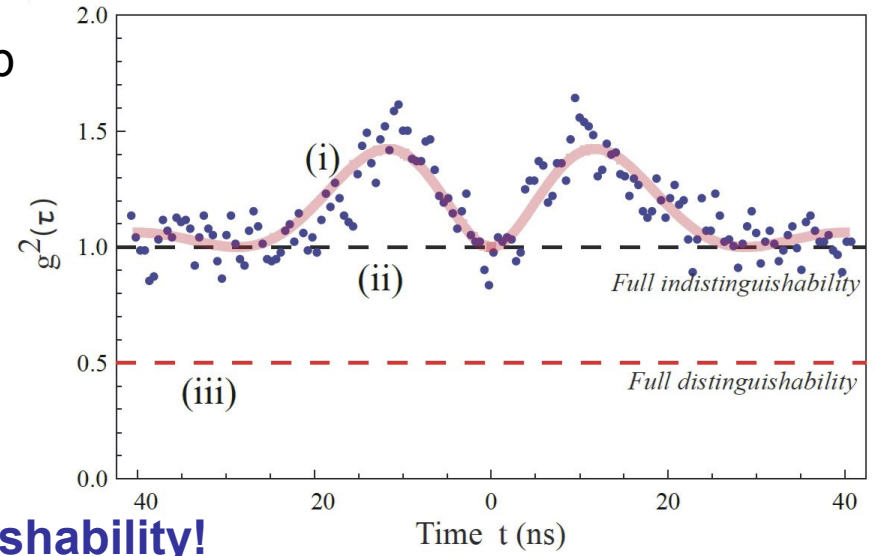
• **2nd order coherence**

$$g_{\text{Tot}}^{(2)}(\tau) = \frac{1}{2} (g^{(2)}(\tau) + |e_1 e_2|^2 |g^{(1)}(\tau)|^2 + 1)$$

