# ROUGH SETS: FROM RUDIMENTS TO CHALLENGES

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## AGENDA

# RUDIMENTS OF ROUGH SETS

CHALLENGES FOR INTERACTIVE **COMPUTATIONAL SYSTEMS (ICS): GRANULARITY OF INFORMATION VAGUENESS** INTERACTIONS **ADAPTIVE JUDGMENT** HIERARCHICAL LEARNING **CONTROL & RISK MANAGEMENT IN ICS** LIST OF CHALLENGES

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## **RUDIMENTS OF ROUGH SETS**

Pawlak, Z.: Rough sets. International Journal of Computer and Information Sciences 11 (1982) Pawlak, Z.: Rough sets. Theoretical Aspects of Reasoning About Data. Kluwer (1991)



Now thousands of papers http://rsds.univ.rzeszow.pl/ <sup>3</sup>

# **VAGUENESS IN PHILOSOPHY**

Discussion on vague (imprecise) concepts includes the following :

- 1. The presence of borderline cases.
- 2. Boundary regions of vague concepts are not crisp.
- 3. Vague concepts are susceptible to sorites paradoxes.

Keefe, R. (2000) Theories of Vagueness. Cambridge Studies in Philosophy, Cambridge, UK)

# **RUDIMENTS OF ROUGH SETS**

- One of the main goals of the rough set analysis is construction of concept descriptions and induction of concept approximations.
- In particular, rough set theory constitutes a sound basis for KDD. It offers methods for:
  - discovering patterns hidden in data
  - for feature selection, feature extraction, data reduction, decision rule generation, pattern extraction (templates, association rules) etc.
  - extraction partial or total dependencies from data elimination of redundant data
  - dealing with null values, missing data
  - dealing with incremental data and others.

# **RUDIMENTS OF ROUGH SETS**

- Basic Concepts of Rough Sets
- Relationships with other approaches
- Rough Sets and Boolean Reasoning

# BASIC CONCEPTS OF ROUGH SETS

- Information/Decision Systems (Tables)
- Indiscernibility and Discernibility
- Set Approximation
- Reducts and Core
- Rough Membership
- Dependency of Attributes
- Decision Rules

# **INDISCERNIBILITY RELATIONS**



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## DISCERNIBILITY

# $xDIS_{IS}(B)y iff non(xIND_{IS}(B))y$

#### However, this is only the simplest case!



# LOWER AND UPPER APROXIMATION

#### $\underline{B}X = \bigcup \{Y \in U / B : Y \subseteq X\}$



 $BX = \bigcup \{Y \in U / B : Y \cap X \neq 0\}$ 

# PROPERTIES OF APPROXIMATIONS

 $\underline{B}(X) \subseteq X \subseteq \overline{B}X$   $\underline{B}(\phi) = \overline{B}(\phi) = \phi, \underline{B}(U) = \overline{B}(U) = U$   $\overline{B}(X \cup Y) = \overline{B}(X) \cup \overline{B}(Y)$   $\underline{B}(X \cap Y) = \underline{B}(X) \cap \underline{B}(Y)$   $X \subseteq Y \text{ implies } \underline{B}(X) \subseteq \underline{B}(Y) \text{ and } \overline{B}(X) \subseteq \overline{B}(Y)$ 

PROPERTIES **OF APPROXIMATIONS**  $B(X \cup Y) \supseteq B(X) \cup B(Y)$  $B(X \cap Y) \subseteq B(X) \cap B(Y)$ B(-X) = -B(X)B(-X) = -B(X)B(B(X)) = B(B(X)) = B(X)B(B(X)) = B(B(X)) = B(X)

where -X denotes U - X.

