



Palacký University
Olomouc

Quantum operations with light

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University of Tokyo
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Laboratoire Kastler Brossel, Sorbone, Paris
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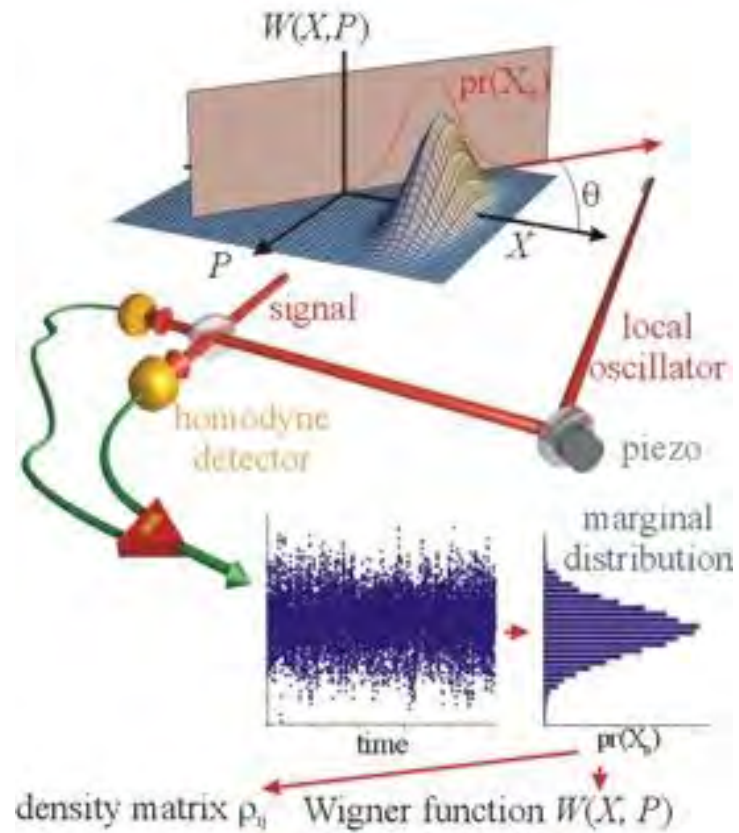
SHORT OVERVIEW OF CV QUANTUM OPERATIONS WITH LIGHT



- **Quantum communication:**
quantum distillation and noiseless amplification by weak measurement
coherent quantum error-correction
entanglement-based quantum key distribution
- **Quantum amplifiers and interfaces:**
universal squeezer and its applications
effective manipulation with non-Gaussian states
amplification of optomechanical coupling
- **Quantum nonlinear dynamics:**
deterministic cubic quantum operation
simulations of quantum nonlinearity
noise-enhanced quantum effects



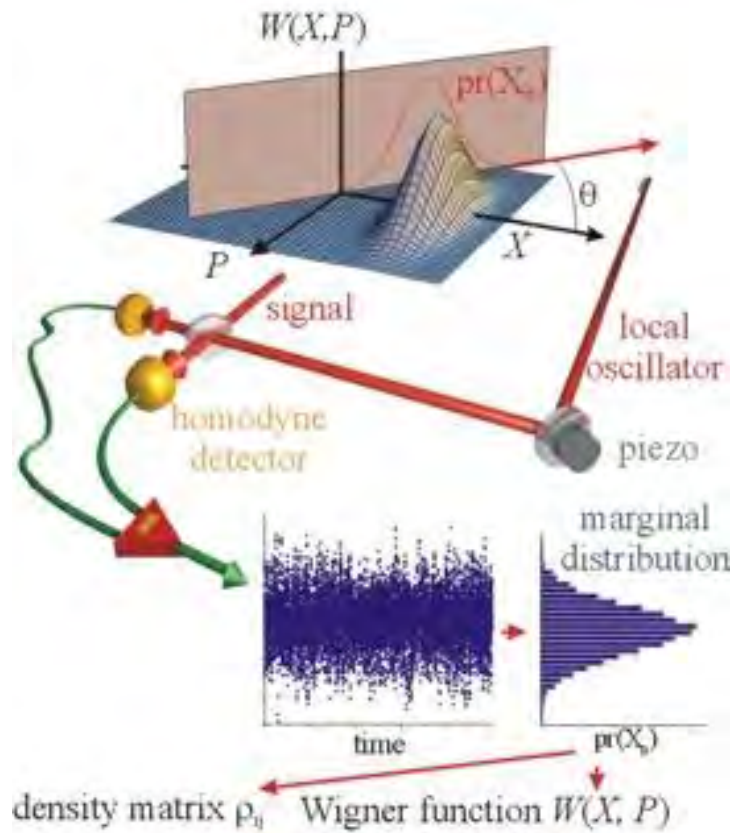
INTRO: CV QUANTUM NOISE



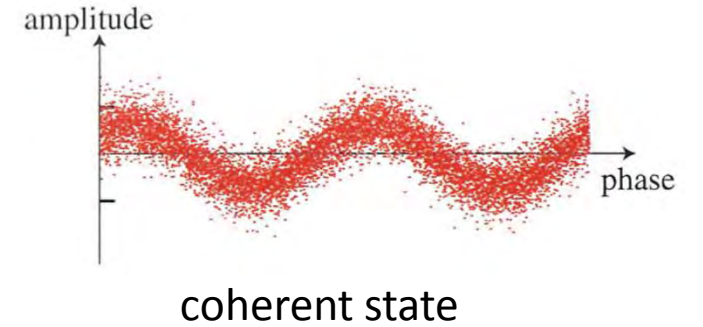
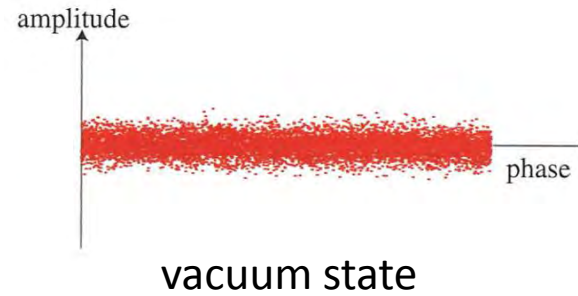
Homodyne detection
(from A. Lvovsky's web)



INTRO: CV QUANTUM NOISE



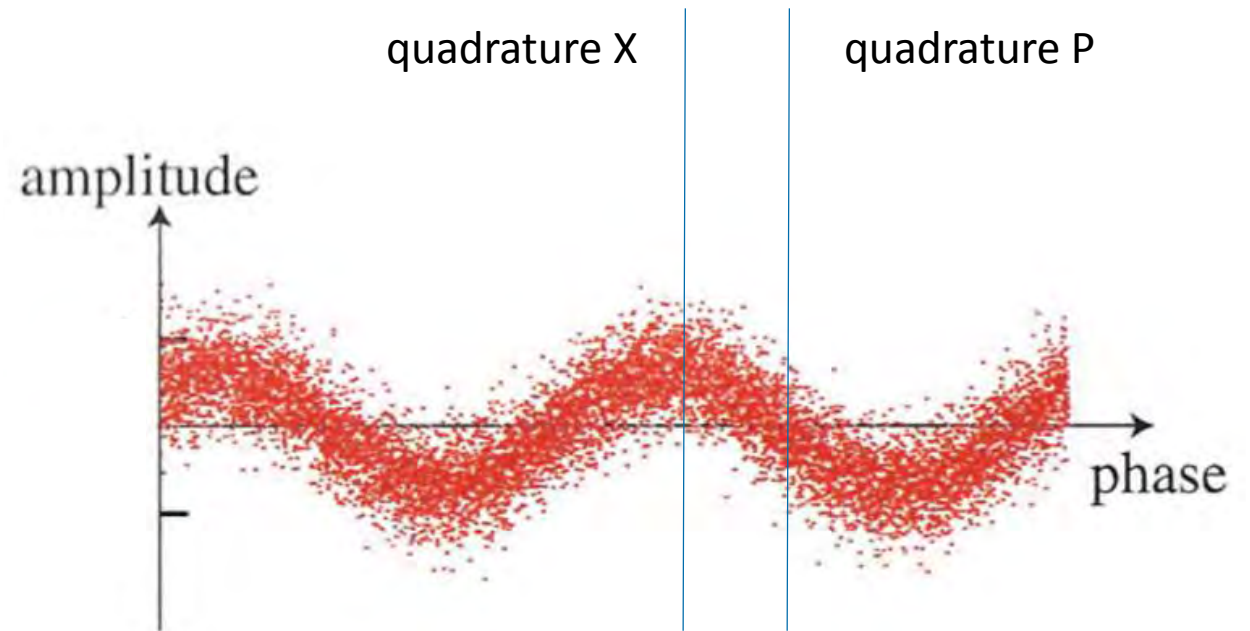
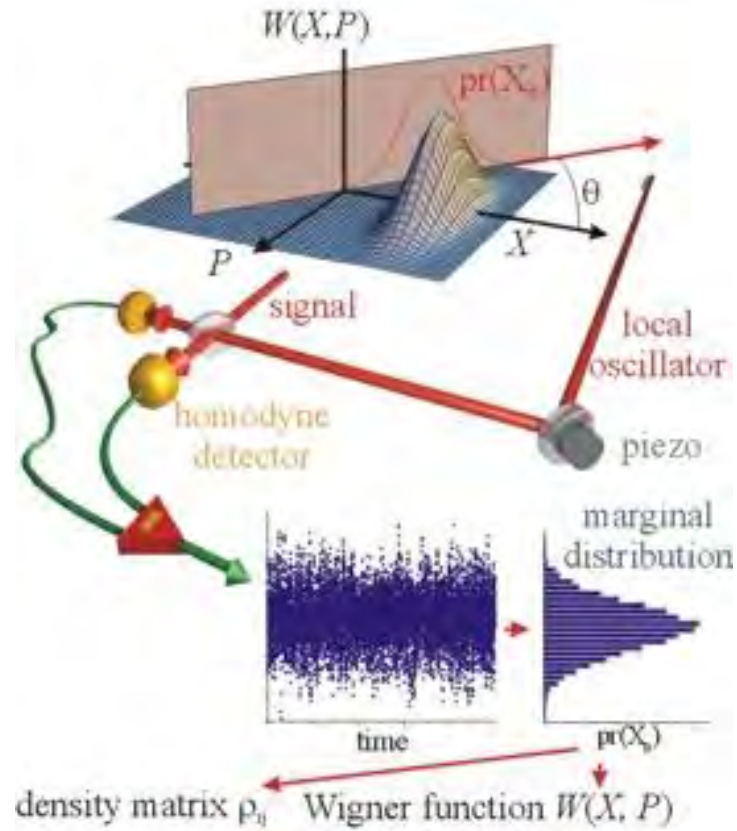
Homodyne detection
(from A. Lvovsky's web)



data from Furusawa lab



INTRO: CV QUANTUM NOISE



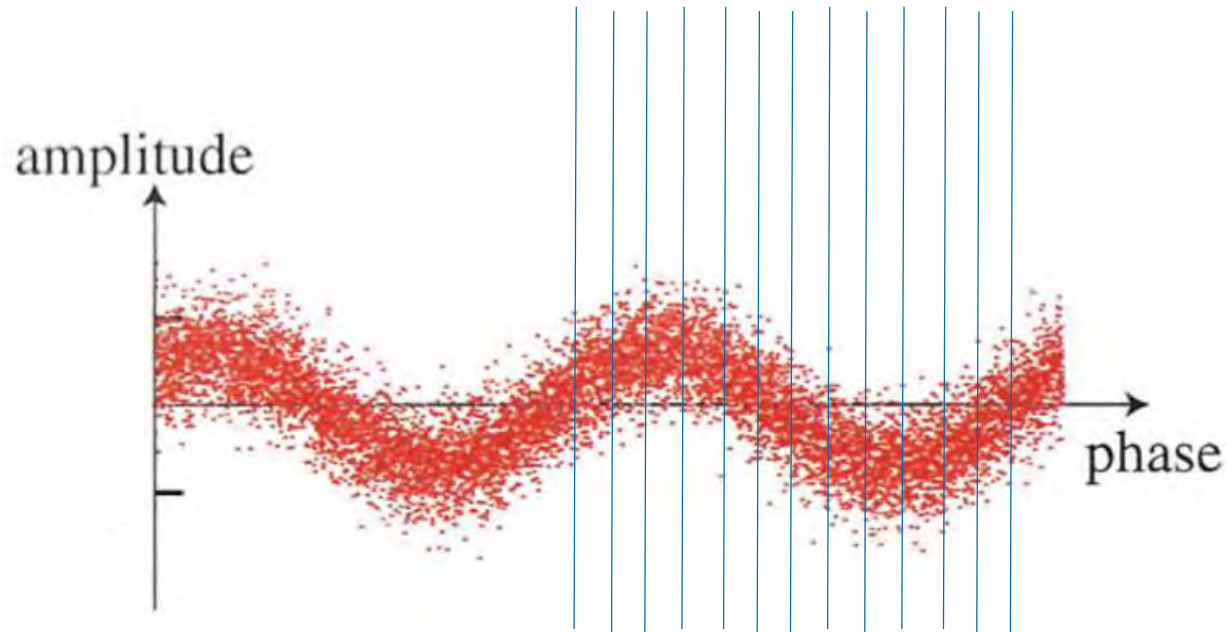
$$V_X V_P \geq 1 \quad [\hat{X}, \hat{P}] = 2i$$