mode overlap
single-ion functions

two-ion  $g^{(2)}$

$$g_{\text{Tot}}^{(2)}(0) = 0.98 \pm 0.07$$



**Good spatial and polarization indistinguishability!**

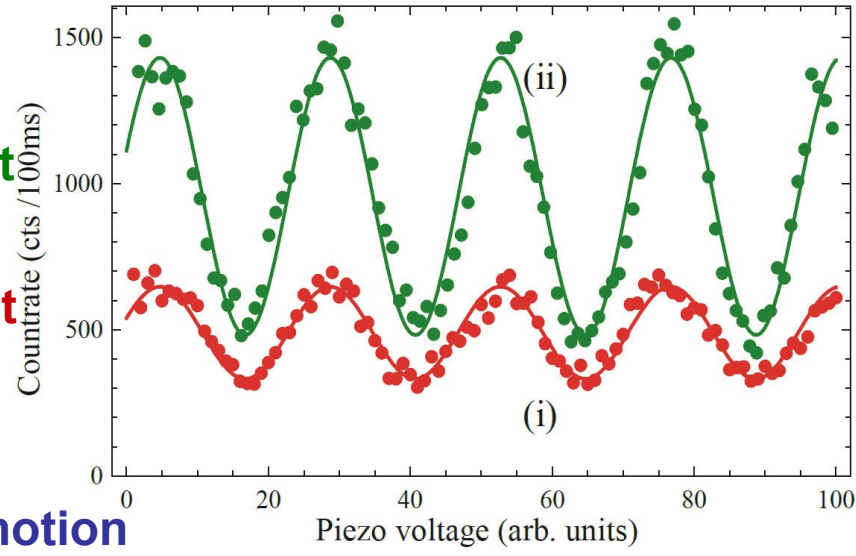
• **1st order coherence**

Interference visibility  $\sim e^{-2(k\sigma)^2}$

Mean atomic wavepacket extent

**Single ion**  
~ 60% contrast

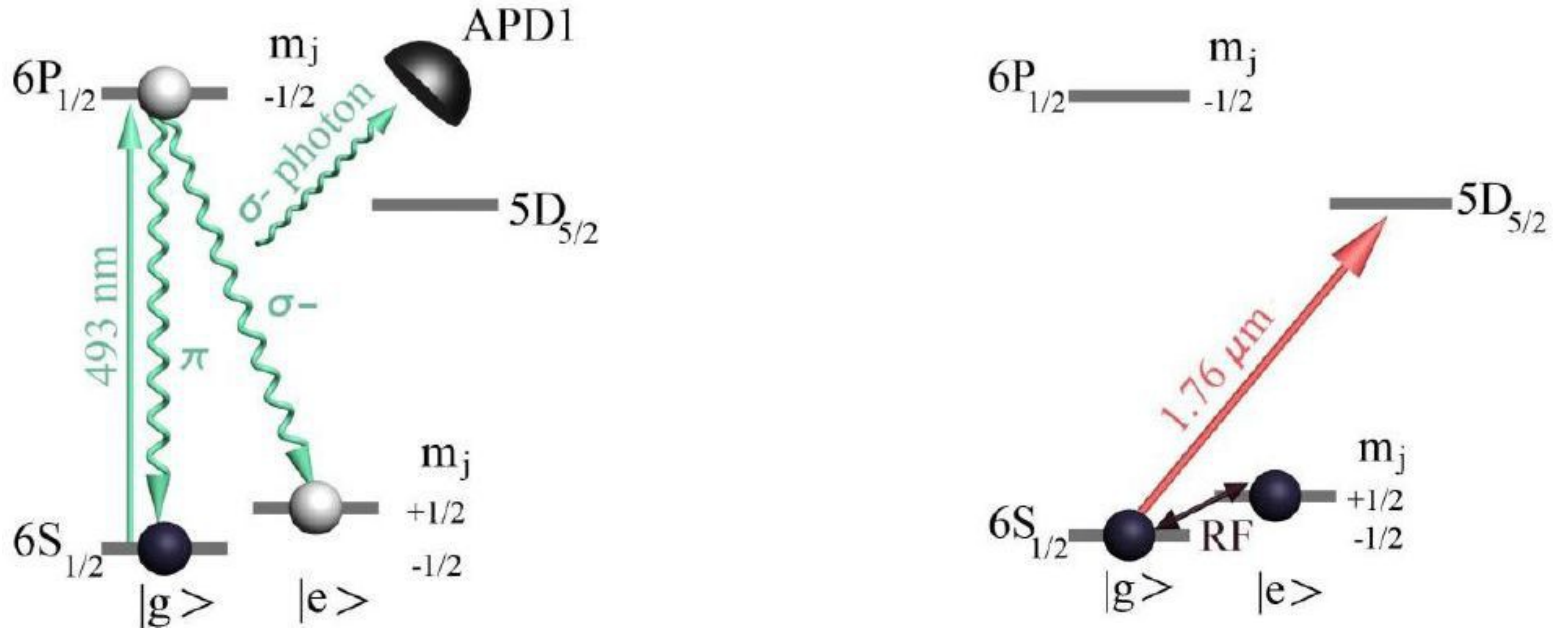
**Two ions**  
~ 35% contrast



**Main source of distinguishability ~ atomic motion**  
 → **excitation along the detection direction**

# Atom-atom entanglement

## Experimental sequence



### Entanglement generation

- Cooling and phase stabilization (4 ms)
- Optical pumping (5  $\mu$ s)
- Raman excitation (100 ns)
- Single photon detection

### State analysis

- RF q-bit rotations (6  $\mu$ s)
- Shelving to D state (2  $\mu$ s)
- Fluorescence detection (5 ms)

NO

? Photon detected ?

YES

$$F = \langle \Psi^+ | \rho | \Psi^+ \rangle = \frac{1}{2} \left[ \underbrace{\rho_{ge} + \rho_{eg}}_{\text{Populations}} + \underbrace{2\text{Re}(\rho_{eg,ge})}_{\text{Coherences}} \right]$$