#### GENERALIZED APPROXIMATION SPACES

A. Skowron, J. Stepaniuk, Generalized Approximation Spaces 1994

$$\begin{split} AS &= (U, N, \nu) \\ N: U \to P(U) \quad \text{neighborhood function} \\ \nu: P(U) \times P(U) \to [0, 1] \quad \text{rough inclusion} \\ \quad \text{partial function} \end{split}$$

$$x \rightarrow Inf(x) \rightarrow N(x) = Inf^{-1}(Inf(x))$$
  
neighborhood of x

# **APPROXIMATION SPACE**

# $AS = (U, N, \nu)$

 $LOW(AS, X) = \{x \in U : v(N(x), X) = 1\}$ 

 $UPP(AS, X) = \{x \in U : v(N(x), X) > 0\}$ 

# **ROUGH MEREOLOGY**

MEREOLOGY St. LEŚNIEWSKI (1916) x is\_a\_ part\_of y **ROUGH MEREOLOGY** L. Polkowski and A. Skowron (1994-...) x is\_a\_ part\_of y in a degree

L. Polkowski, A. Skowron, Rough mereology, ISMIS'94, LNAI 869, Springer, 1994, 85-94

L. Polkowski, Reasonng by parts: An outline of rough mereology, Warszawa 2011

#### **EXTENSIONS OF APPROXIMATIONS**



# APPROXIMATION EXTENSIONS: CLASSIFIERS



# ACCURACY OF APPROXIMATION

 $\alpha_B(X) = \frac{|\underline{B}(X)|}{|\overline{B}(X)|}$ where |X| denotes the cardinality of  $X \neq 0$ . Obviously  $0 \le \alpha_B \le 1$ . If  $\alpha_B(X) = 1$ , X is crisp with respect to B. If  $\alpha_R(X) < 1$ , X is rough with respect to B. POSITIVE REGION OF DECISION SYSTEM T=(U,A,d)

For any C $\subseteq$ A we define the *C*-positive region of *d*:

$$POS_C(d) = \bigcup_{X \in U/d} CX$$

Remark: Analogously one can define *C*-positive region of *D* if we have a set *D* of decisions instead of one decision.

# POSITIVE REGION OF DECISION SYSTEM T=(U,A,d)

#### Decision classes:

 $U/d = \{X_1, X_2, X_3\}$ 



### **ROUGH MEMBERSHIP**

• The rough membership function quantifies the degree of relative overlap between the set X and the equivalence class  $[x]_{B}$  to which x belongs.

$$\mu_X^B: U \to [0,1]$$
  $\mu_X^B(x) = \frac{|[x]_B \cap X|}{|[x]_B|}$ 

• The rough membership function can be interpreted as a frequency-based estimate of  $P(x \in X | u)$ , where  $u=[x]_B$  is the equivalence relation of IND(B).

$$[x]_B \longrightarrow U$$

### **DEPENDENCY OF ATTRIBUTES**

Let *D* and *C* be subsets of *A*. *D* depends on *C* in a degree k ( $0 \le k \le 1$ ),

$$C \Rightarrow_k D$$
,

where

$$k = \gamma(C, D) = \frac{|POS_C(D)|}{|U|}$$

#### **DESCISION RULES**

T = (U, A, d) - decision systemDecision rule  $a_{i_1} = v_{i_1} \wedge ... \wedge a_{i_k} = v_{i_k} \Longrightarrow d = v \in V_d$ Generalized decision rule

Generalized decision rule  $a_{i_1} = v_{i_1} \wedge ... \wedge a_{i_k} = v_{i_k} \Longrightarrow \partial_A = V \subseteq V_d$ 

### MINIMAL SETS OF CONDITION ATTRIBUTES PRESERVING DISCERNIBILITY CONSTRAINTS: REDUCTS

- between discernible objects in a given information system → reducts in information systems
- between objects from different decision classes → decision reducts
- between a given object x with a decision *i* and other objects with a decision different from *i* Jocal reducts relative to the object x

#### REDUCTS IN INFORMATION SYSTEMS

 For a given information system IS=(U, A) we are searching for minimal subsets B\_A such that

$$IND_{IS}(B) = IND_{IS}(A)$$

- *RED(IS)* or *RED(A)* the set of all reducts in *IS*.
- CORE(IS)=/ RED(IS).