Homodyne detection
(from A. Lvovsky's web)



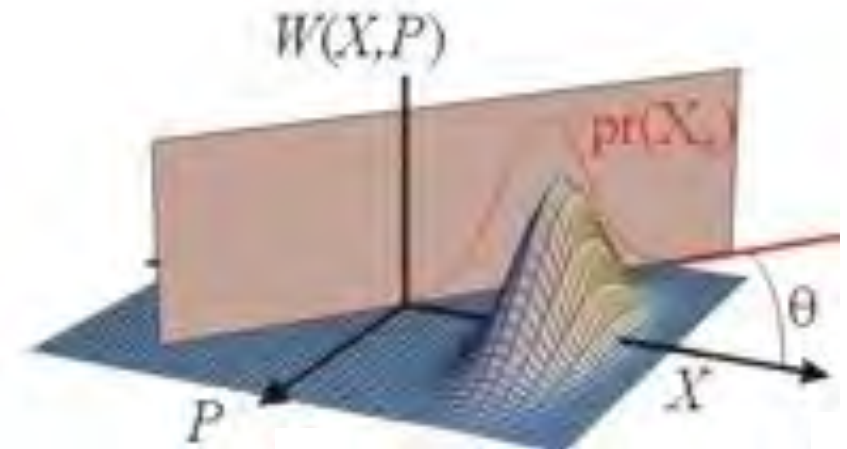
INTRO: CV QUANTUM NOISE

quantum tomography



X_θ

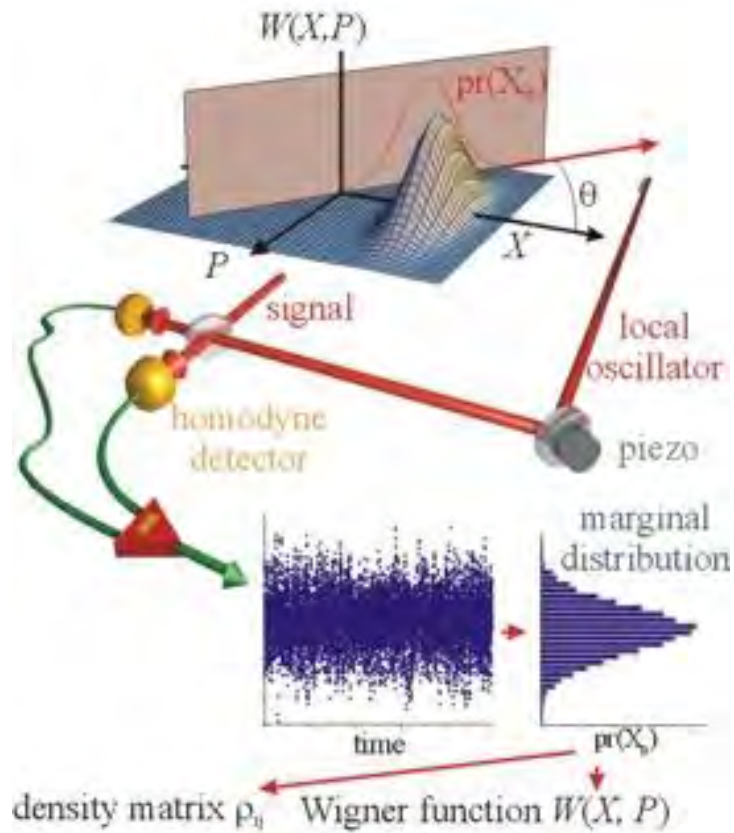
Wigner function



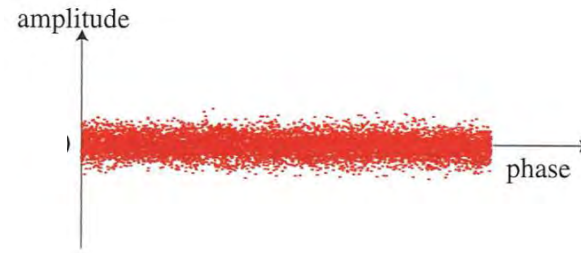
$$W(x, p) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \langle x - x' | \rho | x + x' \rangle \exp(ix'p) dx'$$



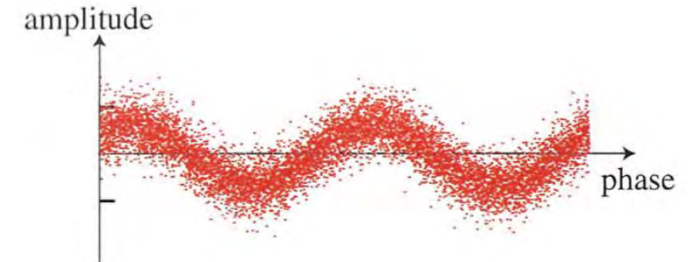
INTRO: CV QUANTUM NOISE



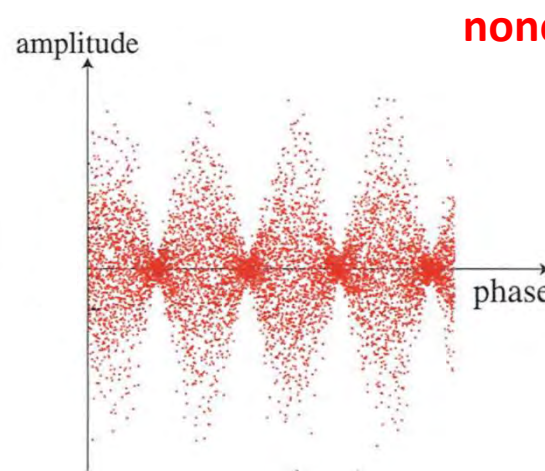
Homodyne detection
(from A. Lvovsky's web)



vacuum state



coherent state



nonclassical squeezed state

nonclassical states:

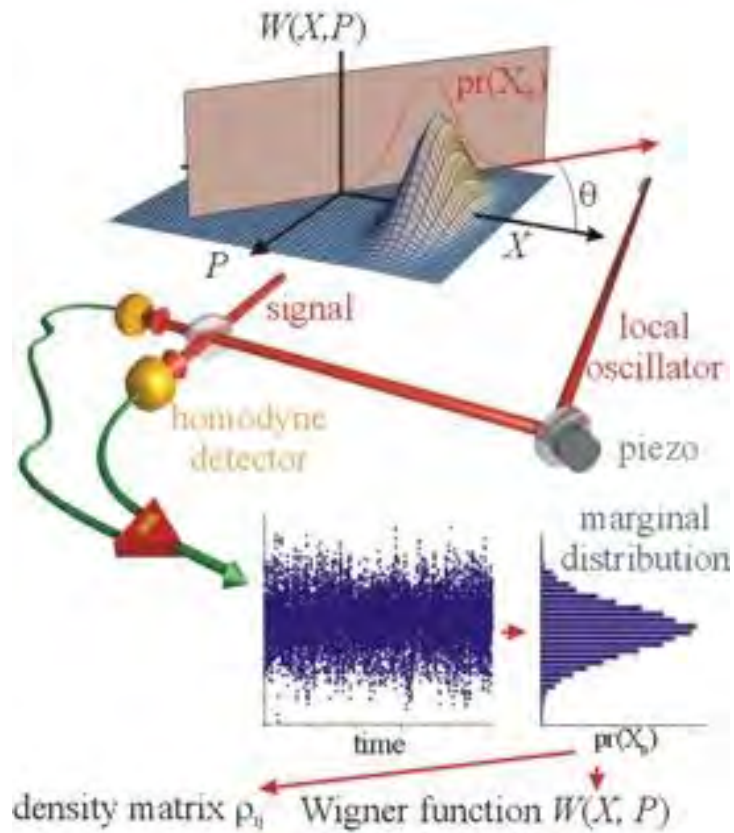


nonclassical Fock $|1\rangle$ state

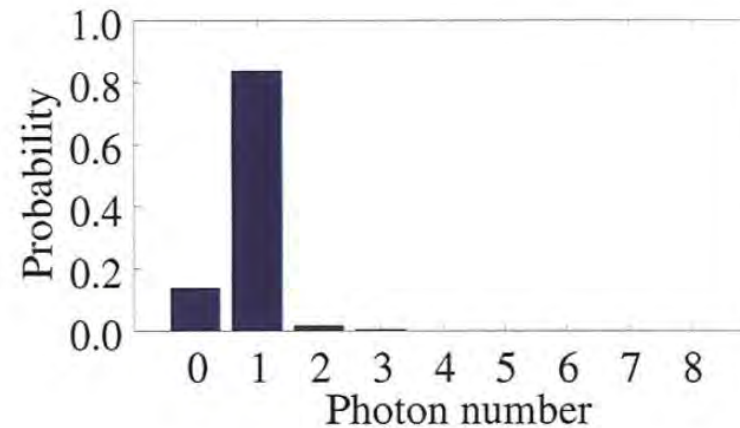
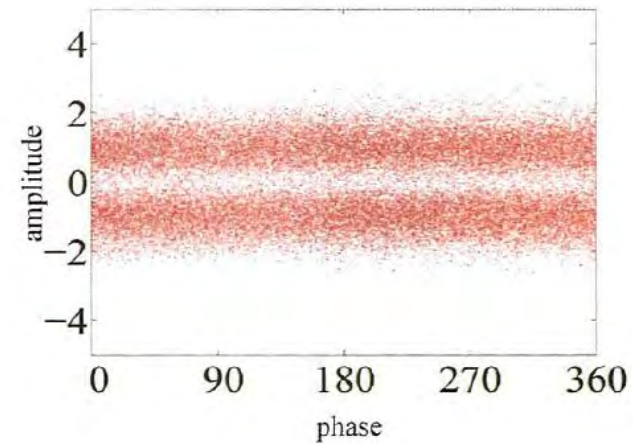
data from Furusawa lab