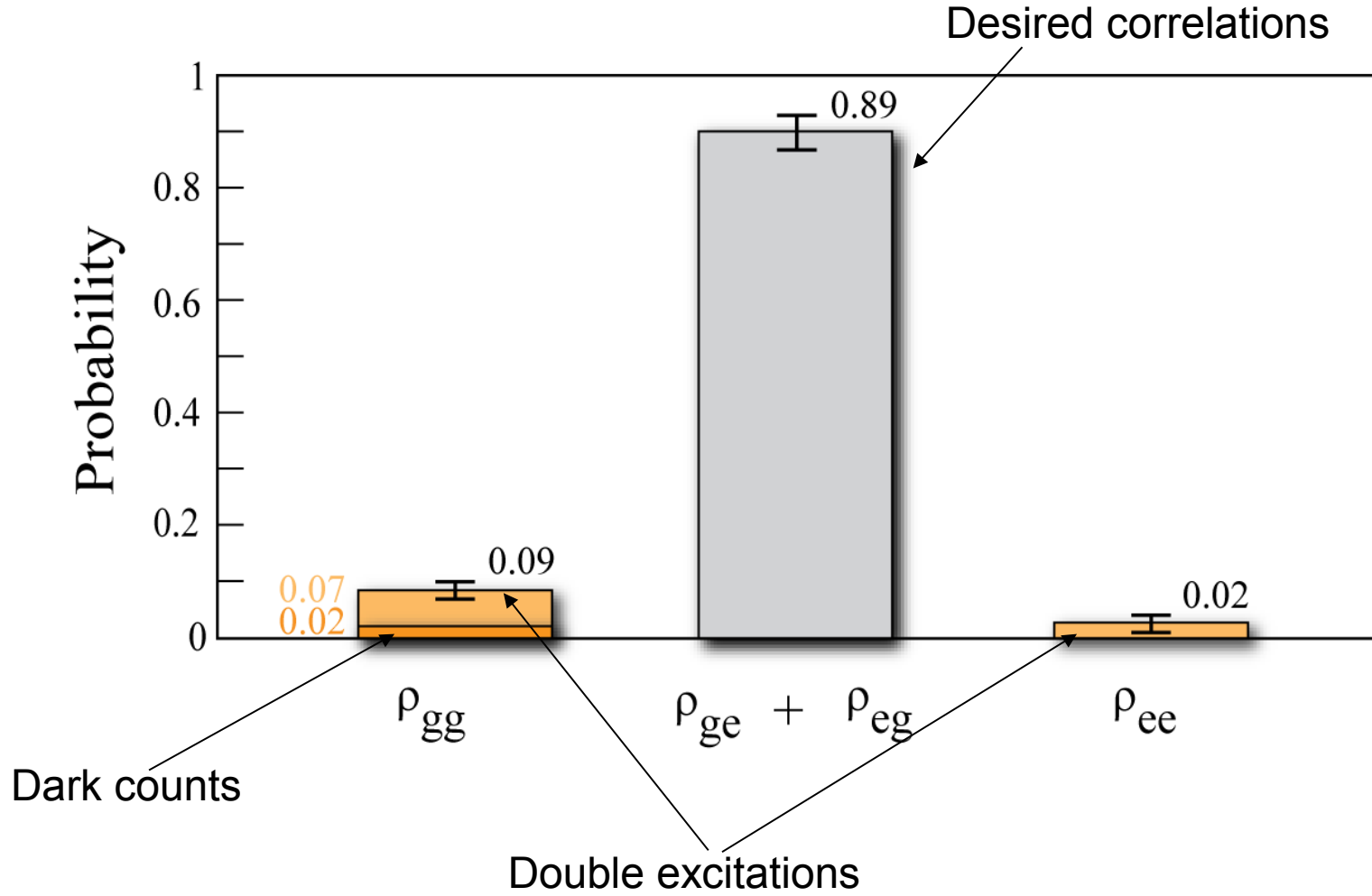
Measured directly (electron shelving)