## **PROBLEMS WITH REDUCTS**

- The number of reducts can be large, e.g., in case if reducts of information systems some information systems can have exponential number of reducts with respect to the number of attributes
- Problems of computing minimal reducts are of high complexity, usually they are NP-hard.

Fortunately there have been developed efficient heuristics for computing relevant reducts or sets of reducts based on BOOLEAN REASONING.

### RELATIONSHIPS WITH OTHER APPROACHES

- Fuzzy sets
- Dempster-Shafer Theory
- Boolean Reasoning
- Statistics
- Mereology
- Mathematical Morphology

RELATIONSHIPS OF ROUGH SETS WITH BOOLEAN REASONING



# **BOOLEAN REASONING**

- Rough Sets and Boolean Reasoning
  - Reducts in information systems
  - Decision reducts
  - Local reducts relative to objects
  - Discretization
  - Symbolic value grouping
  - Approximate reducts and association rules

# **BOOLEAN REASONING**

DISCERNIBILITY CONSTRAINTS TO BE PRESERVED CAN BE ENCODED BY MEANS OF BOOLEAN FUNCTIONS RELEVANT FOR BOOLEAN REASONING

# BOOLEAN REASONING FOR COMPUTING REDUCTS IN INFORMATION SYSTEMS



# **REDUCTS IN /S**



# **CHALLENGES**

#### for making progress in constructing of the high quality intelligent systems


### AGENDA

- MOTIVATION
- ► INTERACTIVE ROUGH GRANULAR COMPUTING
  - CONTRUCTION OF GRANULES
    - ♦ HIERARCHICAL LEARNING AND ONTOLOGY APPROXIMATION
      - ♦ ROLE OF DOMAIN KNOWLEDGE
      - CASE STUDIES
  - INTERACTIVE COMPUTATIONS AND DECISION SUPPORT IN PROBLEM SOLVING
    - CONTROL
      - ADAPPTIVE JUDGMENT
        - REASONING ABOUT CHANGES ROUGH CALCULUS
      - BEYOND ONTOLOGIES: EVOLVING COMMUNICATION LANGUAGES
      - RISK MANAGEMENT IN INTERACTIVE COMPUTATIONAL SYSTEMS

CASE STUDY: ALGORITHMIC TRADING

CHALLENGES

# MOTIVATION

- Making progress in constructing of the high quality intelligent systems
- Examples: approximation of complex vague concepts such as guards of actions or behavioral patterns
- Reasoning about vague concepts



UAV



**OBSTACLE AVOIDANCE** 





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### **REAL-LIFE PROJECTS**

- UAV control of unmaned helicopter (Wallenberg Foundation, Linkoeping University)
- **Medical decision support (glaucoma attacs, respiratory failure,...)**
- Fraud detection (Bank of America)
- Logistics (Ford GM)
- **Dialog Based Search Engine (UNCC, Excavio)**
- **Algorithmic trading (Adgam)**
- Semantic Search (SYNAT) (NCBiR)
- Firefighter Safty (NCBiR)

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Editors Witold Pedrycz | Andrzej Skowron | Vladik Kreinovich

#### Handbook of Granular Computing



Plays a key role in implementation of the strategy of divide-andconquer in human problem-solving – Lotfi Zadeh

Zadeh, L. A. (1979) Fuzzy sets and information granularity. In: Gupta, M., Ragade, R., Yager, R. (eds.), Advances in Fuzzy Set Theory and Applications, Amsterdam: North-Holland Publishing Co., 3-18

Zadeh, L.A. (2001) A new direction in Al-toward a computational theory of perceptions. Al Magazine 22(1): 73-84

#### **LESLIE VALIANT: TURING AWARD 2010**

March 10, 2011:

Leslie Valiant, of Harvard University, has been named the winner of the 2010 Turing Award for his efforts to develop computational learning theory. http://www.techeye.net/software/leslie-valiant-gets-turing-award#ixzz1HVBeZWQL Current research of Professor Valiant http://people.seas.harvard.edu/~valiant/researchinterests.htm A fundamental question for artificial intelligence is to characterize the **computational building blocks that are** necessary for cognition.