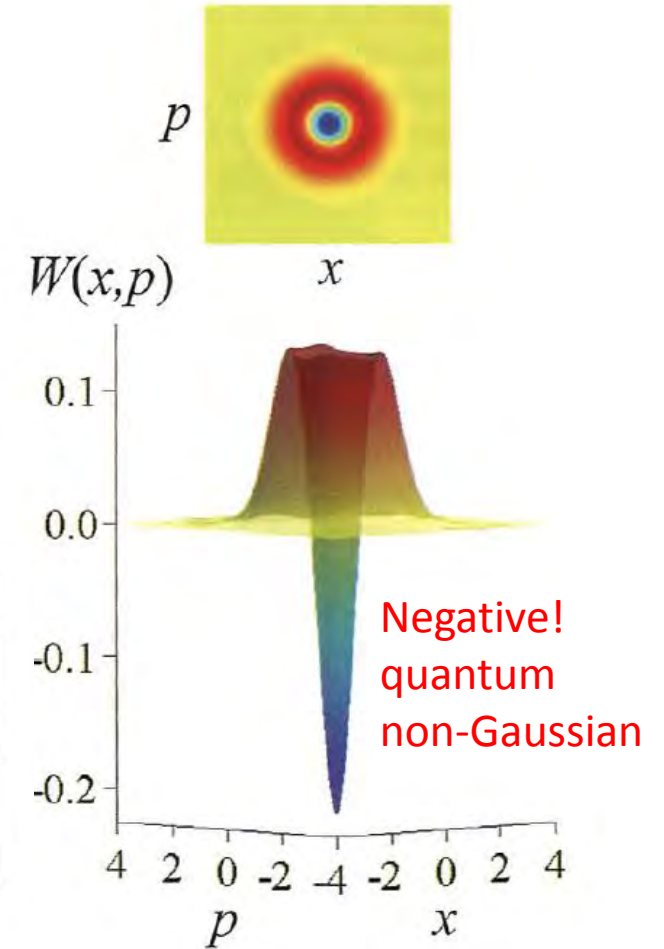
INTRO: CV QUANTUM NOISE



Homodyne detection
(from A. Lvovsky's web)



High quality single photon state

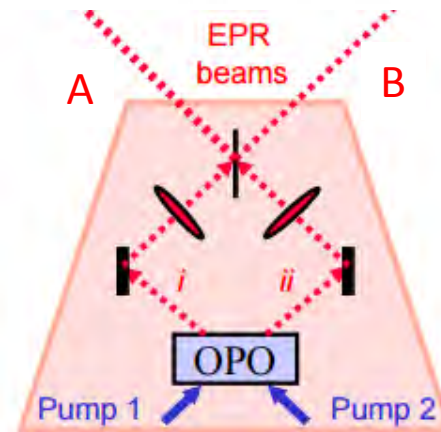
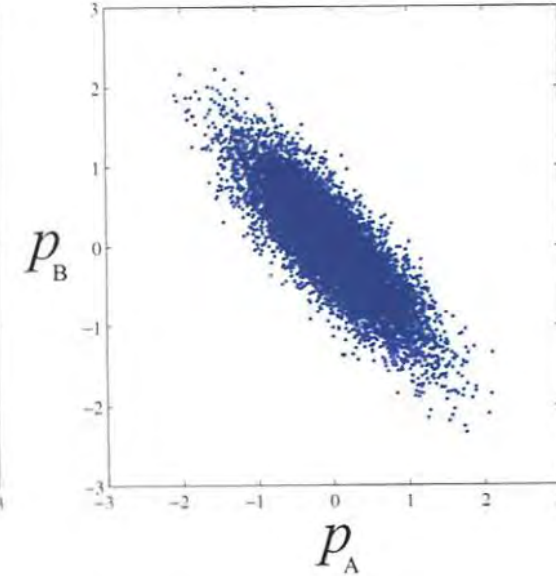
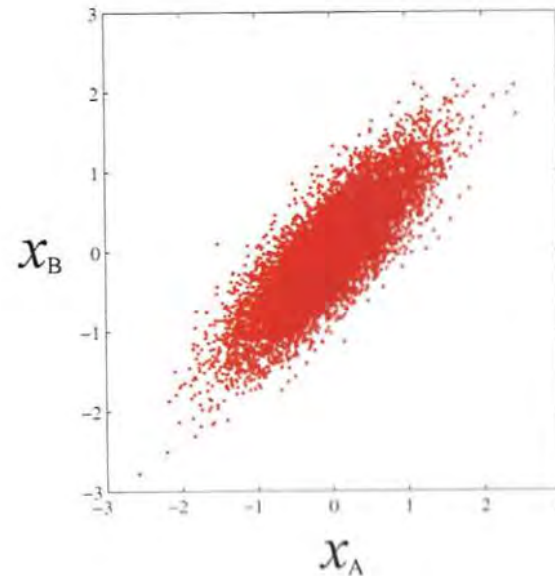
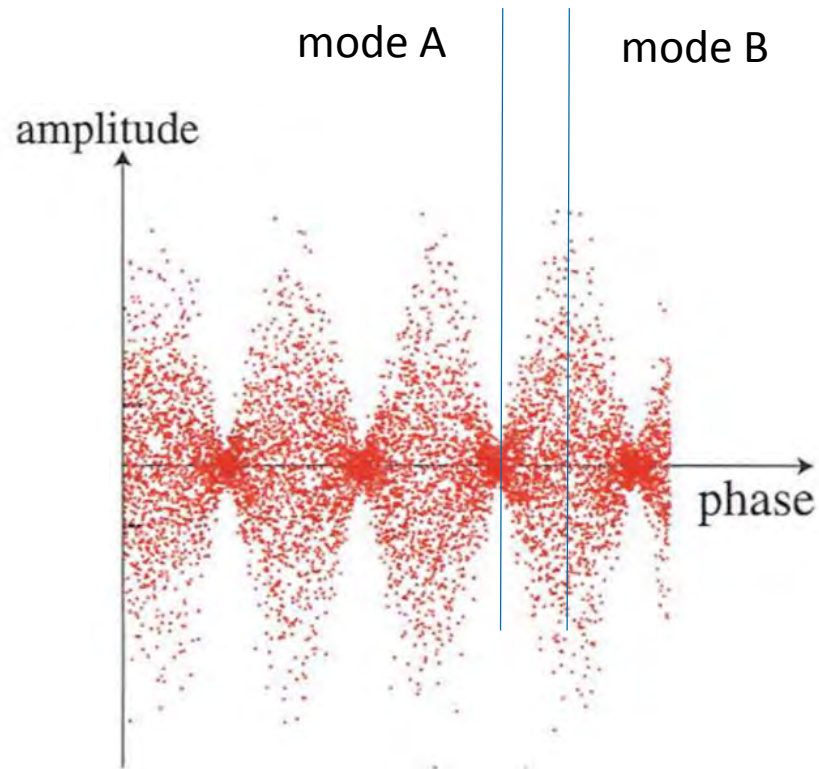


data from Furusawa lab



INTRO: CV QUANTUM NOISE

quantum interference at beam splitter



EPR quantum entanglement

$$V(x_A - x_B) \rightarrow 0$$

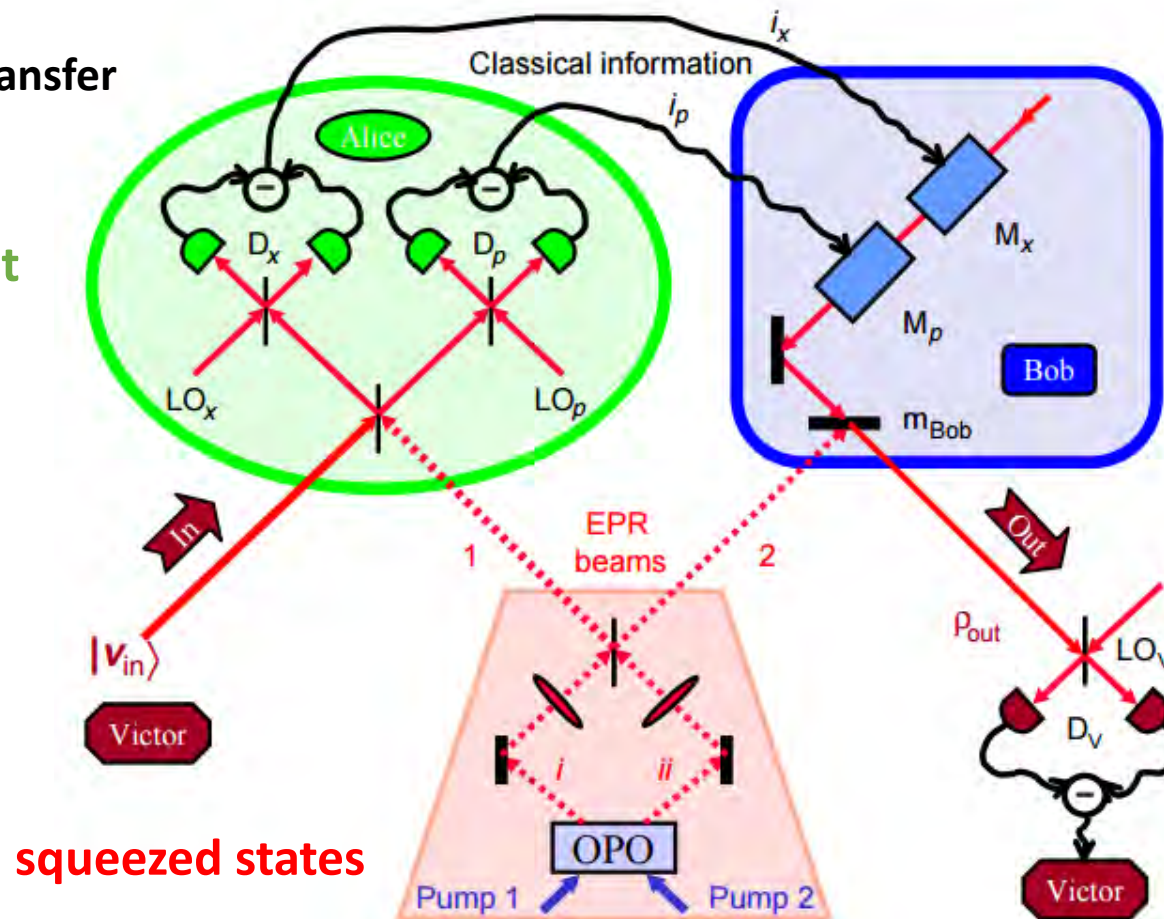
$$V(p_A + p_B) \rightarrow 0$$



INTRO: CV QUANTUM NOISE

quantum teleportation =
measurement-induced transfer

measurement
(erasing)



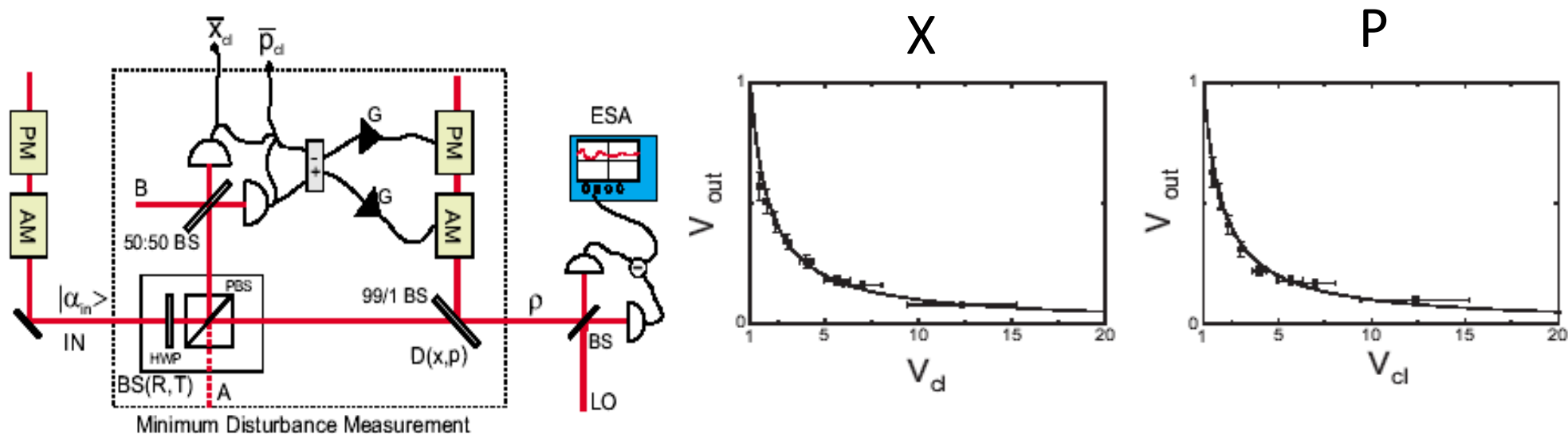
Electro-optical quantum
control

squeezed states



CV QUANTUM MEASUREMENT (OPERATION)

- CV quantum **measurement and erasing** using **squeezed light**, **homodyne detection**, linear optics and **quantum feedforward control**.
- **Minimum disturbance measurement** by linear optics, **homodyne measurements** and **quantum feedforward control**.