Parity measurement

# Atom-atom entanglement

## Measurement results

### Populations - diagonal elements

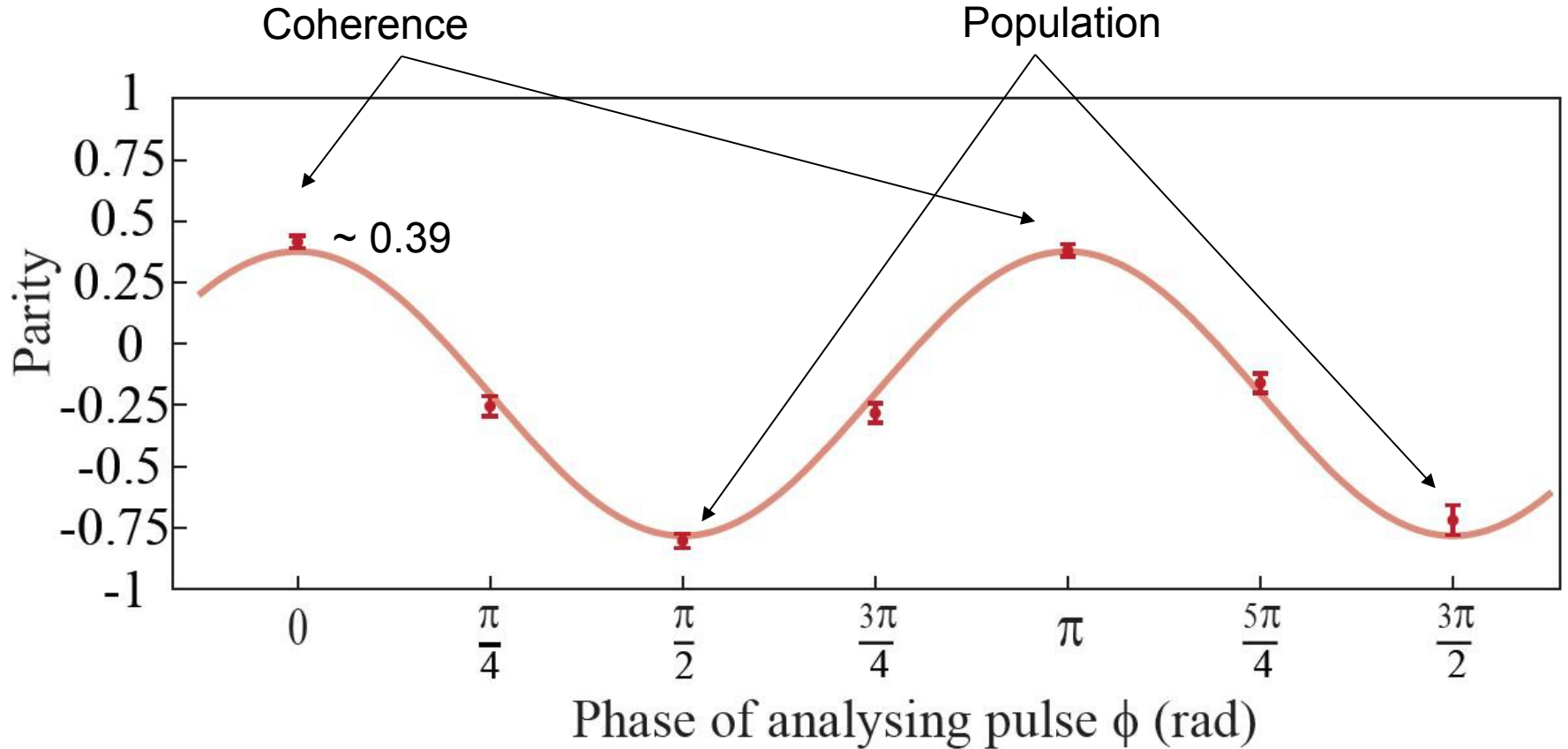


**In 89% of the cases correct correlation between atomic states**

# Atom-atom entanglement

## Measurement results

### Off diagonal elements - coherences



**Measured parity contrast  $\approx 58\%$**

Fidelity with  $|\Psi^+\rangle = 64 \pm 2\%$

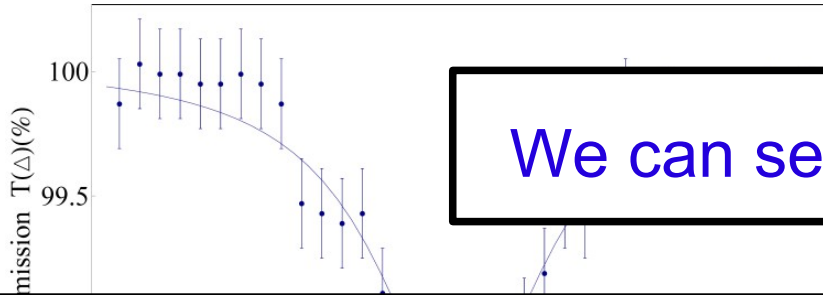
# Atom-atom entanglement

## Results

- **First demonstration** of the single-photon entanglement scheme with single atoms
- **Fidelity** with  $|\Psi^+\rangle = 64\%$ 
  - Limited by atomic recoils
  - Can be improved by excitation along the detection direction
- Entanglement **generation rate**:
  - 1 photon is easier to detect than 2!
  - With our experimental duty cycle  $\sim 14$  entanglement events/min
    - $\sim$  **Two orders of magnitude gain in  $P_{\text{succ}}$**



# Summary



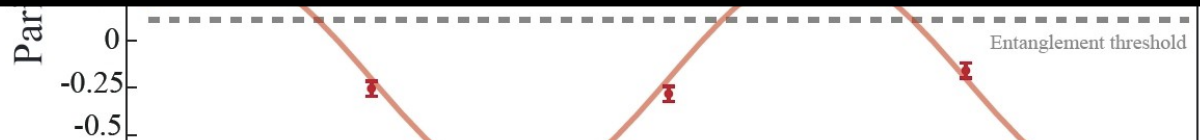
We can see the “shadow” of a single atom!

Other recent work:

**Shot-noise limited monitoring and phase locking of the motion of a single trapped ion**  
(Phys. Rev. Lett. 110, 133602 (2013))

**Single ion single photon source**

...