**INFORMATION GRANULES** 

#### **INDISCERNIBILITY GRANULES**



## ELEMENTARY GRANULES + INTERACTIVE CALCULULI OF GRANULES









### **JOIN WITH CONSTRAINTS**



Objects (granules) in *IS* are composed out of attribute value vectors from  $IS_1...IS_k$  satisfying  $W_{45}$ 

### INTERACTIVE HIERARCHICAL STRUCTURES



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### **STRUCTURAL OBJECTS**

### SEARCHING FOR RELEVANT FEATURES

### GENERALIZATIONS OF GRANULES: TOLERANCE GRANULES

invariants over tolerance classes; compare invariants in the Gibson approach



#### **GRANULES REPRESENTING STRUCTURES OF OBJECTS**



### **COMPLEX ATTRIBUTES**



## STRUCTURAL GRANULES **SEARCHING FOR RELEVANT** FEATURES



### **DEFINABLE GRANULES**

### **ROUGH GRANULES**

### APPROXIMATION OF GRANULES

### **INTERACTIONS**

### INTERACTIONS

[...] interaction is a critical issue in the understanding of complex systems of any sorts: as such, it has emerged in several wellestablished scientific areas other than computer science, like biology, physics, social and organizational sciences.

Andrea Omicini, Alessandro Ricci, and Mirko Viroli, The Multidisciplinary Patterns of Interaction from Sciences to Computer Science. In: D. Goldin, S. Smolka, P. Wagner (eds.): Interactive computation: The new paradigm, Springer 2006

### INTERACTIONS

[...] One of the fascinating goals of natural computing is to understand, in terms of information processing, the functioning of a living cell. An important step in this direction is understanding of interactions between biochemical reactions.... the functioning of a living cell is determined by interactions of a huge number of biochemical reactions that take place in living cells.



A human dendritic cell (blue pseudocolor) in close interaction with a lymphocyte (yellow pseudo-color). This contact may lead to the creation of an immunological synapse.

The Immune Synapse by Olivier Schwartz and the Electron Microscopy Core Facility, Institut Pasteur <u>http://www.cell.com/Cell\_Picture\_Show</u>

Andrzej Ehrenfeucht, Grzegorz Rozenberg: Reaction Systems: A Model of Computation Inspired by Biochemistry, LNCS 6224, 1–3, 2010

#### **GENERAL SCHEME OF INTERACTION**



# HIERARCHICAL LEARNING IN INTERACTION WITH DOMAIN EXPERTS

### ROUGH SET BASED ONTOLOGY APPROXIMATION



#### UAV





### **SUNSPOT CLASSIFICATION**



T.T. Nguyen, C.P. Willis, D.J. Paddon, S.H. Nguyen, H.S. Nguyen: Learning Sunspot Classification. Fundamenta Informaticae 72(1-3): 295-309 (2006)

#### HARD SAMPLES



Nguyen, T.T., Skowron, A.: Rough-granular computing in human-centric information processing. In; Bargiela, A., Pedrycz, W. (eds.), Human-Centric Information Processing Through Granular Modelling, Springer, Heidelberg (2009) 1-30

### MEDICAL DIAGNOSIS AND THERAPY SUPPORT RESPIRATORY FAILURE



Jan Bazan et al, Cooperation with Polish-American Pediatric Institute, Jagiellonian University Medical College, Cracow, Poland

#### **SCALABILITY**



### **ADAPTIVE JUDGMENT**

#### **LESLIE VALIANT: TURING AWARD 2010**

A specific challenge is to build on the success of machine learning so as to cover broader issues in intelligence.

This requires, in particular a reconciliation between two contradictory characteristics -- the apparent logical nature of reasoning and the statistical nature of learning.

Professor Valiant has developed a formal system, called robust logics, that aims to achieve such a reconciliation.