U.L. Andersen, O. Glöckl, S. Lorenz, G. Leuchs, and R. Filip, Phys. Rev. Lett. 93, 100403 (2004)

U.L. Andersen, M. Sabuncu, R. Filip, G. Leuchs, Phys. Rev. Lett. 020409 (2006).

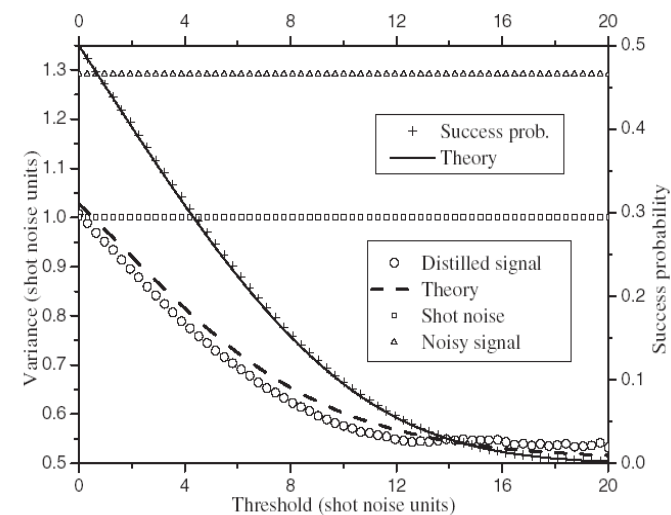
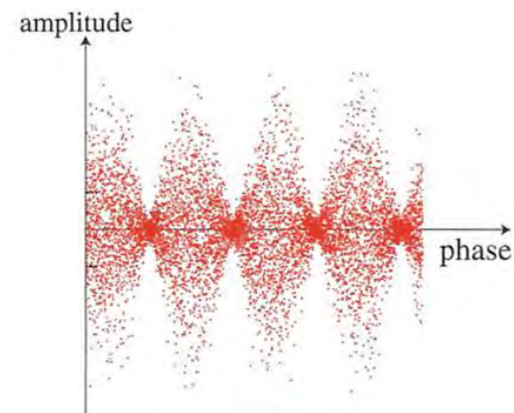
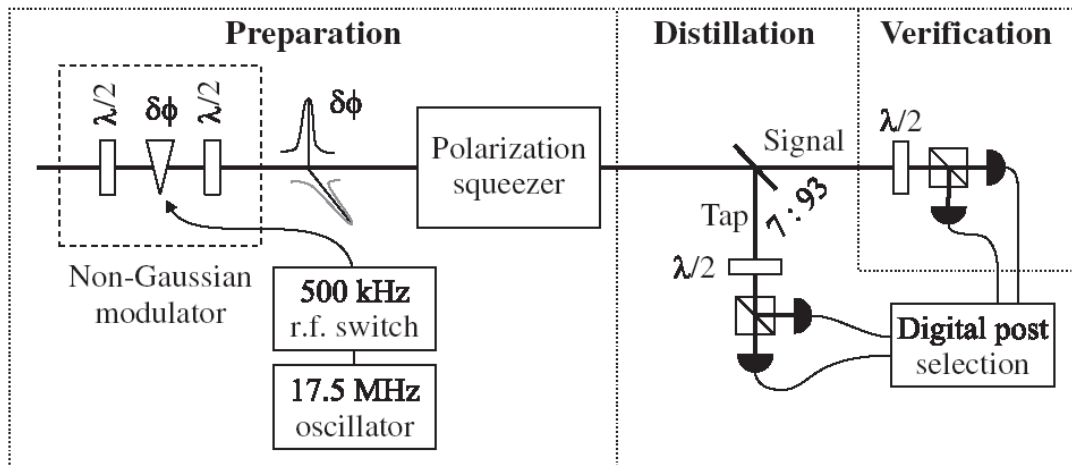


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CV QUANTUM DISTILLATION BY WEAK MEASUREMENT

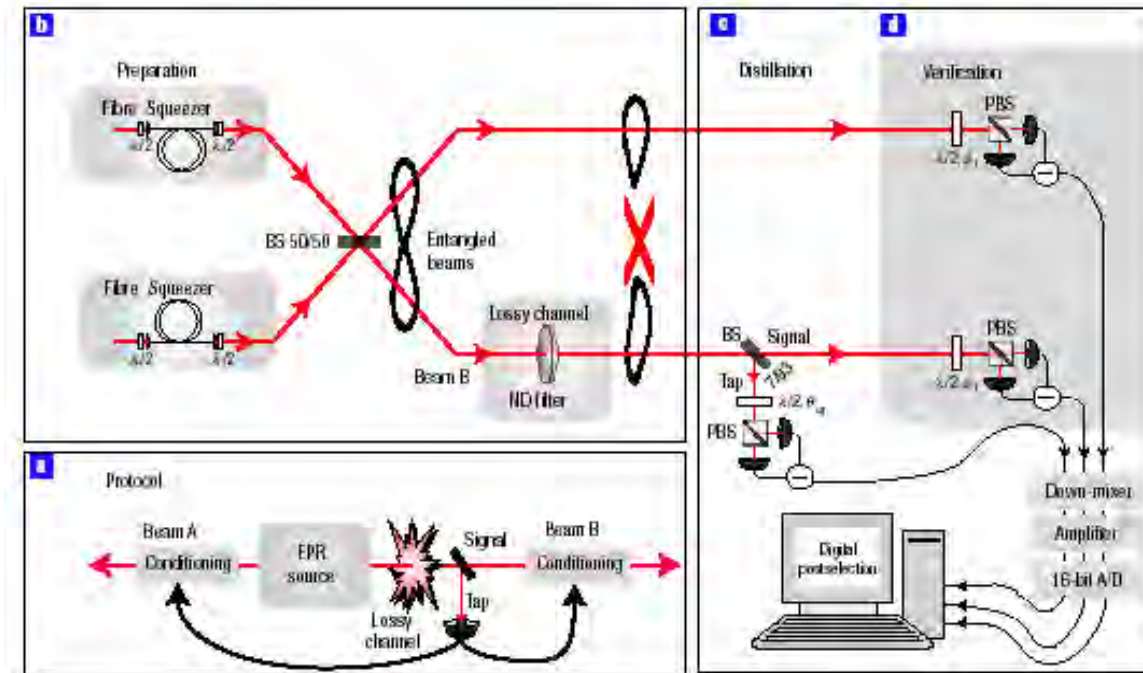
Quantum squeezing is **reduced or lost** by fluctuating pump or fading in transmission channel.

Distillation by **measurement** can recover it.



J. Heersink, Ch. Marquardt, R. Dong, R. Filip, S. Lorenz, G. Leuchs and U. L. Andersen, Phys. Rev. Lett. **96**, 253601 (2006).

CV ENTANGLEMENT DISTILLATION

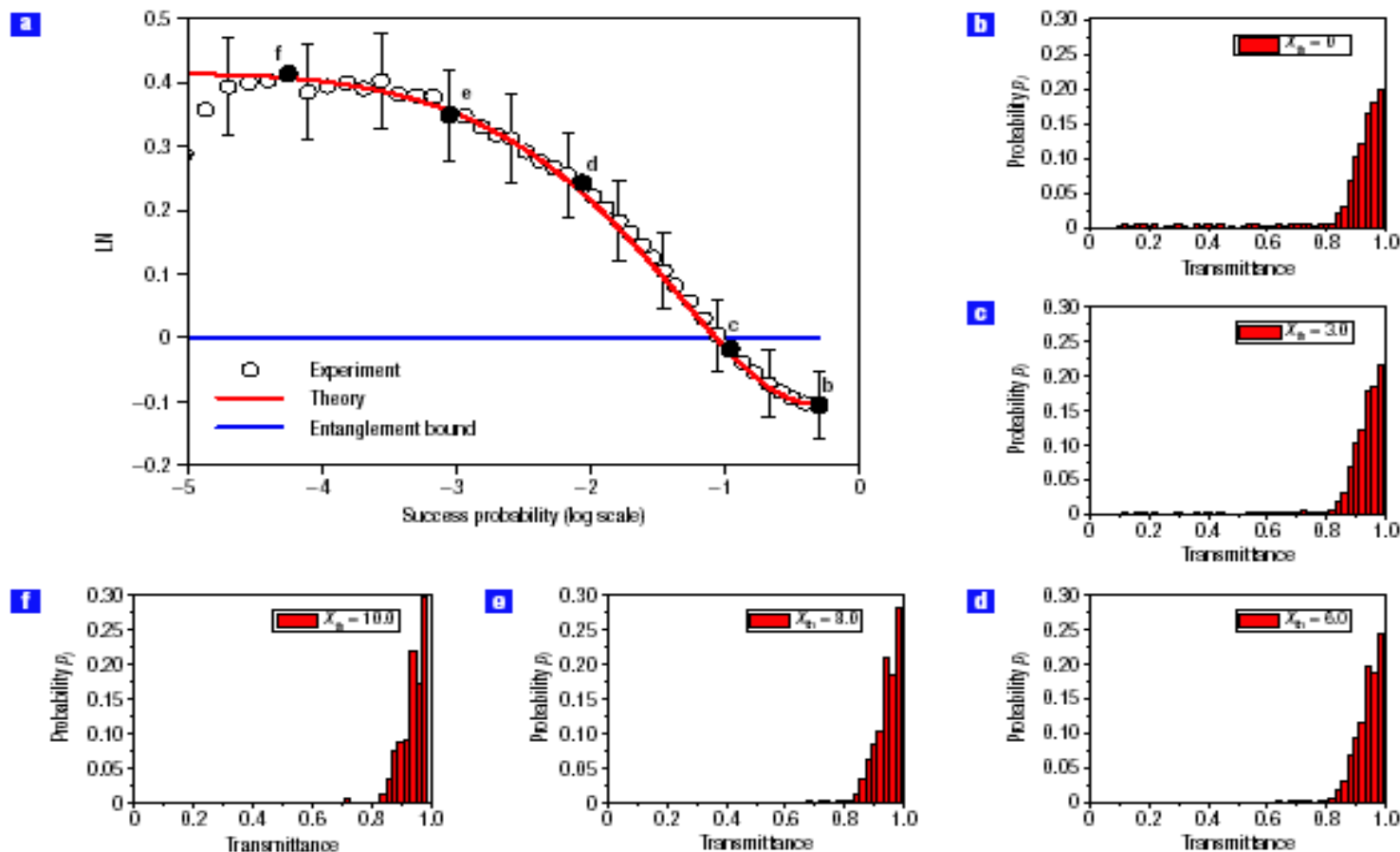


- Quantum entanglement **vanishes** by fading in free-space transmission channel.
- **Distillation** by **measurement** can recover quantum entanglement.

R.-F. Dong, M. Lassen, J. Heersink, Ch. Marquardt, R. Filip, G. Leuchs and U.L. Andersen,
Nature Physics 4, 919 (2008).