We can generate entanglement between two atoms  
by mere observation of single photon scattering!

# Our group

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***Innsbruck***



Nadia Röck

Gabriel Hétet

Miroslav Ježek

Michal Mičuda

Martina Miková

Ivo Straka

Miloslav Dušek

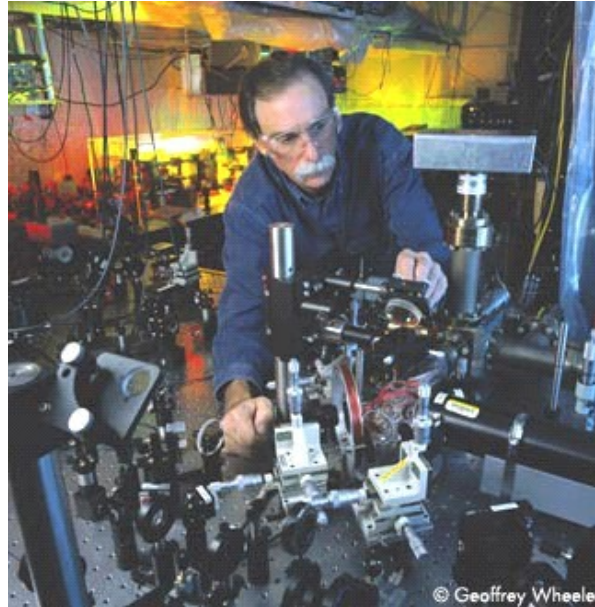
Radim Filip

***Olomouc***

Jaromír Fiurášek



## D. Wineland (NIST)



**“Ion trappers are encouraged because we can at least see a straightforward path to making a large processor, but the technical problems are extremely challenging. It might be fair to say that ion traps are currently in the lead; however, a good analogy might be that we’re leading in a marathon race, but only one metre from the start line.”**



# Atom-atom entanglement

## State analysis

- We aim to generate

$$|\Psi^+\rangle = \frac{1}{\sqrt{2}}(|eg\rangle + |ge\rangle)$$

All we need to measure!

- Any 2-qubit state

$$\hat{\rho} = \begin{pmatrix} \boxed{\rho_{gg}} & \rho_{gg,eg} & \rho_{gg,ge} & \rho_{gg,ee} \\ \rho_{gg,eg}^* & \boxed{\rho_{eg}} & \boxed{\rho_{eg,ge}} & \rho_{eg,ee} \\ \rho_{gg,ge}^* & \boxed{\rho_{eg,ge}^*} & \boxed{\rho_{ge}} & \rho_{ge,ee} \\ \rho_{gg,ee}^* & \rho_{eg,ee}^* & \rho_{ge,ee}^* & \boxed{\rho_{ee}} \end{pmatrix}$$

- Fidelity

$$F = \langle \Psi^+ | \rho | \Psi^+ \rangle = \frac{1}{2} \left[ \boxed{\rho_{ge} + \rho_{eg}} + \boxed{2\text{Re}(\rho_{eg,ge})} \right]$$

Populations
Coherences

- We measure:

**Populations** ~ directly (electron shelving)

**Coherences** ~ the value of parity operator for collective RF rotations  $R(\theta, \phi)$

$$\hat{P} = \hat{p}_{gg} + \hat{p}_{ee} - \hat{p}_{eg} - \hat{p}_{ge}$$

Amplitude of the pulse

Phase of the pulse

# Atom-atom entanglement

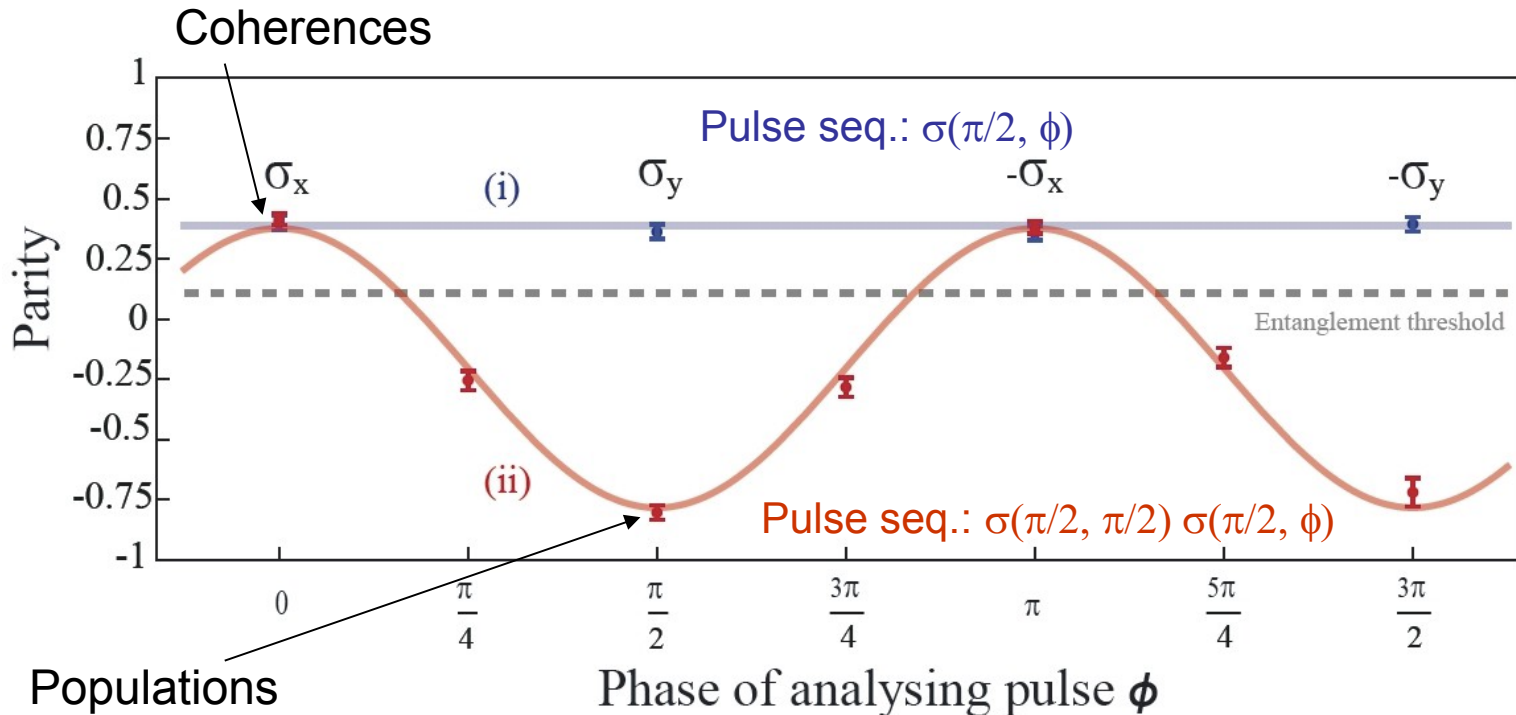
## Measurement results

### Off diagonal elements - coherences

- We first rotate the output so that

$$|\Psi^+\rangle = |\uparrow\downarrow\rangle + |\downarrow\uparrow\rangle \xrightarrow{R(\pi/2, \pi/2)} |\Phi\rangle = |\uparrow\uparrow\rangle - |\downarrow\downarrow\rangle$$

- Parity signal oscillates when applying  $R(\pi/2, \phi)$  rotation on this state