### INTERACTIVE HIERARCHICAL STRUCTURES



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#### **ADAPTIVE JUDGMENT**

- Searching for relevant approximation spaces
  - new features, feature selection
  - rule induction
  - measures of inclusion
  - strategies for conflict resolution
- Adaptation of measures based on the minimal description length: quality of approximation vs description length
- Reasoning about changes
- Perception (action and sensory) attributes selection
- Adaptation of quality measures over computations relative to agents
- Adaptation of object structures
- Strategies for knowledge representation and interaction with knowledge bases
- Ontology acquisition and approximation
- Language for cooperation development and evolution
- •

### REASONING ABOUT CHANGES

### **ROUGH CALCULUS**

#### PROCESS MODELS AND INTERACTIONS Example

$$\begin{aligned} x_i(t+1) &= f(x_i(t)) + \kappa \frac{1}{d_i} \sum_{j: j \approx i} (f(x_j(t-\tau)) - f(x_i(t))) \\ & \text{neighborhood relation} \\ \mathbf{x}_i(t) &= f(x_i(t)) + \varkappa \frac{1}{d_i} \sum_{j: j \approx i} (f(x_j(t-\tau)) - f(x_i(t))) \end{aligned}$$

Feng, J., Jost, J., Minping, Q. (eds): Network: From Biology to Theory, Springer, Berlin, 2007

$$\frac{ds}{dt} = G(t, s(t), e(t))$$

$$\frac{de}{dt} = H(t, s(t), e(t))$$
?

#### **FUNCTION APPROXIMATION**

Skowron, A., Stepaniuk, J., Swiniarski, R.: Approximation spaces in roughgranular computing. Fundamenta Informaticae 100 (1-4) (2010) 141-157



### EXAMPLE: TRAJECTORY APPROXIMATION

# Adaptation must be used to fix the deviation of the model


# BEYOND ONTOLOGIES EVOLVING COMMUNICATION LANGUAGE

## FROM INFORMATION RETRIEVAL TO DECISION SUPPORT



SYNAT project H.S.Nguyen et al

## BIOLOGY

[...] Tomorrow, I believe, every biologist will use computer to define their research strategy and specific aims, manage their experiments, collect their results, interpret their data, incorporate the findings of others, disseminate their observations, and extend their experimental observations - through exploratory discovery and modeling - in directions completely unanticipated

Bower, J.M., Bolouri, H. (Eds.): Computational Modeling of Genetic and Biochemical Networks. MIT Press, Cambridge, MA (2001)

## **GOTTFRIED WILHELM LEIBNIZ**

[...] If controversies were to arise, there would be no more need of disputation between two philosophers than between two accountants. For it would suffice to take their pencils in their hands, and say to each other: *Let us calculate*.

[...] Languages are the best mirror of the human mind, and that a precise analysis of the signification of words would tell us more than anything else about the operations of the understanding.

Leibniz, G.W. : Dissertio de Arte Combinatoria (1666). Leibniz, G.W.: New Essays on Human Understanding (1705), (translated by Alfred Gideon Langley, 1896), (Peter Remnant and Jonathan Bennett (eds.)). Cambridge University Press (1982).

#### **JUDEA PEARL- TURING AWARD 2011**

for fundamental contributions to artificial intelligence through the development of a calculus for probabilistic and causal reasoning.

- Traditional statistics is strong in devising ways of describing data and inferring distributional parameters from sample.
- Causal inference requires two additional ingredients:
  - a science-friendly language for articulating causal knowledge,

and

- a mathematical machinery for processing that knowledge, combining it with data and drawing new causal conclusions about a phenomenon.

Judea Pearl: Causal inference in statistics: An overview. Statistics Surveys 3, 96-146 (2009)

## COMPUTING WITH WORDS LOTFI A. ZADEH

[...] Manipulation of perceptions plays a key role in human recognition, decision and execution processes. As a methodology, computing with words provides a foundation for a computational theory of perceptions - a theory which may have an important bearing on how humans make - and machines might make – perception - based rational decisions in an environment of imprecision, uncertainty and partial truth.

[...] computing with words, or CW for short, is a methodology in which the objects of computation are words and propositions drawn from a natural language.