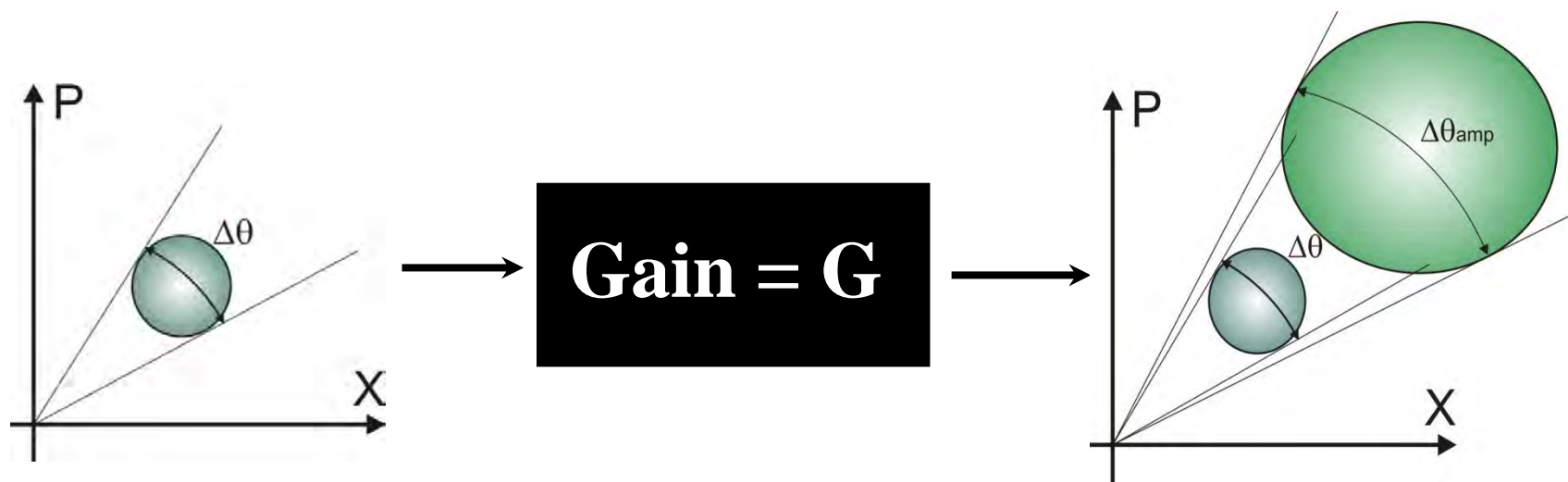
CV ENTANGLEMENT DISTILLATION



R.-F. Dong, M. Lassen, J. Heersink, Ch. Marquardt, R. Filip, G. Leuchs and U.L. Andersen,
Nature Physics 4, 919 (2008).



QUANTUM AMPLIFICATION

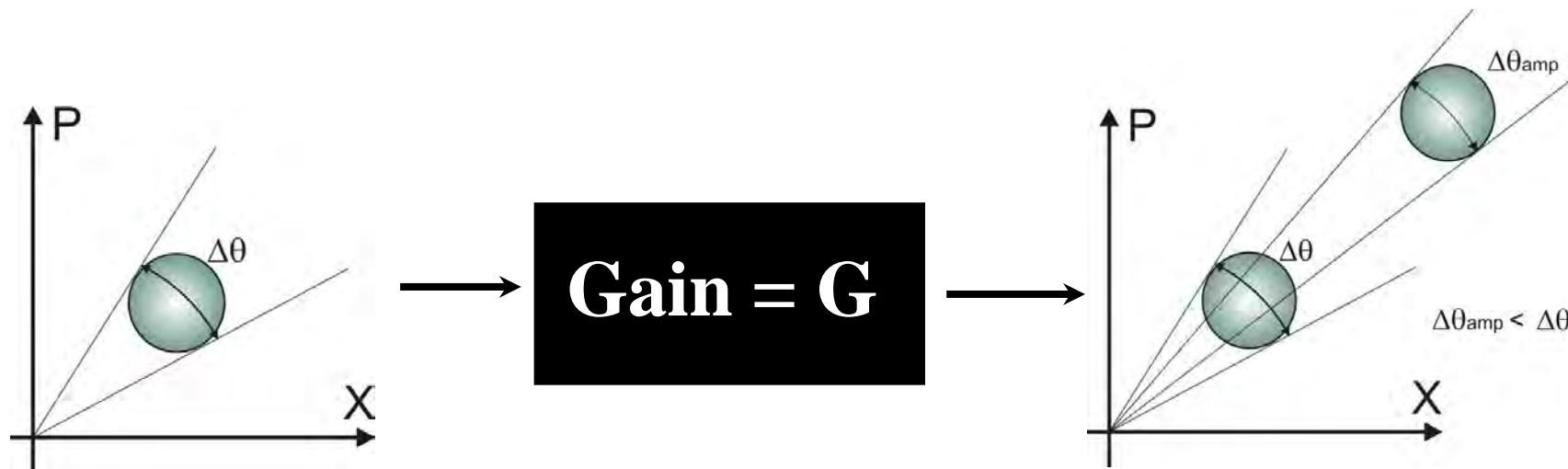


Quantum operation:

$$a_{out} = \sqrt{G}a_{in} + \sqrt{G-1}v^+$$



NOISELESS AMPLIFICATION



Unphysical operation:

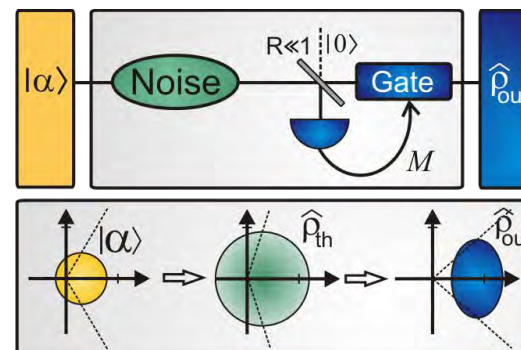
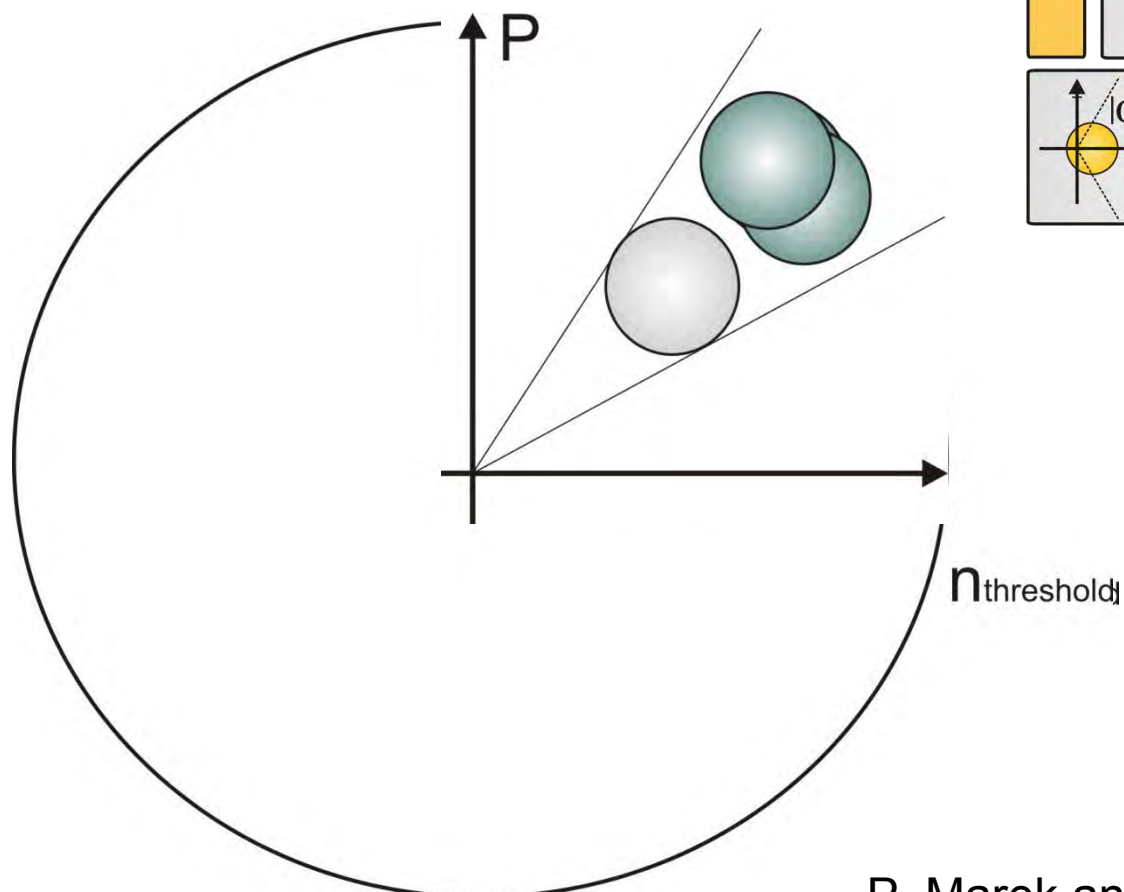
$$a_{out} = \sqrt{G}a_{in} + \sqrt{G-1}v^+$$



Who first asked this question?