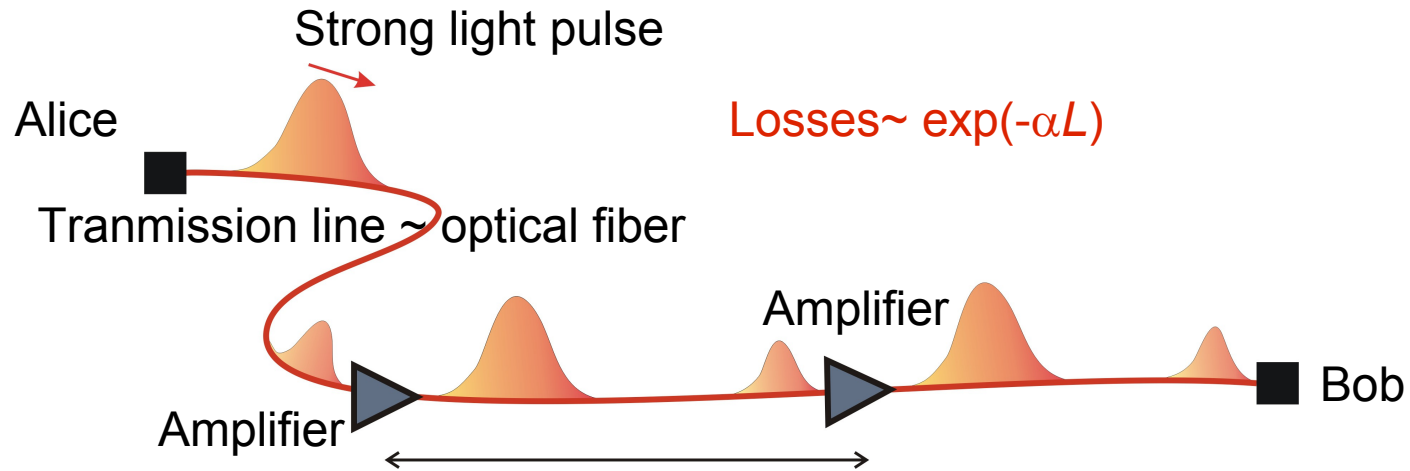


**Measured parity contrast  $\approx 58\%$**

# Atom-atom entanglement

## Motivation

### Classical communication

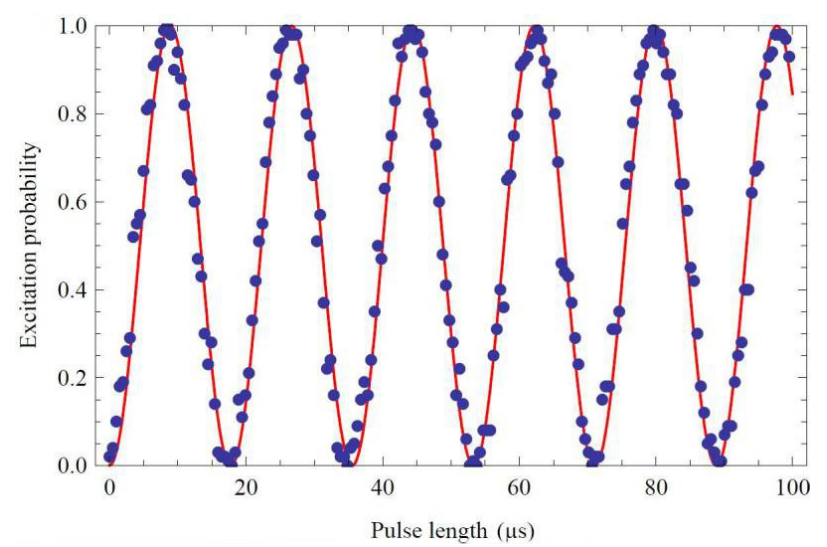
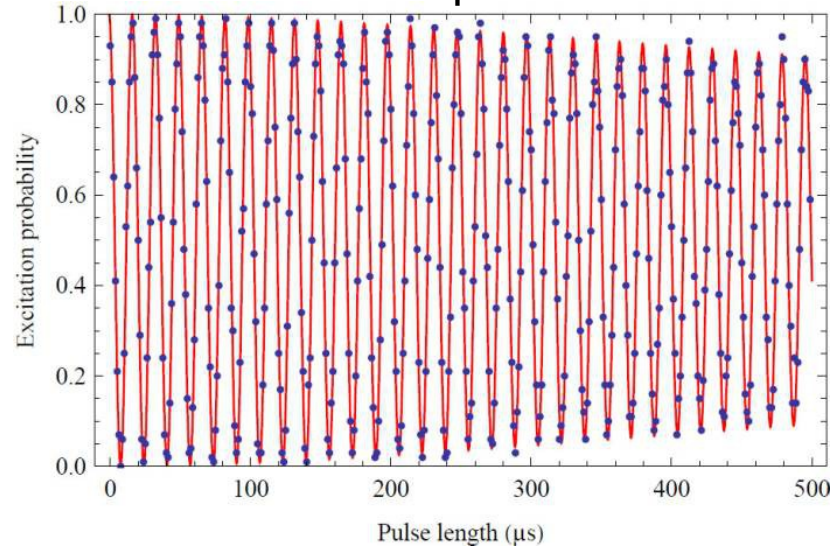
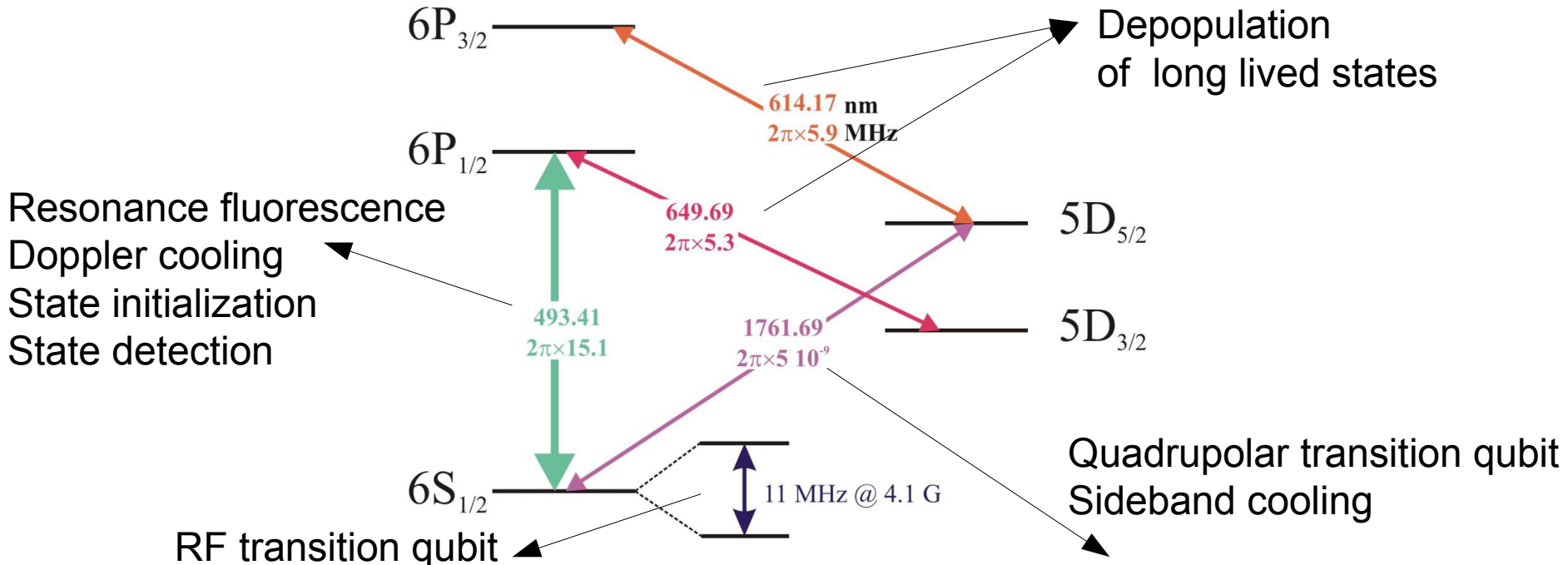