Lotfi A. Zadeh1: From computing with numbers to computing with words – From manipulation of measurements to manipulation of perceptions. IEEE Transactions on Circuits and Systems 45(1), 105–119 (1999) <sup>78</sup>

## INTERACTIVE COMPUTATIONAL SYSTEMS (ICS)

## EXAMPLES OF COMPLEX SYSTEMS

SOFTWARE PROJECTS MEDICAL SYSTEMS ALGORITHMIC TRADING SYSTEMS INTEGRATING TEAMS OF ROBOTS AND HUMANS TRAFFIC CONTROL SYSTEMS SYSTEMS IN ACTIVE MEDIA TECHNOLOGY PERCEPTION BASED SYSTEMS

## **CURRENT PROJECTS**



- 'Interdisciplinary System for Interactive Scientific and Scientific-Technical Information' (<u>www.synat.pl</u>).
- Our task:
  - SONCA an application based on a hybrid database framework, wherein scientific articles are stored and processed in various forms.
  - Semantic indexing, classification, grouping and
  - Semantic information retrieval
- Aug. 2010 -> Aug. 2013 -> Apr. 2014

#### • Firefighter safety

- The project aims to improve the safety of firefighters during rescue fire fighting operations, and minimalization of the effects of fire.
- The task is to create a computer system that improves the quality of
  - information flow,
  - decision-making operations
  - and the time of the rescue and fire fighting.
- From June 2013 to June 2016

## PERCEPTION BASED COMPUTING

The main idea of this book is that perceiving is a way of acting. It is something we do. Think of a blind person tap-tapping his or her way around a cluttered space, perceiving that space by touch, not all at once, but through time, by skillful probing and movement. This is or ought to be, our paradigm of what perceiving is.

Alva Noë: Action in Perception, MIT Press 2004

<u>interaction</u>: agent  $\rightarrow$  sensory and action attributes - only activated by agent attributes A(t) at time t are performing measurements and actions

history of sensory measurements and selected lower level actions over a period of time

	-			
	time	a <sub>1</sub>	 ac <sub>1</sub>	
<b>x</b> <sub>1</sub>	1			
<b>x</b> <sub>2</sub>	2			

	features of histories	higher level action

## DISCOVERY OF COMPLEX GAMES OF INTERACTIONS



complex vague concepts initiating actions

## THE WITTGENSTEIN IDEA ON LANGUAGE GAMES

Wittgenstein, L.: Philosophical Investigations. (1953) (translated by G. E. M. Anscombe) (3rd Ed), Blackwell Oxford1967

#### Granules

#### information granules (infogranules)

physical granules (hunks)

#### STATES IN INTERACTIVE COMPUTATIONAL MODELS





possible cases of interpretation (implementation) of interactive computations specified by abstract semantics which could be exressed by algorithms (procedures) for performing computations by control using hunks and other infogranules; computations are influenced by interactions among different hunks (e.g., during sensory measurements, performing actions, realisation of procedures in computers); possible cases of interpretation are often defined relative to different universes of infogranules and hunks

### **SENSORS**



## ACTION



## ACTION



## **CONFIGURATION**



#### **TRANSITION RELATION**

agent configuration at time t (with a predicted granule structure at the time unit next to t) agent configuration at the time unit next to *t* (not necessarily satisfying the predicted results): the result of interactions caused by undertaken actions and unpredicted interactions with the environment

(parallel) realization by the agent of selected actions, sensory measurements, new information granule construction/destruction, etc. **Aristotle** has dedicated many papers to clarify the relationships between concepts such as thinking, imagination, judgment, perception and psyche issue:

Thinking is different from perceiving and is held to be in part imagination, in part judgment: we must therefore first mark off the sphere of imagination and then speak of judgment.