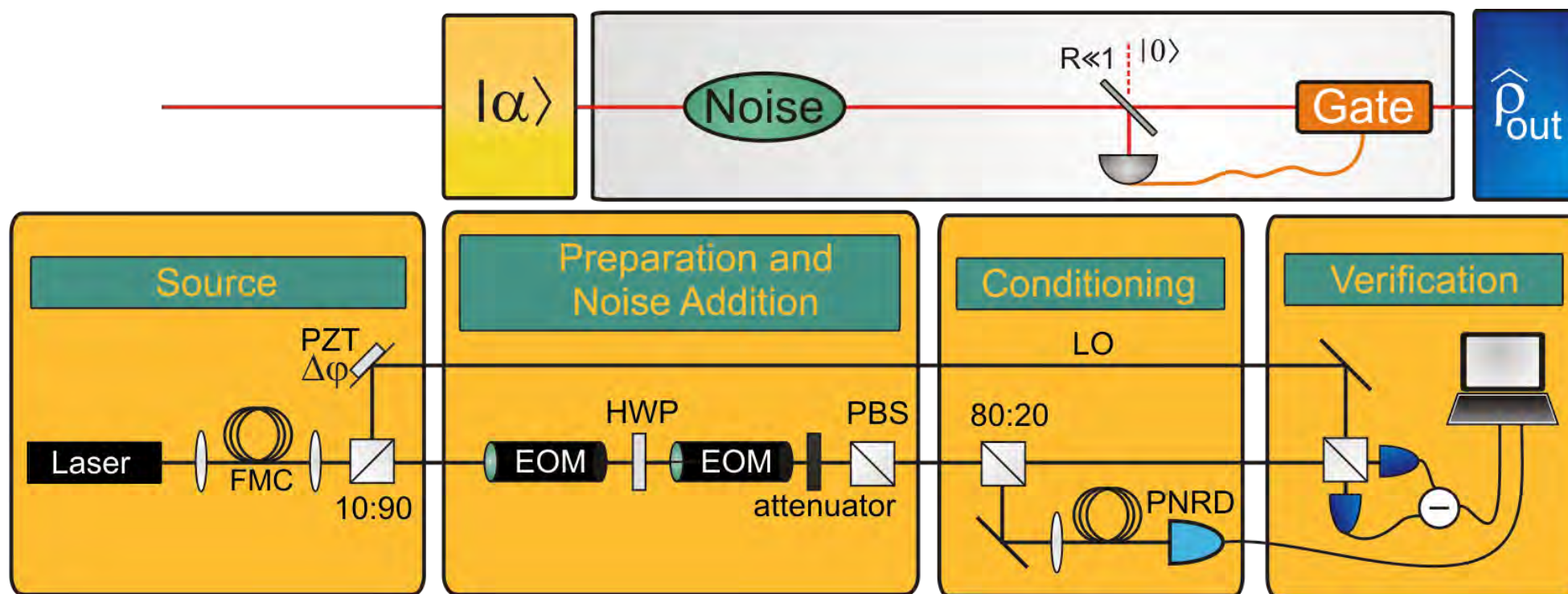


NOISELESS AMPLIFICATION



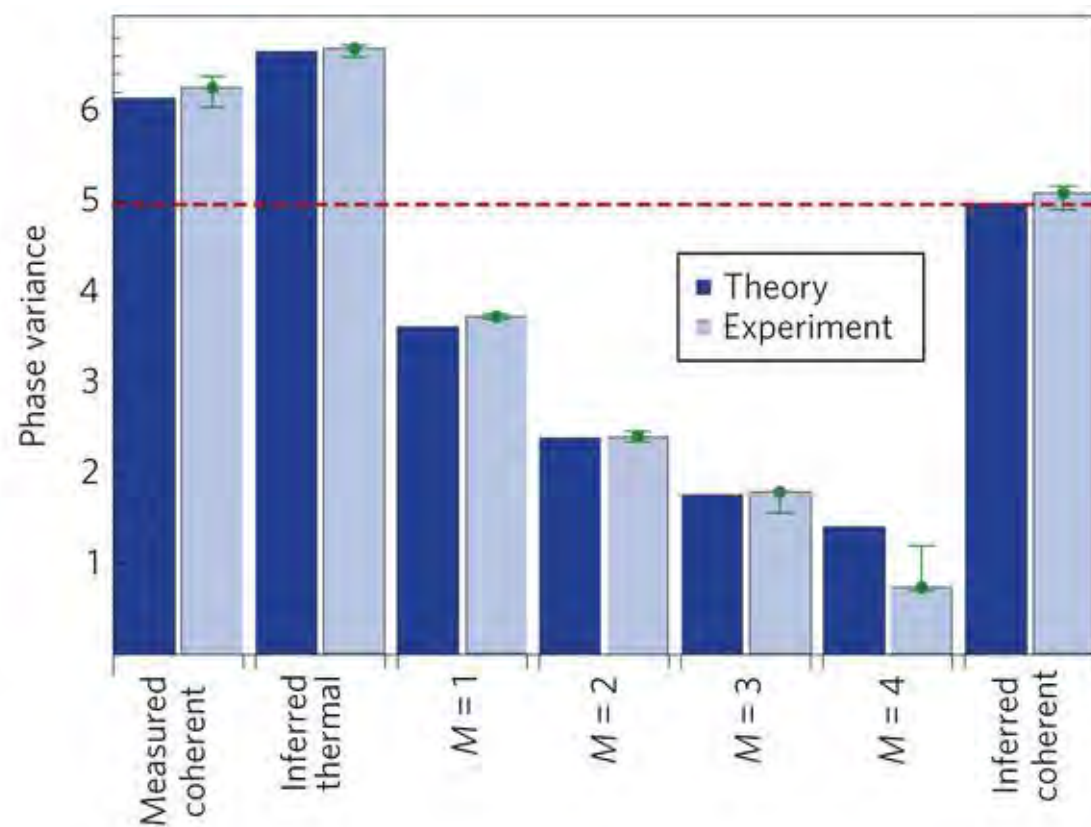
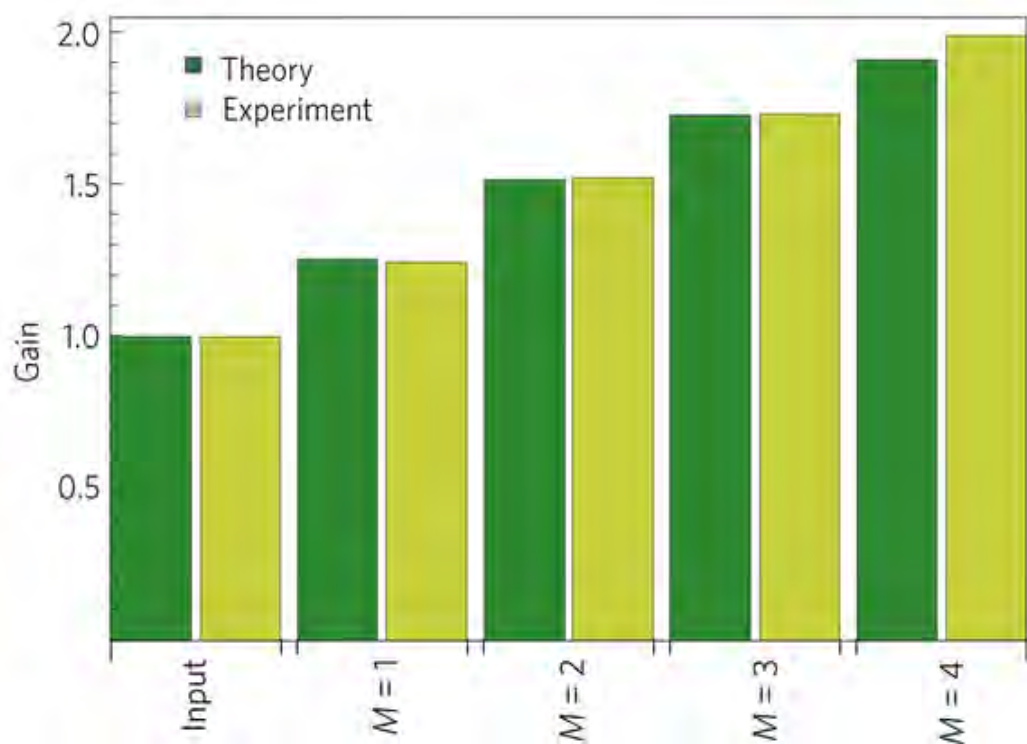


NOISELESS AMPLIFICATION



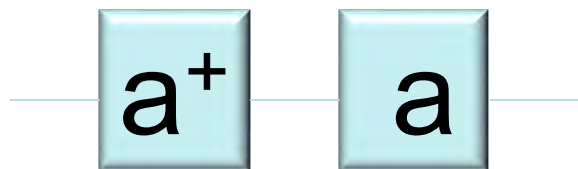


NOISELESS AMPLIFICATION





NOISELESS AMPLIFICATION



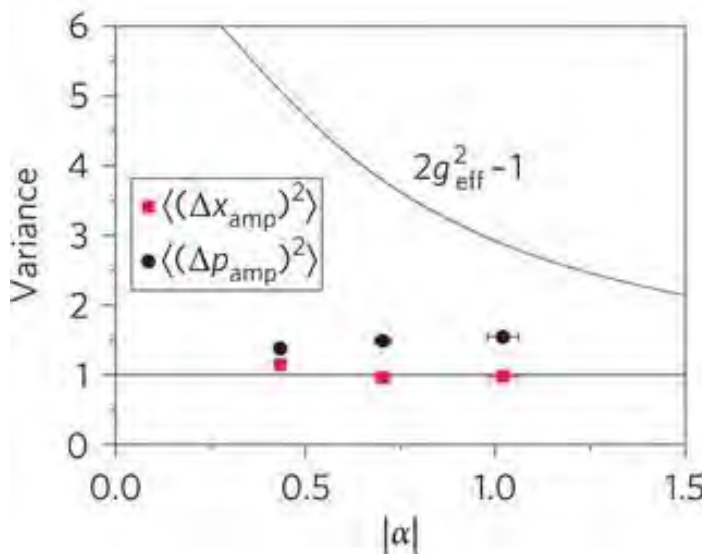
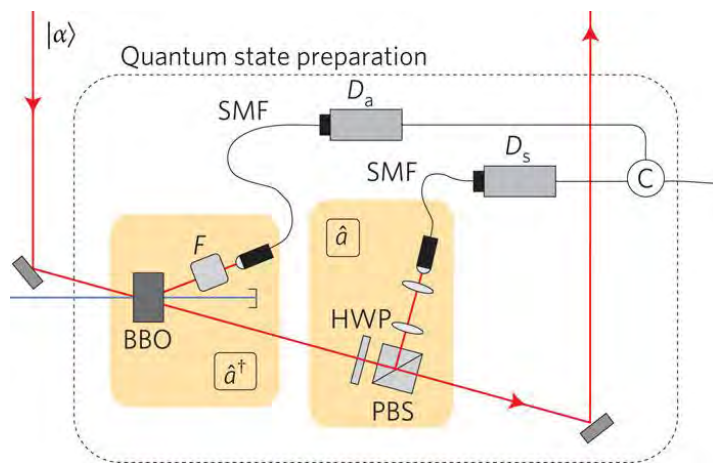
$$|\alpha\rangle = |0\rangle + \alpha|1\rangle + \dots$$

$$a^+|\alpha\rangle = |1\rangle + 2^{1/2} \alpha|2\rangle + \dots$$

$$aa^+|\alpha\rangle = |0\rangle + 2\alpha|1\rangle + \dots$$

$$\rightarrow g^{\hat{n}}, g > 1$$

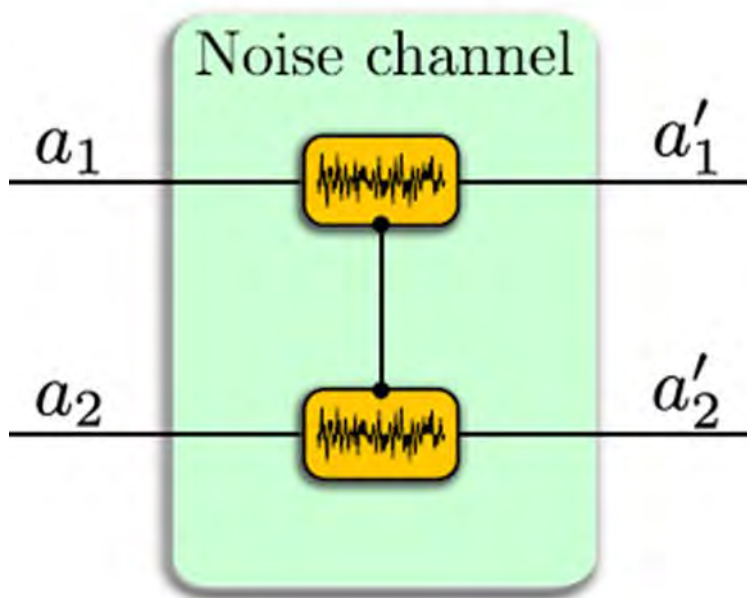
P. Marek and R. Filip, Phys. Rev. A 81, 022302 (2010).



A. Zavatta, J. Fiurášek, M. Bellini, Nature Phot. 5, 52 (2011)



ERROR CORRECTION FOR CHANNEL WITH CLASSICALLY CORRELATED NOISE



Asymmetrical
loss channels

$$\hat{a}'_1 = \sqrt{\eta_1} \hat{a}_1 + \sqrt{1 - \eta_1} \hat{v}_1 + \sqrt{g_1} v_C$$

$$\hat{a}'_2 = \sqrt{\eta_2} \hat{a}_2 + \sqrt{1 - \eta_2} \hat{v}_2 + \sqrt{g_2} v_C$$