Works well, but quantum physics can offer us more!

- Absolutely secure communication (Quantum cryptography)
- Faithful transfer of unknown quantum state (Quantum teleportation)

# Overview

$^{138}\text{Ba}^+$

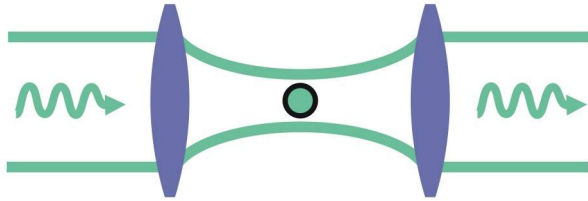




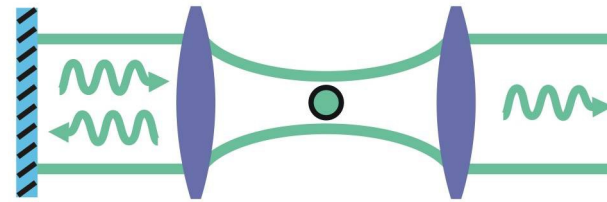
# Overview

## Single atom in free space

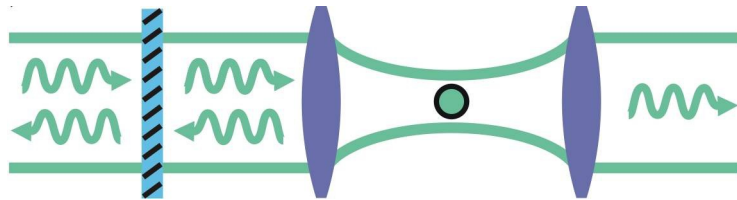
Free space extinction



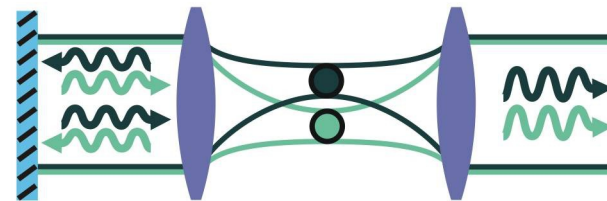
Half-cavity setup



Single-atom mirror



Atom-atom entanglement



Phase interference of scattered light!