## INTERACTIVE INFORMATION AND DECISION SYSTEMS



links to parts of a structure of hunks in global states defined by the agent control system at time t = t < t

system at time  $t_1, \dots, t_k \le t$ 

using the agent knowledge bases and, in particular, parameters of the (actual at time  $t_1, ..., t_k$ ) agent mereology, relations on values of control parameters at time t and/or values of conditional attributes at time t;

the structure of hunks in global states is defined by agent control using some constraints over values of conditional attributes and/or control parameters

## **INTERACTIVE INFORMATION AND**

structured objects ↓			decisions
structure over values of conditional attributes and values of control parameters at time ≤ t fixed by the agent control	values of control parameters at some moments of time ≤ <i>t</i>	values of new conditional attributes over structured objects at some moments of time $\leq t$	values of control parameters at time <i>t + 1</i>

#### row of decision system

links to parts of a structure of hunks in global states defined by the agent control system at at some moments of time  $\leq t$ 

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using the agent knowledge bases and, in particular, parameters of the (actual at at some moments of time  $\leq t$ ) agent mereology, relations on values of control parameters at time t and/or values of conditional attributes at time t; the structure of hunks in global states is defined by agent control using some constraints over values of conditional attributes and/or control parameters

### HOW TO CONTROL COMPUTATIONS IN ICS ? \*\*\*

## **RISK MANAGEMENT IN ICS**

Jankowski, A., Skowron, A., Wasilewski, P.: Interactive Computational Systems. CS&P 2012 Jankowski, A., Skowron, A., Wasilewski, P.: Risk Management and Interactive Computational Systems. Journal of Advanced Mathematics and Mathematics 2012 99

- Threat
  - A potential occurrence that can have an undesirable effect on the system assets of resources
  - Results in breaches in confidentiality, integrity, or a denial of service, e.g., outsider penetrating a system is an outsider threat
  - Need to identify all possible threats and address them to generate security objectives
- Vulnerability
  - A weakness that makes it possible for a threat to occur

'vulnerability' refers to **the capacity to be wounded**, **i.e.**, **the degree to which a system is likely to experience harm due to exposure to a hazard** Turner II, B.L., Kasperson, R.E., Matson, P.A., McCarthy, J.J., Corell, R.W., Christensen, L., Eckley, N., Kasperson, J.X., Luers, A., Martello, M.L., Polsky, C., Pulsipher, A., Schiller, A., 2003. A framework for vulnerability analysis in sustainability science. Proceedings of the National Academy of Sciences of the United States of America 100, 8074–8079. (Turner II et al., 2003)











#### **Threats**

#### **Vulnerabilities**

#### **Security**

#### target

expressed by a value hierarchy of needs and assets



#### vulnerabilities used by threats



#### vulnerabilities used by threats

## EXAMPLE OF A PROBABILITY CRITERIA MATRIX

	E	IV	III	II	I	I	I
Likelihood rating	D	IV	III	III	II	I	I
	С	V	IV	III	II	II	I
	В	v	IV	III	Ш	II	I
	A	v	v	IV	ш	II	II
		1	2	3	4	5	6
		Consequence rating					

#### **RISK MANAGEMENT PROCESS**



## EXAMPLE OF BOW TIE DIAGRAM FOR UNWANTED CONSEQUENCES

Sources of risk


# **ALGORITHMIC TRADING**

# THE CONCEPT OF TRADING ROBOTS



The <u>trading robots</u> system, is the use of electronic financial markets platforms for entering trading orders with an algorithm deciding on basic aspects of the order such as the asset, timing, price, or quantity of the order, or in many cases initiating the order without human intervention. The concept of such type of use of software is also known as <u>robo trading</u> or <u>algorithmic trading</u> or <u>automated trading</u>, also <u>algo</u> trading, <u>black-box trading</u>

Based on definition from: <u>http://en.wikipedia.org/wiki/Algorithmic\_trading</u>

**PEARL'S POSTULATE:** a science-friendly language for articulating causal knowledge about market crash & a mathematical machinery for processing that knowledge combining it with data and drawing new causal conclusions



## THE ESSENCE OF ADGAM GROUP TECHNOLGICAL SOLUTIONS FOR ALGORITHMIC TRADING



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## THE ESSENCE OF ADGAM GROUP TECHNOLGICAL SOLUTIONS FOR ALGORITHMIC TRADING