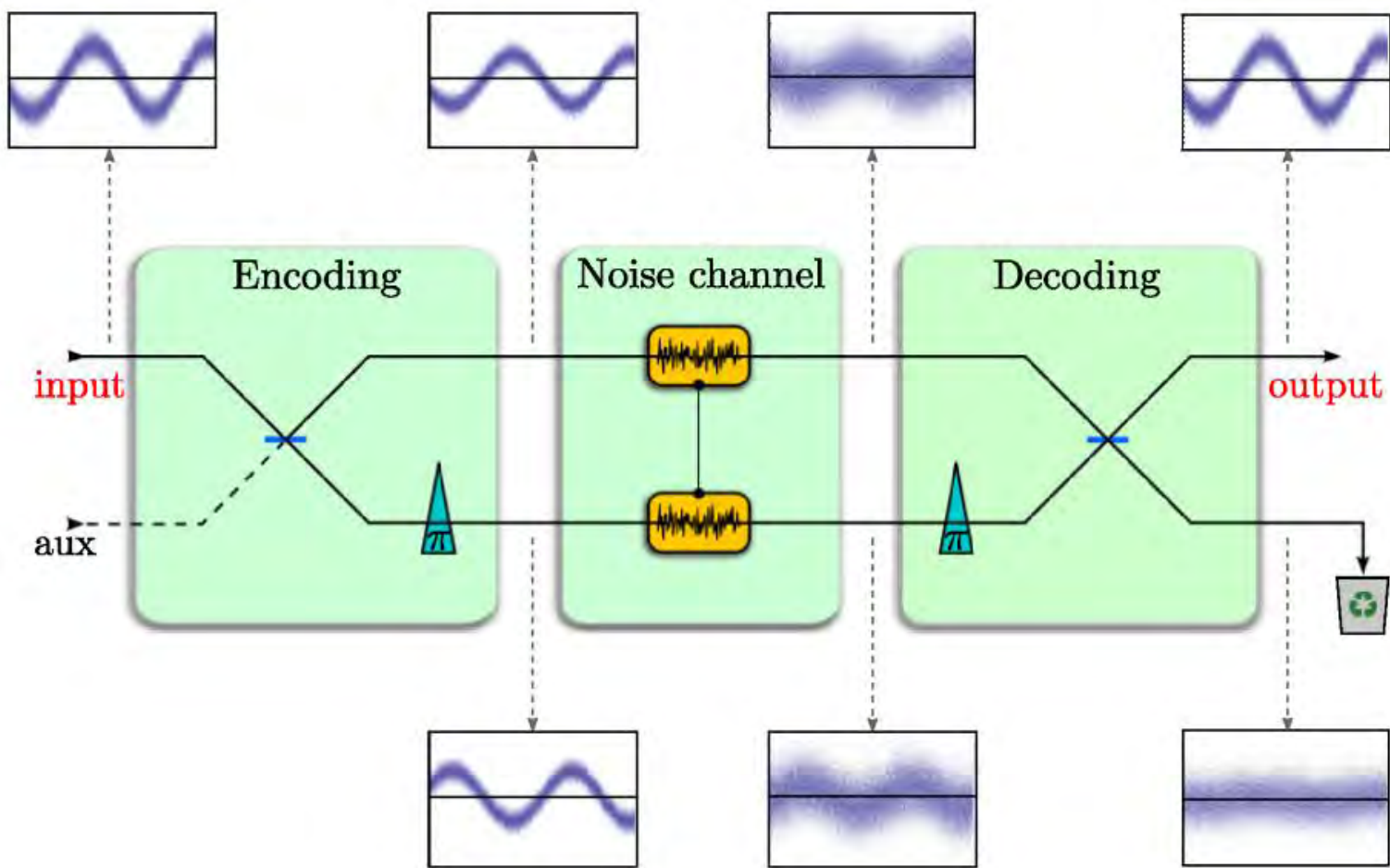
Asymmetrical
perfectly uncorrelated noise

Asymmetrical
perfectly correlated noise



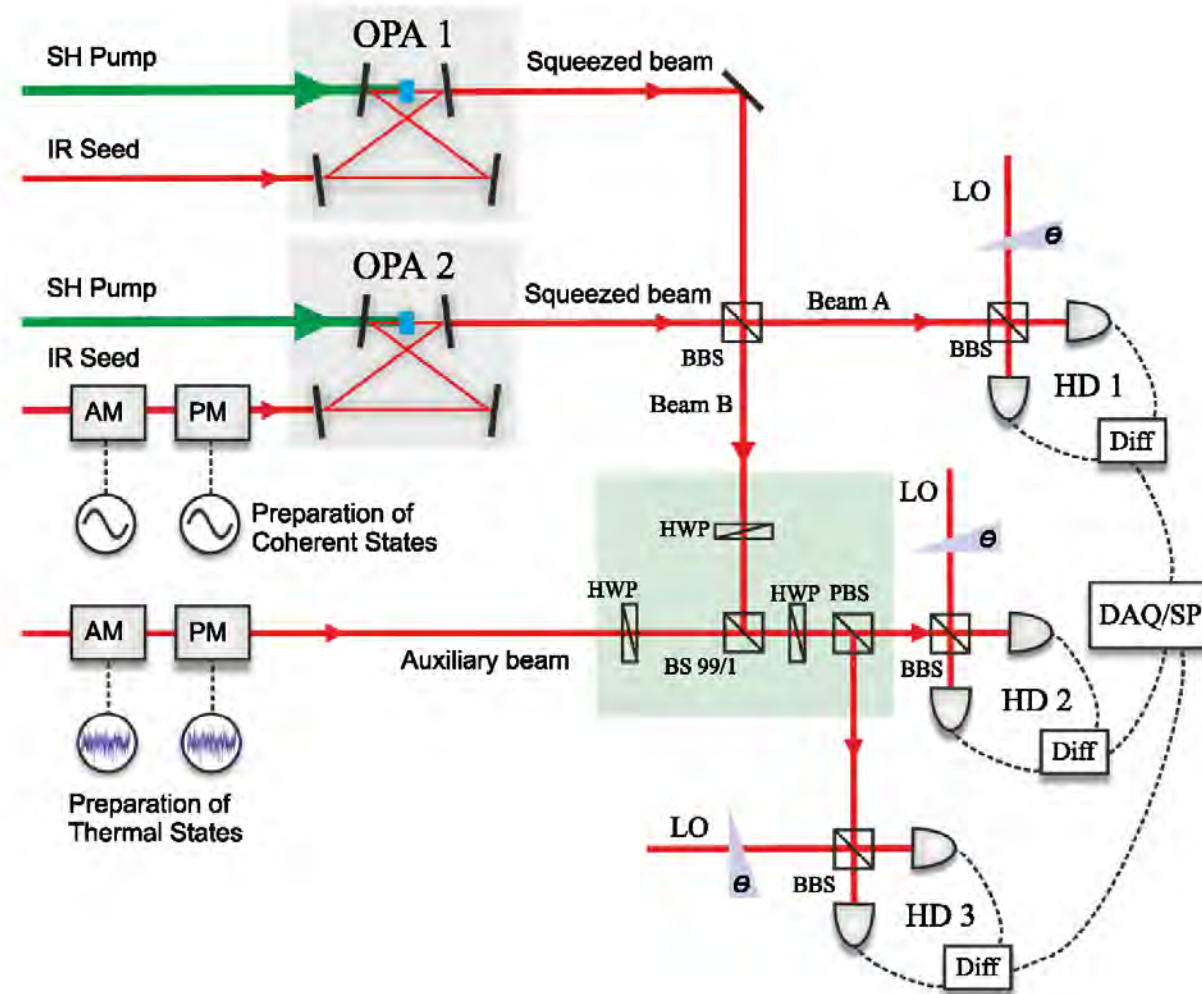
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ERROR CORRECTION FOR CHANNEL WITH CLASSICALLY CORRELATED NOISE