## ADGAM GROUP EFFORTS ON THE DEVOLOPMENT OF ALGORITHMIC TRADING TECHNOLOGY

Project duration [years]	5
man – months	1 000
mathematical models implemented	100
experiments tested on many years historical data and many thousands of years of Monte Carlo generated data	1000
lines of code	300 000

### **REAL-MONEY Account Live Trading by rescaled** AdgaM TRADING ROBOTS & WALLSTREET FOREX ROBOT





The essence of algorithmic trading based on AdgaM Group experience

### The essence of algorithmic trading

#### Causal inference supporting market crash forecast is not easy task



Years from Peak posted on http://calculatedrisk.blogspot.com/

"Those of us who have looked to the self-interest of lending institutions to protect shareholders' equity, myself included, are in a state of shocked disbelief....

# The whole intellectual edifice

[of risk-management in

financial markets]....

<u>collapsed last summer."</u>

Alan Greenspan former Fed chairman at a congressional hearing in October 2008.

### THE ESSENCE OF ALGORITHMIC TRADING

#### Causal inference supporting market crash forecast is not easy task



Traditional statistics is strong in devising ways of describing data and <u>inferring distributional</u> parameters from sample. Causal inference requires two additional ingredients:

1. a science-friendly language for articulating causal knowledge about market crash

&

2. a mathematical machinery for processing that knowledge,

combining it with data and drawing new causal conclusions

about a phenomenon.

# **CHALLENGES SUMMARY**

### ♦ RS & INTRACTIVE COMPUTATIONS

- MODELING OF INTERACTIVE COMPUTATIONS
  - GENERALIZED INFORMATION SYSTEMS
    - INTERACTIVE INFORMATION SYSTEMS
    - HIERARCHIES AND NETWORKS OF INFORMATION SYSTEMS
    - CONTEXT DEPENDENT INFORMATION SYSTEMS
    - DYNAMICAL NETWORKS OF INFORMATION SYSTEMS
- CONTROL OF INTERACTIVE COMPUTATIONS

### RS & ADAPTIVE JUDGMENT

- LEARNING HIERARCHIES OF INFORMATIOIN SYSTEMS
- LERNING HIERARCHIES OF SATISFIABILITY RELATIONS
- NEW FEATURE DISCOVERY
- REASONING ABOUT CHANGES
  - ROUGH CALCULUS
  - ◆ STRATEGIES FOR ADAPTATION OF APPROXIMATION SPACES
- CONTEXT DISCOVERY

### • RS & EVOLUTION OF COMMUNICATION LANGUAGE

- LEARNING NEW FEATURES, PHRASES, SENTENCES, SITUATION DESCRIPTION
- LEARNING SCHEMES OF REASONING AND COMPOSITIONS OF RULES
- LEARNING INCLUSION RELATION IN INTERACTION WITH USERS (EXPERTS)
- LEARNING OF COALITIONS AND ORGANIZATIONS
- AUTONOMIC LEARNING, SELF ORGANIZATION
- RISK MANAGEMENT IN INTERACTIVE COMPUTATIONAL SYSTEMS

### • RS & SCALABILITY

- PARALLEL ALGORITHMS
- EMBEDDED HARDWARE
- CLOUD COMPUTING

## WISDOM TECHNOLOGY (WisTech)

A. Jankowski, A. Skowron: A wistech paradigm for intelligent systems, Transactions on Rough Sets VI: LNCS Journal Subline, LNCS 4374, 2007, 94–132
A. Jankowski A., Skowron A.: Logic for artificial intelligence: The Rasiowa-Pawlak school perspective, In: Ehrenfeucht, A., Marek V., Srebrny M. (Eds.) Andrzej Mostowski and Foundational Studies, IOS Press, Amsterdam, 2008, 106-143.

# WISDOM= INTERACTIONS + ADAPTIVE JUDGMENT + KNOWLEDGE BASES



IRGC = systems based on interactive computations on granules with use of domain (expert) knowledge, process mining and concept learning 121



# **THANK YOU !**

**APPENDIX** 

# **REFERENCES AND FURTHER READINGS**

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