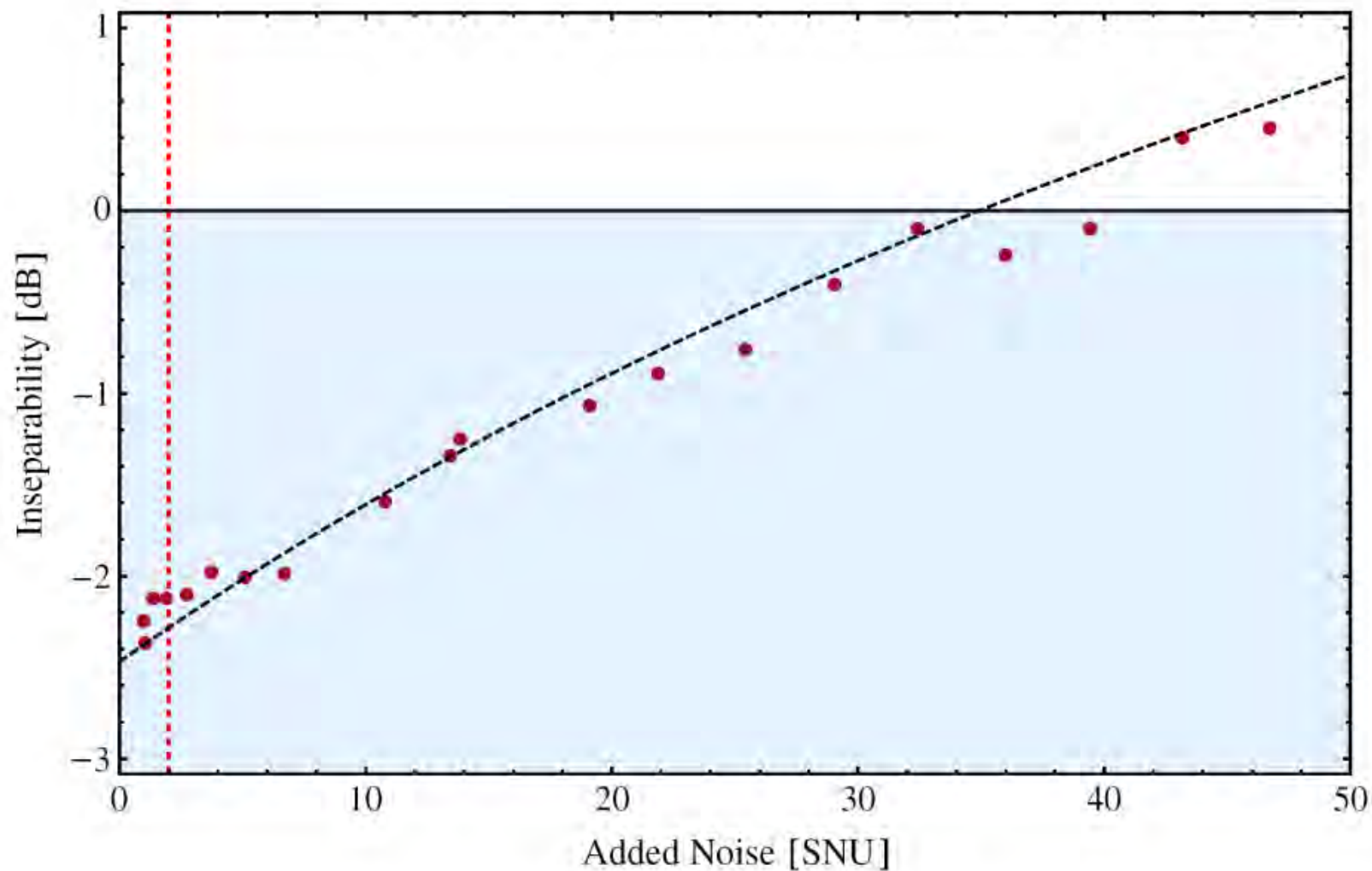


ERROR CORRECTION FOR CHANNEL WITH CLASSICALLY CORRELATED NOISE



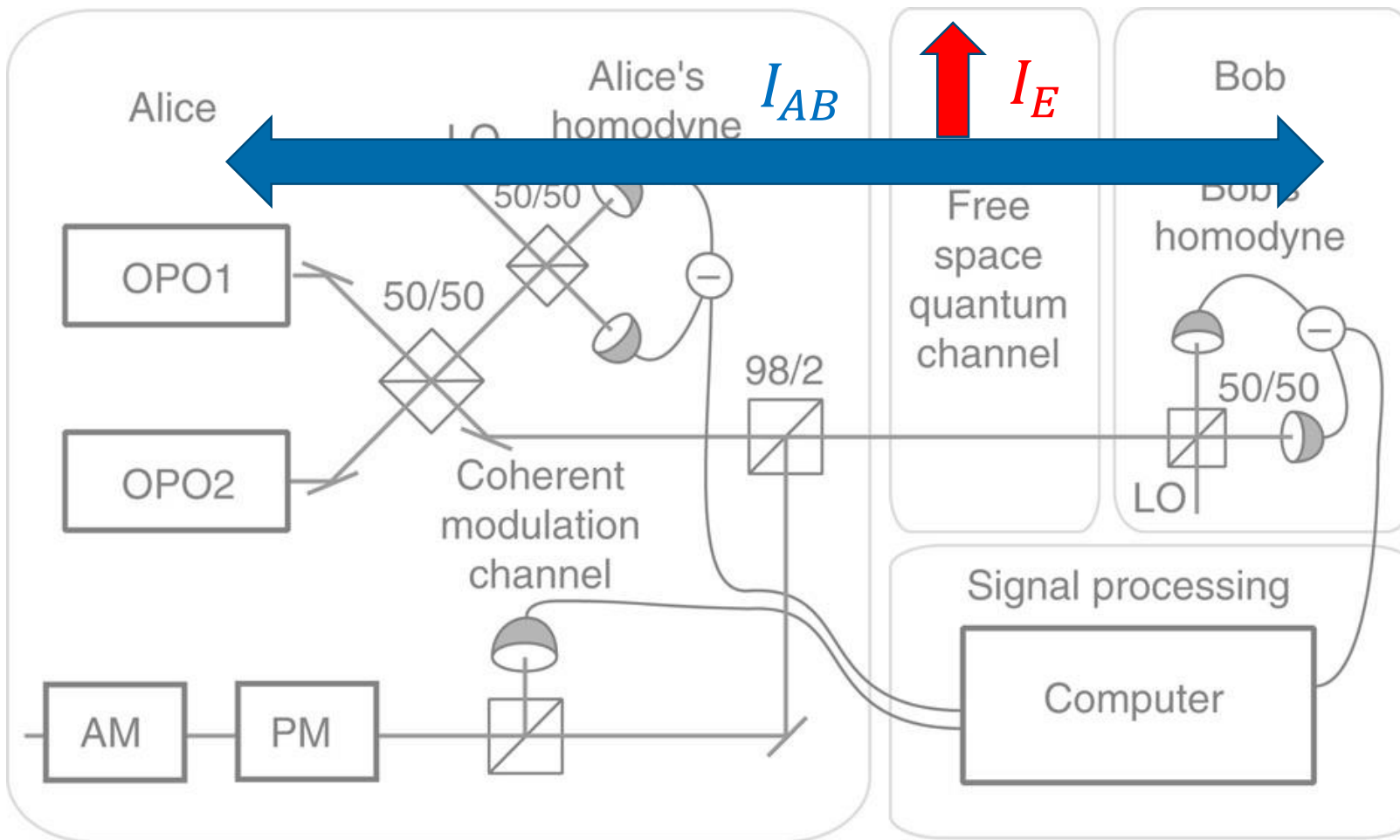


ERROR CORRECTION FOR CHANNEL WITH CLASSICALLY CORRELATED NOISE





APPLICATION: CV QKD



$$I_{AB} > I_E$$

Csiszár and Körner's theorem

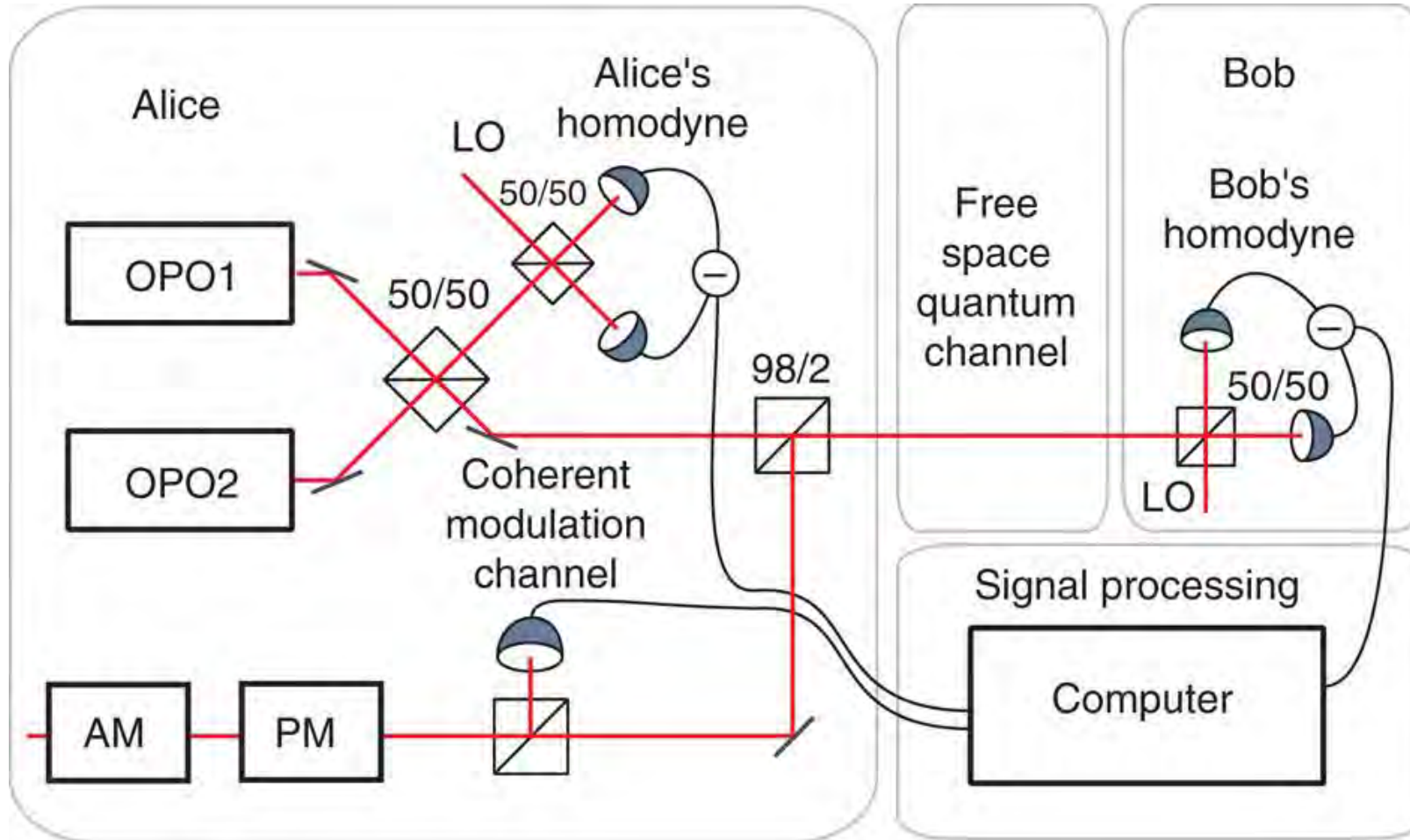
$$K = \beta I_{AB} - I_E$$

secure key rate

F. Grosshans et al.,
Quantum key distribution
using gaussian-modulated
coherent states, Nature
421, 238 (2003).



APPLICATION: ENTANGLED STATE CV QKD

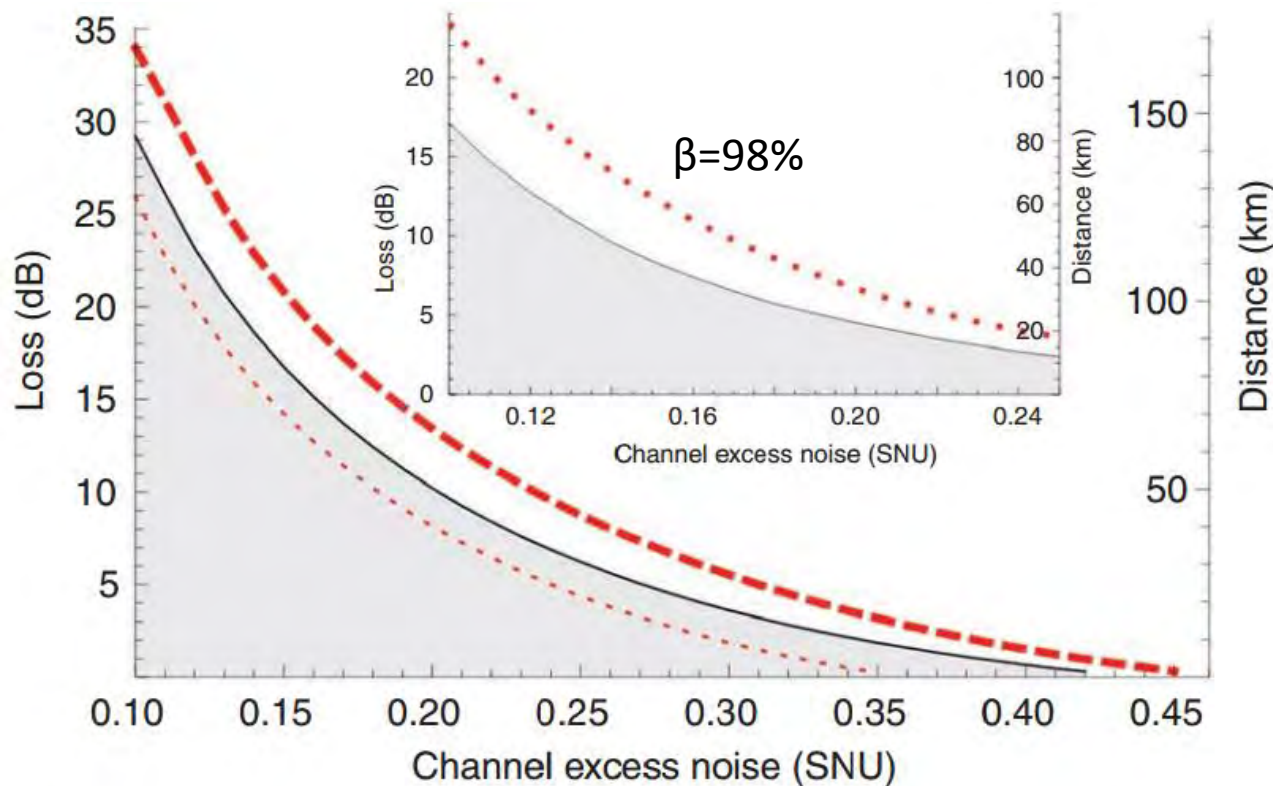




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APPLICATION: ENTANGLED STATE QKD

It overcomes coherent state protocol.
Entanglement allows larger distance.

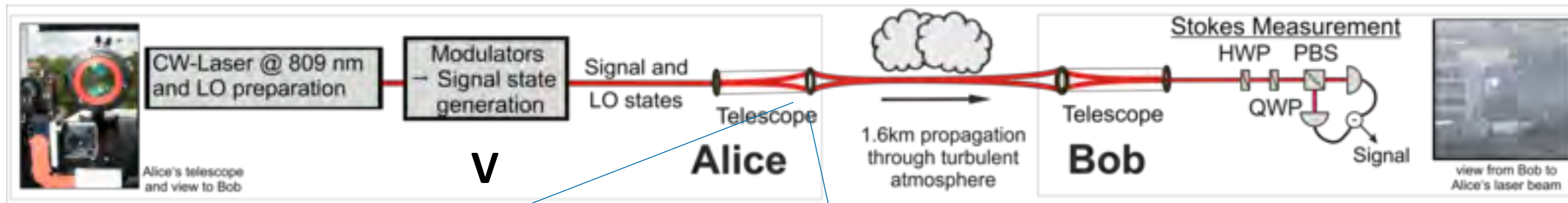


3.5 dB two-mode squeezing



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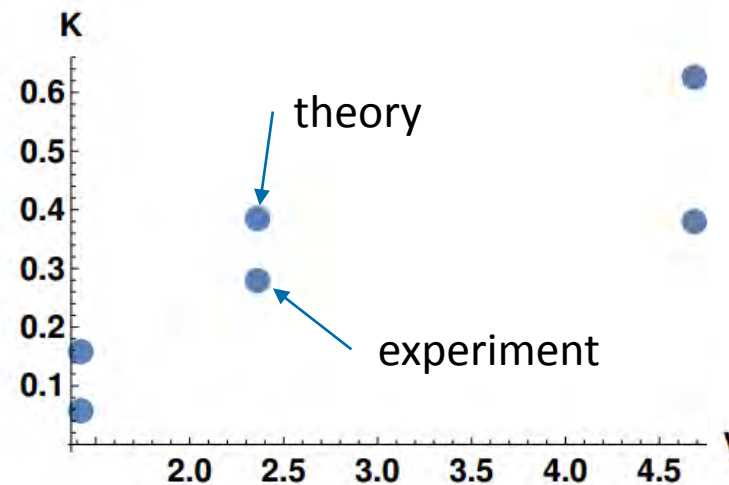
NEXT: FREE-SPACE CV QKD



V



First data of CV free-space coherent state QKD





SUMMARY



- Minimal disturbance quantum measurements
- Quantum distillation of squeezing and entanglement
- Noiseless quantum amplification
- Quantum error correction for correlated noise
- Entangled based quantum key distribution
- Universal squeezer and its applications
- Optimal non-Gaussian state manipulation
- Amplification of optomechanical coupling
- Deterministic cubic quantum operation
- Simulations of quantum nonlinearity
- Noise enhanced quantum effects